

Physics 590 Homework, Week 2

Week 2, Homework 1

Prob. 2.1.1

A race car can be slowed with a deceleration of -11 m/s^2 . (a) If it is going $+55 \text{ m/s}$, how many meters will it take to stop? (b) Repeat part (a) for a car going 110 m/s .

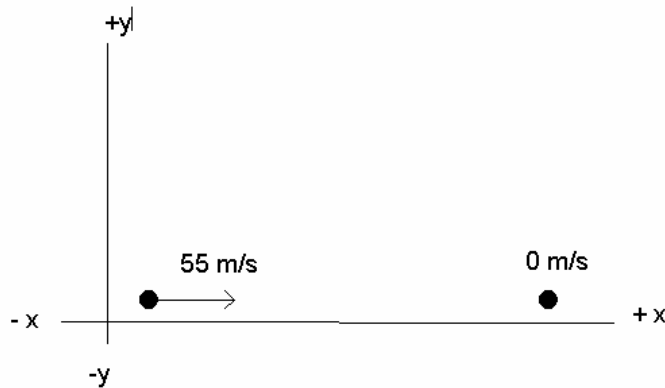
a) $v_f^2 = v_i^2 + 2ad$

$v_{\text{final}} = 0 \text{ m/s}$

$v_{\text{initial}} = 55 \text{ m/s}$

$a = -11 \text{ m/s}^2$

$d = ?$



$$(0 \text{ m/s})^2 = (55 \text{ m/s})^2 + 2(-11 \text{ m/s}^2)d$$

$$0 = (3025 \text{ m}^2/\text{s}^2) - 22 \text{ m/s}^2 * d$$

$$(-3025 \text{ m}^2/\text{s}^2) = -22 \text{ m/s}^2 * d$$

$$\frac{(-3025 \text{ m}^2/\text{s}^2)}{(-22 \text{ m/s}^2)} = d \rightarrow 137.5 \text{ m} = d \rightarrow$$

$d = 1.4 \times 10^2 \text{ m}$

b) $v_f^2 = v_i^2 + 2ad$

$v_{\text{final}} = 0 \text{ m/s}$

$v_{\text{initial}} = 110 \text{ m/s}$

$a = -11 \text{ m/s}^2$

$d = ?$

$$(0 \text{ m/s})^2 = (110 \text{ m/s})^2 + 2(-11 \text{ m/s}^2)d$$

$$0 = (12100 \text{ m}^2/\text{s}^2) - 22 \text{ m/s}^2 * d$$

$$(-12100\text{m}^2/\text{s}^2) = -22 \text{ m/s}^2 * d$$

$$\frac{(-12100\text{m}^2/\text{s}^2)}{-22 \text{ m/s}^2} = d \rightarrow 550 \text{ m} = d \rightarrow$$

$$d = 5.5 \times 10^2 \text{ m}$$

Prob. 2.1.2

An astronaut dropped a feather from 1.2 m above the surface of the moon. If the acceleration of gravity on the moon is 1.6 m/s^2 , how long did it take to hit the surface?

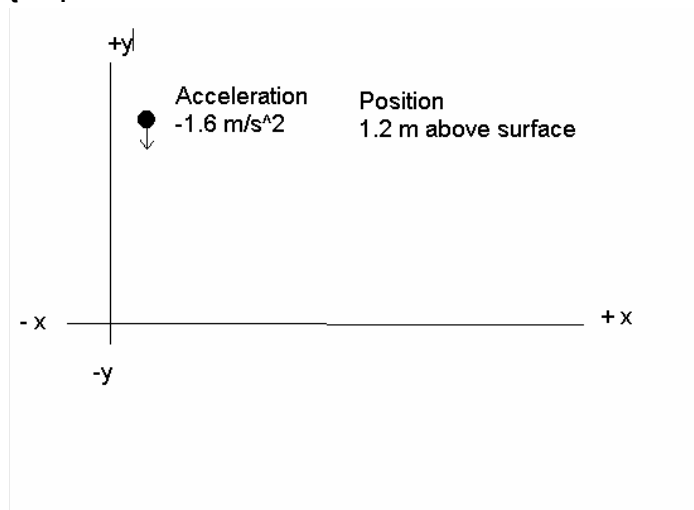
$$d = v_i * t + \frac{1}{2}at^2$$

$$d = 1.2 \text{ m}$$

$$a = 1.6 \text{ m/s}^2$$

$$v \text{ initial} = 0 \text{ m/s}$$

$$t = ?$$



$$1.2 \text{ m} = (0 \text{ m/s}) * t + \frac{1}{2}(1.6 \text{ m/s}^2) * t^2$$

$$1.2 \text{ m} = \frac{1}{2}(1.6 \text{ m/s}^2) * t^2$$

$$(1.2 \text{ m}) * 2 = (1.6 \text{ m/s}^2) * t^2$$

$$(2.4 \text{ m}) = (1.6 \text{ m/s}^2) * t^2$$

$$\frac{2.4 \text{ m}}{(1.6 \text{ m/s}^2)} = t^2$$

$$1.5 \text{ s}^2 = t^2$$

$$1.2247 \text{ s} = t \rightarrow$$

$$t = 1.2 \times 10^0 \text{ s}$$

Prob. 2.1.3

Find the uniform acceleration that will cause an object's speed to change from 32. m/s to 96. m/s in an 8.0 s period.

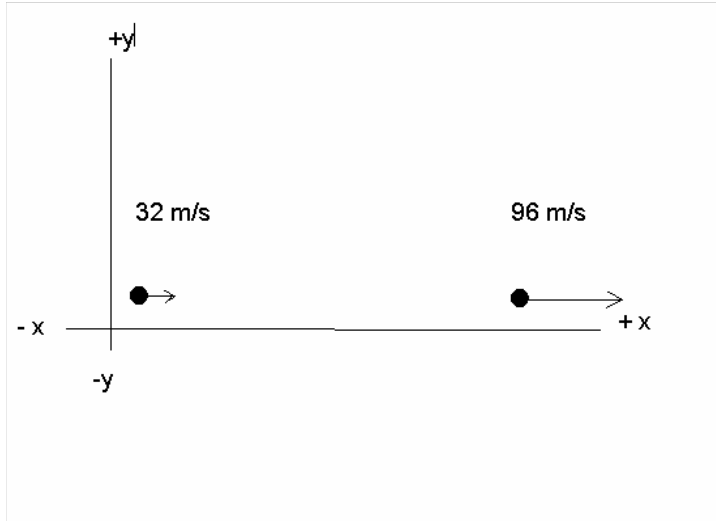
$$\mathbf{v_f = v_i + at}$$

$$v \text{ final} = 96 \text{ m/s}$$

$$v \text{ initial} = 32 \text{ m/s}$$

$$t = 8.0 \text{ s}$$

$$a = ?$$



$$96 \text{ m/s} = 32 \text{ m/s} + a(8.0 \text{ s})$$

$$96 \text{ m/s} - 32 \text{ m/s} = a(8.0 \text{ s})$$

$$64 \text{ m/s} = a(8.0 \text{ s})$$

$$\frac{64 \text{ m/s}}{8.0 \text{ s}} = a \rightarrow$$

$$\mathbf{a = 8.0 \times 10^0 \text{ m/s}^2}$$

Prob. 2.1.4

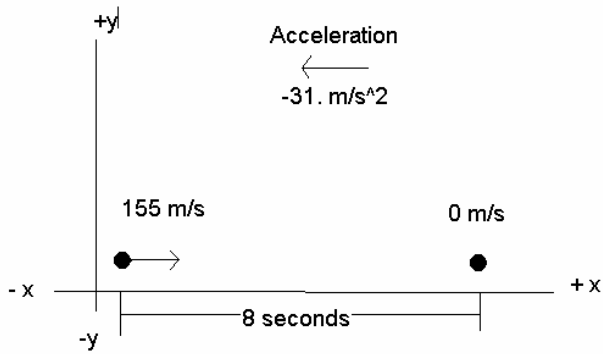
A rocket traveling at +155. m/s is decelerated at a rate of $-31. \text{ m/s}^2$. (a) How long will it take before the instantaneous speed is 0 m/s? (b) How far will it travel during this time? (c) What will be its velocity after 8.0 s?

$$\mathbf{a) \ v_f = v_i + at}$$

$$v \text{ initial} = 155 \text{ m/s}$$

$$v \text{ final} = 0 \text{ m/s}$$

$$a = -31 \text{ m/s}^2$$



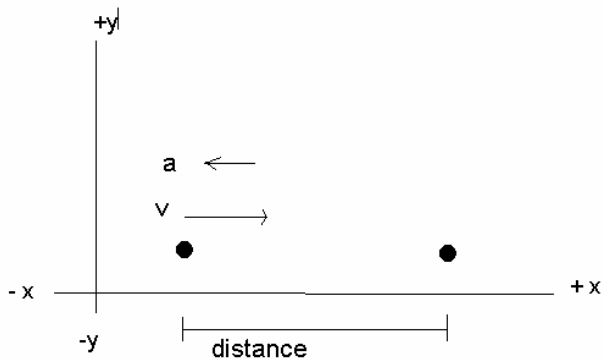
$$0 \text{ m/s} = 155 \text{ m/s} + (-31 \text{ m/s}^2) * t$$

$$-155 \text{ m/s} = (-31 \text{ m/s}^2) * t$$

$$\frac{155 \text{ m/s}}{(-31 \text{ m/s}^2)} = t$$

$$5 \text{ s} = t \rightarrow \boxed{t = 5.0 \times 10^1 \text{ s}}$$

$$\text{b) } d = \frac{v_i + v_f}{2} * t$$



$$v \text{ initial} = 55 \text{ m/s}$$

$$v \text{ final} = 0 \text{ m/s}$$

$$t = 5.0 \text{ s}$$

$$d = \frac{(155 \text{ m/s}) + (0 \text{ m/s})}{2} * 5.0 \text{ s}$$

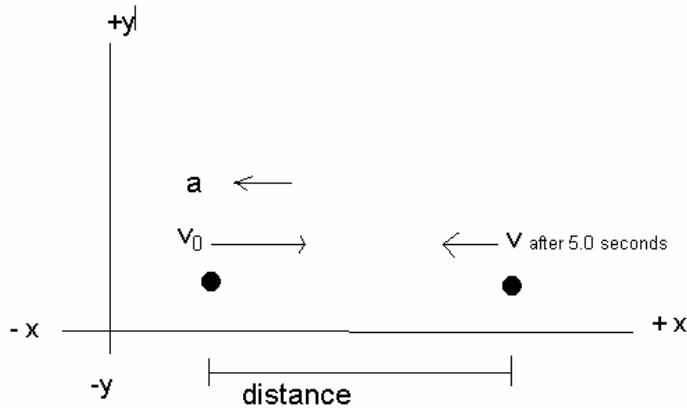
$$d = \frac{(155 \text{ m/s})}{2} * 5.0 \text{ s}$$

$$d = 77.5 \text{ m/s} * 5.0 \text{ s}$$

$$d = 387.5 \text{ m} \rightarrow$$

$$d = 3.9 \times 10^2 \text{ m}$$

c) $v_f = v_i + at$



$$v \text{ initial} = 155 \text{ m/s}$$

$$a = -31 \text{ m/s}^2$$

$$t = 8.0 \text{ s}$$

$$v \text{ final} = 155 \text{ m/s} + (-31 \text{ m/s}^2)(8.0 \text{ s})$$

$$v \text{ final} = 155 \text{ m/s} - 248 \text{ m/s}$$

$$v \text{ final} = -9.3 \times 10^1 \text{ m/s}$$

prob. 2.1.5

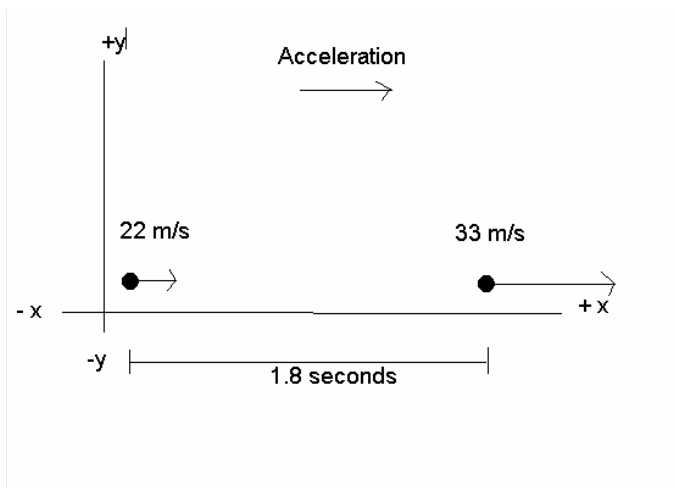
A car with a velocity of 22. m/s is accelerated uniformly at the rate of 1.6 m/s² for 6.8 s. What is its final velocity?

$$v_f = v_i + at$$

$$v \text{ initial} = 22 \text{ m/s}$$

$$a = 1.6 \text{ m/s}^2$$

$$t = 6.8 \text{ s}$$



$$v_{\text{final}} = 22 \text{ m/s} + (1.6 \text{ m/s}^2)(6.8 \text{ s})$$

$$v_{\text{final}} = 22 \text{ m/s} + 10.88 \text{ m/s}$$

$$v_{\text{final}} = 32.88 \text{ m/s} \rightarrow$$

$v_{\text{final}} = 3.3 \times 10^1 \text{ m/s}$
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Prob. 2.1.6

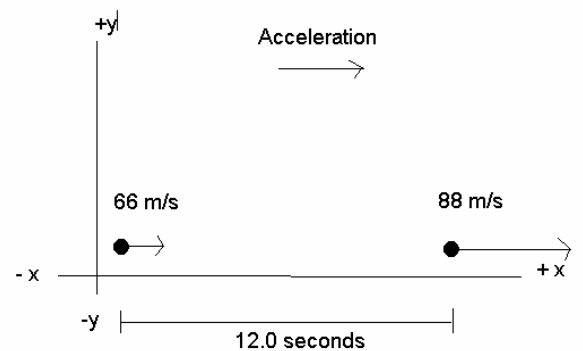
Determine the displacement of a plane that is uniformly accelerated from 66. m/s to 88. m/s in 12.0 s.

First solve for the acceleration with the formula $v_f = v_i + at$

$$v_{\text{final}} = 88. \text{ m/s}$$

$$v_{\text{initial}} = 66. \text{ m/s}$$

$$t = 12.0 \text{ s}$$



$$88 \text{ m/s} = 66 \text{ m/s} + a(12.0 \text{ s})$$

$$22 \text{ m/s} = a(12.0 \text{ s})$$

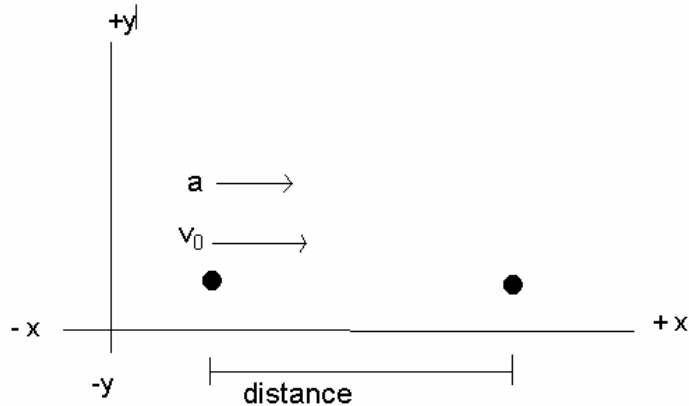
$$1.8 \text{ m/s}^2$$

Use the acceleration that was solved for in the previous section in the following formula: $d = v_i * t + 1/2 at^2$

$$v_{\text{initial}} = 66. \text{ m/s}$$

$$t = 12.0 \text{ s}$$

$$a = 1.8 \text{ m/s}^2$$



$$d = (66. \text{ m/s})(12.0 \text{ s}) + \frac{1}{2} (1.8 \text{ m/s}^2)(12.0 \text{ s})^2$$

$$d = 792 \text{ m} + \frac{1}{2}(1.8 \text{ m/s}^2)(144 \text{ s}^2)$$

$$d = 792 \text{ m} + 129.6 \text{ m}$$

$$d = 921.6 \text{ m} \rightarrow \boxed{d = 9.2 \times 10^2 \text{ m}}$$

Prob. 2.1.7

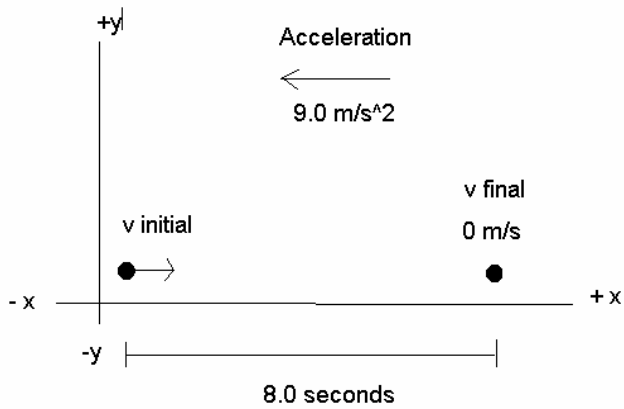
A car comes to rest after uniform deceleration at the rate of 9.0 m/s^2 for 8.0 s . What distance does it travel during this time?

In order to solve for distance, v_{initial} needs to be solved for first by using the formula: $v_f = v_i + at$

$$v_{\text{final}} = 0 \text{ m/s}$$

$$a = 9.0 \text{ m/s}^2$$

$$t = 8.0 \text{ s}$$

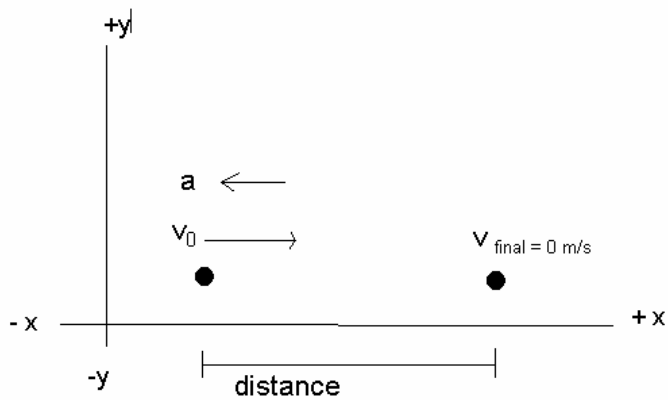


$$0 \text{ m/s} = v \text{ initial} + (-9.0 \text{ m/s}^2)(8.0 \text{ s})$$

$$v \text{ initial} = -(-9.0 \text{ m/s}^2)(8.0 \text{ s})$$

$$v \text{ initial} = 72 \text{ m/s}$$

**Now that I have $v \text{ initial}$; I will use it in the formula: $d = v_i * t + 1/2 at^2$
To solve for distance**



$$d = (72 \text{ m/s})(8.0 \text{ s}) + 1/2(-9.0 \text{ m/s}^2)(8.0 \text{ s})^2$$

$$d = 576 \text{ m} + (-4.5 \text{ m/s}^2)(64 \text{ s}^2)$$

$$d = 576 \text{ m} - 288 \text{ m}$$

$$d = 288 \text{ m} \rightarrow \boxed{d = 2.9 \times 10^2 \text{ m}}$$

Prob. 2.1.8

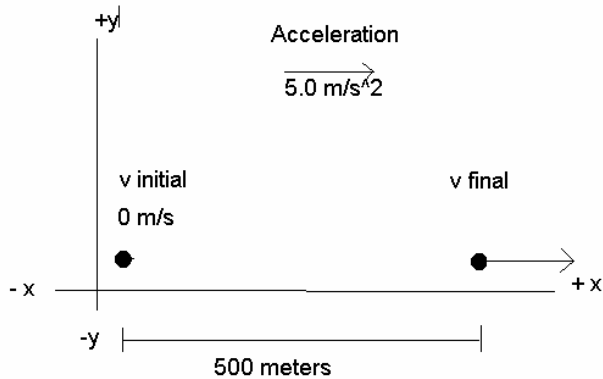
A plane travels a distance of 5.0×10^2 m while being accelerated uniformly from rest at the rate of $+5.0$ m/s². What final speed does it attain?

$$v_f^2 = v_i^2 + 2ad$$

$$v_{\text{initial}} = 0 \text{ m/s}$$

$$a = +5.0 \text{ m/s}^2$$

$$d = 5.0 \times 10^2 \text{ m}$$



$$v_f^2 = (0 \text{ m/s})^2 + 2(5.0 \text{ m/s}^2)(5.0 \times 10^2 \text{ m})$$

$$v_f^2 = (10.0 \text{ m/s}^2)(5.0 \times 10^2 \text{ m})$$

$$v_f^2 = 50.0 \times 10^2 \text{ m}^2/\text{s}^2$$

$$v_{\text{final}} = 70.7107 \text{ m/s} \rightarrow$$

$$\boxed{V_{\text{final}} = 7.1 \times 10^1 \text{ m/s}}$$

Prob. 2.1.9

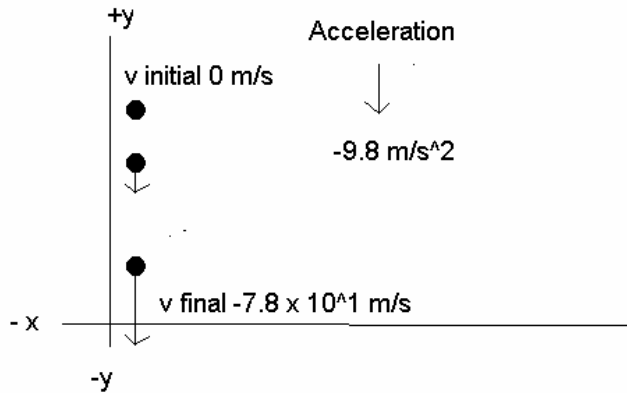
A stone falls freely from rest for 8.0 s. (a) Calculate its final velocity. (b) What distance does the stone fall during this time?

a) $v_f = v_i + at$

$$v_{\text{initial}} = 0 \text{ m/s}$$

$$a = 9.8 \text{ m/s}^2$$

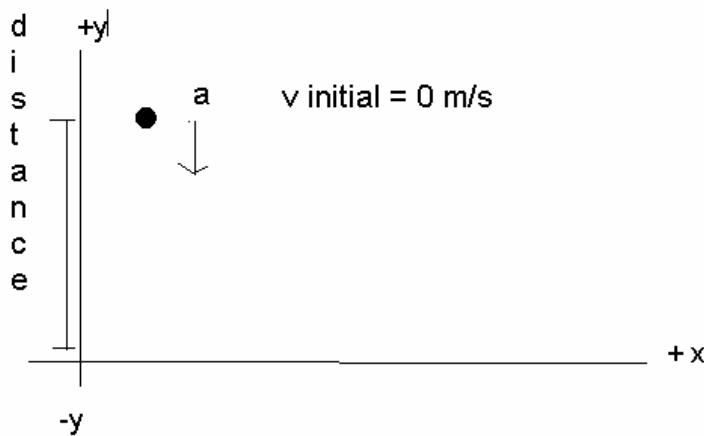
$$t = 8.0 \text{ s}$$



$$v_{\text{final}} = 0 \text{ m/s} + (-9.8 \text{ m/s}^2)(8.0 \text{ s})$$

$$v_{\text{final}} = -78.4 \text{ m/s} \rightarrow \boxed{V_{\text{final}} = -7.8 \times 10^1 \text{ m/s}}$$

b) distance $d = (v_{\text{final}} - v_{\text{initial}})/2 * \text{time}$



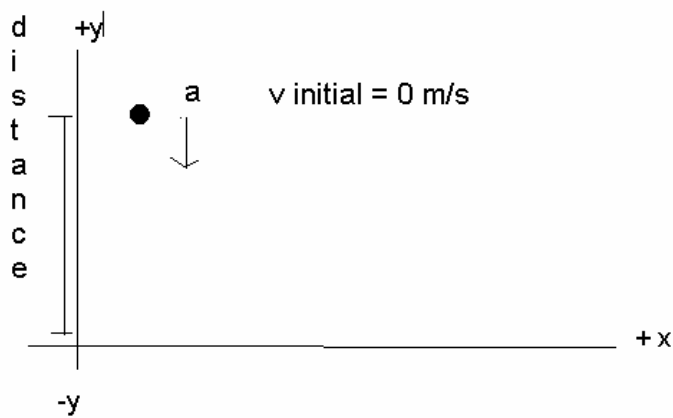
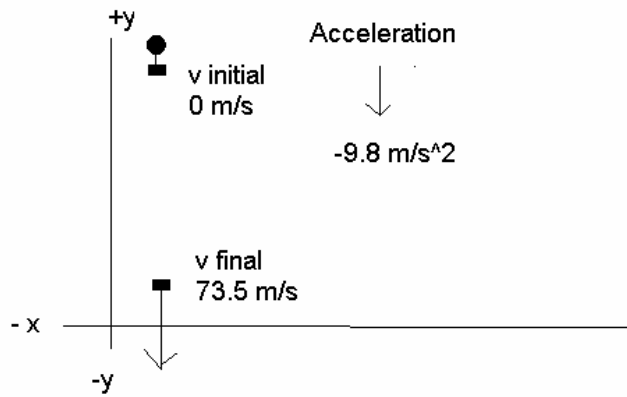
$$(78.0 \text{ m/s} - 0 \text{ m/s})/2 * 8.0 \text{ s} = 310 \text{ m.} \quad \boxed{\text{distance} = 3.1 \times 10^2 \text{ m}}$$

Prob. 2.1.10

A weather balloon is floating at a constant height above the earth when it releases a pack of instruments. (a) If the pack hits the ground with a speed of -73.5 m/s, how far does the pack fall? (b) How long does the pack fall?

a) $v_f^2 = v_i^2 + 2ad$

$v_{\text{initial}} = 0 \text{ m/s}$
 $v_{\text{final}} = 73.5 \text{ m/s}$
 $a = 9.8 \text{ m/s}^2$



$$(0 \text{ m/s})^2 = -(73.5 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)d$$

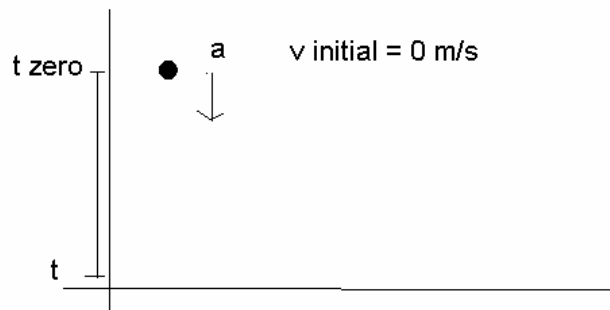
$$(0 \text{ m/s})^2 = -5402.25 \text{ m}^2/\text{s}^2 + (-19.6 \text{ m/s}^2)d$$

$$5402.25 \text{ m}^2/\text{s}^2 = (-19.6 \text{ m/s}^2)d$$

$$\frac{5402.25 \text{ m}^2/\text{s}^2}{(-19.6 \text{ m/s}^2)} = d$$

$$-275.625 \text{ m} = d \rightarrow \boxed{d = -2.76 \times 10^2 \text{ m}}$$

c) $v_f = v_i + at$



$$-73.5 \text{ m/s} = 0 \text{ m/s} + (-9.8 \text{ m/s}^2)t$$

$$-73.5 \text{ m/s} = (-9.8 \text{ m/s}^2)t$$

$$\frac{-73.5 \text{ m/s}}{-9.8 \text{ m/s}^2} = t$$

$$7.5 \text{ s} = t \rightarrow \boxed{t = 7.50 \times 10^0 \text{ s}}$$