

Course in Macro: Econ 8200

I: Reassessing the Role of Heterogeneity for Business Cycles

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 - Consumption
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 - Health and Longevity
- But as Macroeconomists, should we care?



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 - In Heterog Agents Ec changes in aggregates may happen and matter: Land Values.





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 - There is a lot of wealth that can be used efficiently to weather changes in available resources.
- The Great Recession has highlighted its shortcomings: How come we got such a large recession.





AIYAGARI-BEWLEY-HUGGETT-IMROHOROGLU MODELS WITH AGGREGATE SHOCKS

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- Why could they generate larger fluctuations?
 - First set of Empirical Reasons
 - 1. Recessions hit (lower earnings, more unemployment) more vulnerable (poor) households more.
 - Poor households have a higher Marginal Propensity to Consume out of income than rich households (Parker et al., 2013; Misra and Surico, 2014)





Heterogeneity (Inequality) in 2006: Marginal Distributions

	у	С	a	SCF 07 a
Mean (2006\$)	62,549	43,980	291,616	497,747





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Q4	22.8	22.4	13.0	11.9
Q5	47.5	45.6	82.7	82.5
90 – 95	10.8	10.3	13.7	11.1
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- a: Bottom 40% holds basically no wealth
- *y*, *c*: less concentrated



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Q1	8.6	11.3	92.2
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- 80% poorest acount for 63% of consumption



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NEOCIASSICAL HETEROGENEOUS AGENT & BUSINESS CYCLES



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- 3.1 Nonlinear decision rules (at least on the low levels of income and wealth)
- 3.2 A lot of agents in the states where their behavior is non linear (close to zero cash in hand).





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 - 2. Moreover, most agents are in the essentially linear part of the state space
- Heterogeneous agents models are like Rep Agent models for business cycle purposes.
 (Also confirmed in life-cycle models (Ríos-Rull, 1996)).

Why in those models Heterogeneity did not matter much?





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 - 2. Enough Low wealth people
 - 3. Large enough shocks





KRUEGER ET AL. (2016): MORE INEQUALITY, LARGER SHOCKS

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- Unemployment insurance system with size $\rho = 50\%$.

INEQUALITY IN THE BENCHMARK ECONOMY



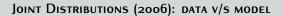
Net Worth	Da	ta	Model
% Share held by:	PSID, 06	SCF, 07	
Q1	-0.9	-0.2	0.3
Q2	0.8	1.2	1.2
Q3	4.4	4.6	4.7
Q4	13.0	11.9	16.0
Q5	82.7	82.5	77.8
90 – 95	13.7	11.1	17.9
95 - 99	22.8	25.3	26.0
Top 1%	30.9	33.5	14.2
Gini	0.77	0.78	0.77

• Get's inquality almost right at the very bottom

JOINT DISTRIBUTIONS (2006): DATA V/S MODEL



% Share of:						
	у с		у с		%	c/y
a Quintile	Data	Model	Data	Model	Data	Model
Q1	8.6	6.0	11.3	6.6	92.2	90.4
Q2	10.7	10.5	12.4	11.3	81.3	86.9
Q3	16.6	16.6	16.8	16.6	70.9	81.1
Q4	22.6	24.6	22.4	23.6	69.6	78.5
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Rudimentary life cycle is crucial for level of consumption rates and their decline with wealth.



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% Share:	KS	no UI	+UI	
ΔC	-1.9%			



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• If we were to think of Endogenous Labor, it would be Worse (Guerrieri and Lorenzoni (2017))





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A PARALLEL STORY WITH NEW KENESIAN MODELS



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 alternative (Carroll (1997), Auclert et al. (2020), Alves, Bustamante, Guo, Kartashova, Lee, Pugh, See,
 Terajima, and Ueberfeldt (2022)) because they have poor people that respond to transitory
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- Heterogeneity is not enough by itself since there is a lot of wealth in the economy (about 4 times GDP) SO



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A PARALLEL STORY WITH NEW KENESIAN MODELS



- Interest Rate Movements as Analyzed by Central Banks Operate through Intertemporal Substitution.
 - They are typically studied with Representative Agent Models.
 - Any effect of wealth or income changes has a small consumption increase: There is a
 lot of wealth (25 times quarterly consumption implying at best a Low Marginal Propensities to
 Consume < 3%)
 - Consumption response is then humped via habits.
- Yet Evidence (Fagereng et al. (2021), Crawley and Kuchler (2021)) points to much larger Marginal Propensities to Consume.
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- Heterogeneity is not enough by itself since there is a lot of wealth in the economy (about 4 times GDP) SO
 - Models difficult access to wealth by imposing large transaction costs in two asset models (Kaplan et al. (2018))
 - Habits or sticky expectations to delay a bit the response (Auclert et al. (2020)) rather than the more grounded rational inattention (Sims (2003), Mackowiak and Wiederholt (2009)).



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 - Much larger response to changes in interest rates.
- Overall, indirect effects of an unexpected changes in interest rates, operating through a general equilibrium increase in labor demand (Kaplan et al. (2018)) outweigh intertemporal substitution mechanisms.



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- Can be easily implemented via an expenditure externality (Krueger, Mitman, and Perri (2016))





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- These margins open the door to other type of shocks (financial shocks, government policy shocks, international shocks).





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- Expenditures play a role and adjustment is costly.
 - These are mechanisms that transform a drop in consumption into drops in TFP without reallocation of output to investment. Triggered by drops in Consumption.

PURPOSE TODAY: LAY OUT A MODEL SUITABLE TO STUDY BUSINESS CYCLES



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 - The economy is too rigid to turn negative wealth effect into an expansion via harder working



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- More financial stability than standard new-Keynesian inflation-output tradeoffs.



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- We also explore slow adjustment of nontradable prices (insufficient devaluation)



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 - Incomplete adjustment on the relative price of inputs (insufficient devaluation) after the rate hike

THE ENVIRONMENT: FIRST THE STEADY STATE:



Three types of Agents

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- Housing H, a combo of structures S & land L in fixed supply.





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Household Problem: State is $\{\eta,\epsilon,\theta^{\rm e},\theta^{\rm x},a\}=\{z,a\}$



$$V(z,a) = \max_{b,h,c} \ u\left[\Psi^{c}(e,m),h\right] + \beta \ \mathbb{E}\left\{V(z',a')\right\}$$

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$$a' = \underbrace{p^{s'}(1 - \delta_h) \ s(h, H)}_{ ext{value of undeprec Struc}} + \underbrace{p^{\ell'} \frac{h}{H}}_{ ext{value of land}} + (1 + r') \ b$$
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$$\Omega^{e}(k, \{n^{e}\}) = \max_{v, k', m, e} \left\{ p^{e} F^{e}(k, n) - m - p^{e}e - \kappa v - \phi^{n}(n', n) - w n + \frac{\Omega^{e}(k', \{n^{e'}\})}{1 + r'} \right\}$$



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$$n^{\epsilon\prime} = \underbrace{\sum_{\tilde{\epsilon}} (1 - \delta_{\tilde{\epsilon}}) n_{\tilde{\epsilon}} \Gamma_{\tilde{\epsilon}\epsilon}}_{\text{unseparated worker}} + \underbrace{\sum_{\tilde{\epsilon}} \Gamma_{\tilde{\epsilon}\epsilon} \frac{u_{\tilde{\epsilon}}}{u} v}_{\text{measure of hiring ϵ next period}}$$



AND SKILL SPECIFIC SEPARATION RATES

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• Dividends $\pi^e = p^e F^e(k, l) - m - p^e e - \kappa v - \phi^n(n, n) - w \sum_{\epsilon} n^{\epsilon} \epsilon$



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Financial constraints limit and change the value of land.

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1 Steady State



• Model period is a quarter

SOME ADDITIONAL ASSUMPTIONS



- Model period is a quarter
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- Non homotetic Utility to prevent housing purchases by the rich

Parameterization for St St			
Risk aversion for consumption	2.0		
Satiation level for housing	4.5		
Loan to value ratio	0.8		
Annual world interest rate	4.0%		
Relevant Out of St St Elasticities			
Wage elasticity	0.5		
TFP elasticity (with externality) (small)	0.3		
Elasticity of Substitution bw nontradable and import	0.8		
Adjustment cost coefficient (to be fine tuned)	1.57		



	Target	Model	
Output	1.00	1.00	



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Frac. of H held by bottom 90%	0.58	0.64	



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Share of Export	0.30	0.30	
	1		



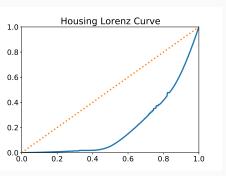
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Relative Price of Nontradable	1.00	1.00	
Share of Export	0.30	0.30	
Employment Rate	0.92	0.92	

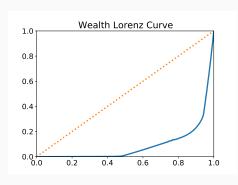


	Target	Model	Tool	Value
Output	1.00	1.00	TFP in Export	0.73
Capital-to-Output	2.00	2.00	Capital dep. rate	0.025
Housing-Value-to-Output	1.80	1.76	Util shifter in housing	0.50
Debt-to-GDP	0.00	0.02	Discount rate	0.92
Wealth-to-Output	4.50	4.57	Dep. rate in housing	0.008
Wealth Gini	0.82	0.82	Top Share holdings	13.20
Frac. of H held by bottom 70%	0.25	0.27	\widehat{h}_{1}	0.98
Frac. of H held by bottom 80%	0.39	0.41	\widehat{h}_{2}	1.80
Frac. of H held by bottom 90%	0.58	0.64	σ_h	2.98
Relative Price of Nontradable	1.00	1.00	TFP in e	0.73
Share of Export	0.30	0.30	CES weight on e	0.75
Employment Rate	0.92	0.92	wage	0.96

STEADY STATE







• Gini coeff: housing 0.63, Wealth 0.82 (data 0.82 in 2007 SFC)

2 Putting the Model to Use: Experiments





• We can estimate the extent of frictions to generate the Recession.



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AN (MIT) FINANCIAL SHOCK HITS



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 - 2. Size of Frictions in goods markets: To match productivity changes.
 - 3. Wage rigidity: Directly from Wage dynamics:
- We look at the transition. It involves solving for the steady state and then iterating backwards (with the additional problem of solving for equilibrium prices. Hard, but not too hard. Dynare can do it.)





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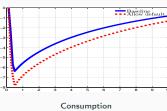


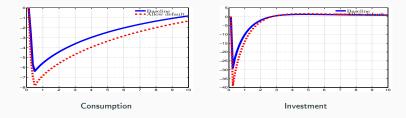
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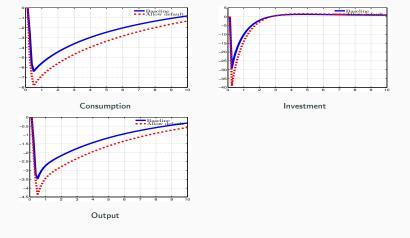
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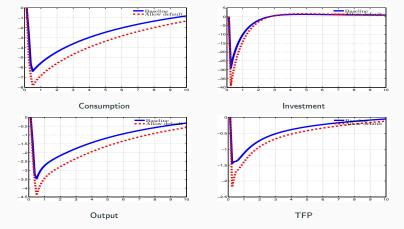
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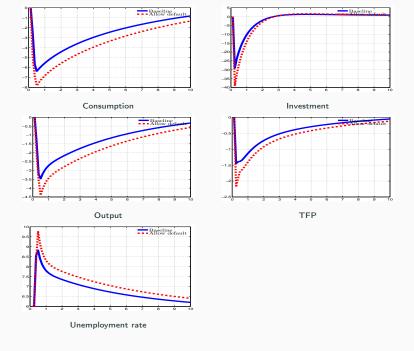
- Like in all heterogeneous agents models, more frictions imply that in the long run output and wealth end up being higher.
- But in our economies the transition is associated to a recession.

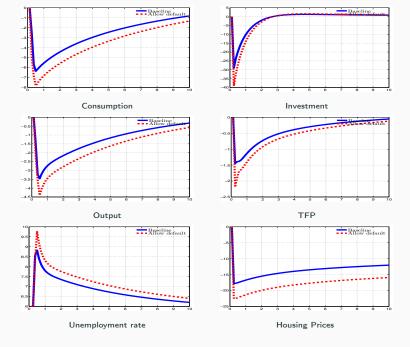






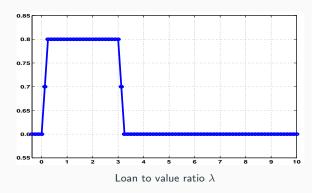






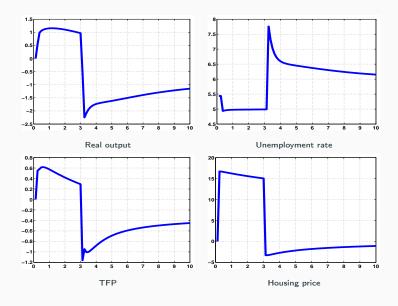
WHAT ABOUT EXPANSIONS?: A CREDIT CYCLE





Another Experiment A Credit Cycle





WHAT ABOUT STANDARD ANALYSIS OF FLUCTUATIONS?



MIT shocks are NOT the way to study fluctuations.

Traditionally very complicated methods have been proposed. Some of them based on
quasilinearity or aggregate capital is the only thing that matters (Krusell and Smith Jr. (1997,?)) interesting
really happens. There are modern linearization versions based on Reiter (SeHyoun Ahn and Wolf (2017) and
Childers (2016)).

 They approximate somehow the distribution of agents and look for its equilibrium law of motion.





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 - Let x_t denote the response of statistic x in period t to an innovation of size one in period zero of say TFP.
 - Consider now a sequence of innovations labeled $\{\epsilon_t\}_{t=0}^T$. Then a linear approximation to x in period t, labeled \hat{x}_t is

$$\widehat{x}_t = x_0 \epsilon_t + x_1 \epsilon_{t-1} + x_2 \epsilon_{t-2} + \dots$$



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 - Consider now a sequence of innovations labeled $\{\epsilon_t\}_{t=0}^T$. Then a linear approximation to x in period t, labeled \hat{x}_t is

$$\widehat{x}_t = x_0 \epsilon_t + x_1 \epsilon_{t-1} + x_2 \epsilon_{t-2} + \dots$$

And we are done!!!!



- There is a wonderful recent innovation Boppart et al. (2018) that uses the Impulse Response from an MIT Shock as a Numerical Derivative to evaluate linear approximations.
 - Only the transition to one (or more) MIT shock needs to be computed.
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- And we are done!!!!
- Adding more shocks is linearly more costly



Assess Equilibrium Implications

1 Increase in Interest Rate (world event or Policy) 1% (Baseline)



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2 Perfect Storm: Base + Financial Constraint: Max LTV 80% \rightarrow 60% + (p^x – 3%)



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3 Base without any negative effect on TFP

4 Base with price stickiness (insufficient devaluation)



 $\bullet\,$ A Temporary but persistent increase in the (World) Interest Rate



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- \bullet With TFP Externality only on Nontradables



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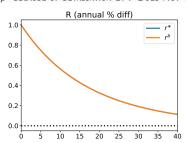
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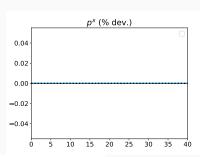
• Import Elasticty .8

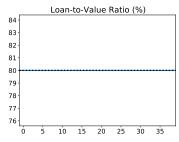
1- Exogenous Shifter: (Only r moves)



 p^{x} because of devaluation LTV Does Not







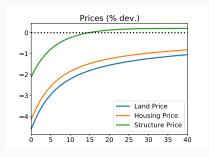
1- Asset Prices & Quantities (Financial and Total Wealth)

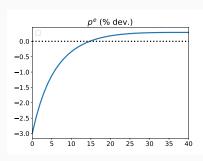




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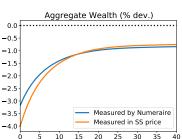


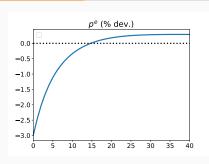


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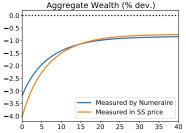


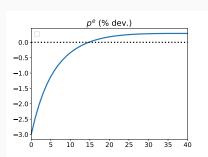


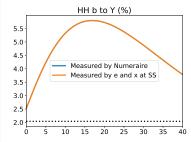
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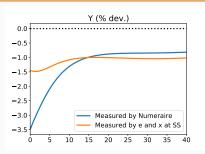




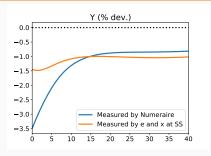


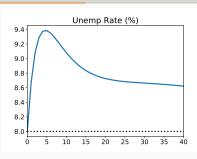




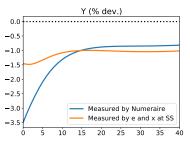


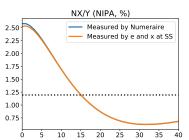


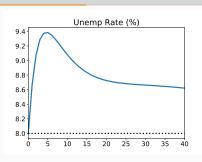




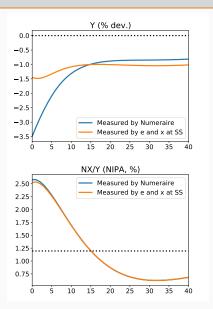


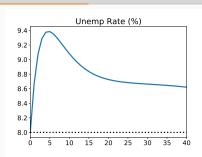


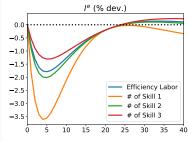




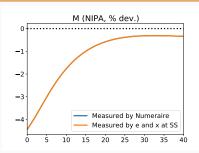




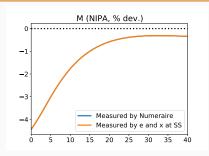


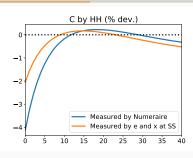




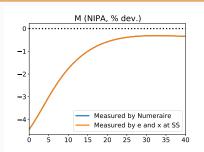


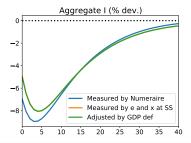


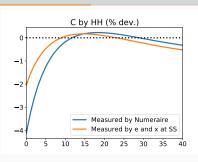




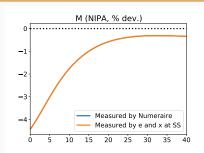


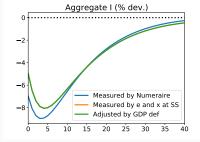


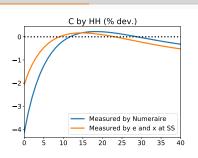


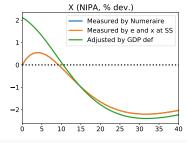




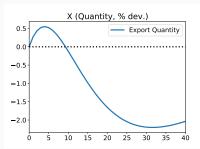




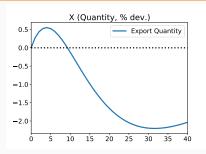


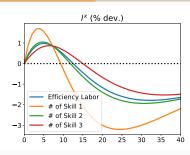




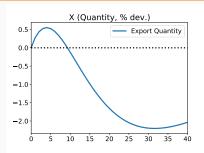


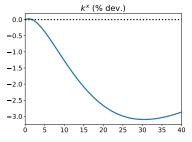


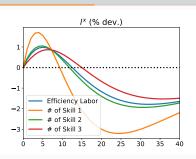




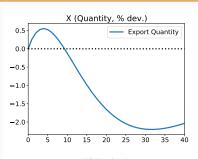


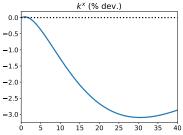


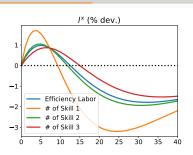


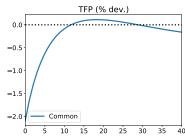




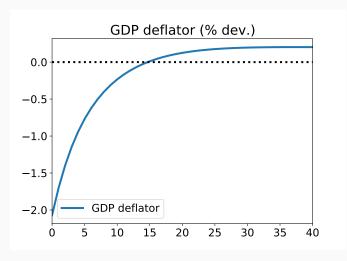




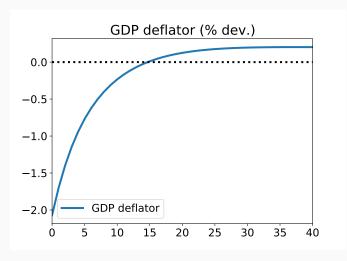




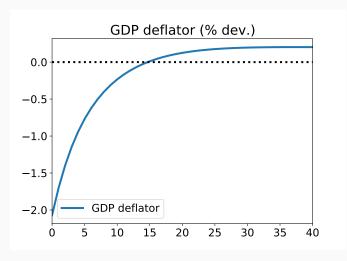




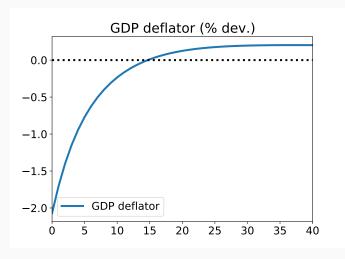




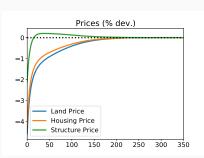




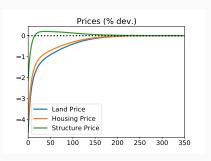


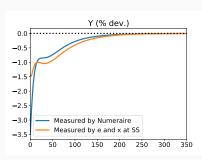




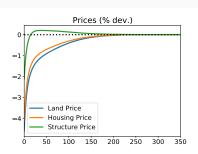


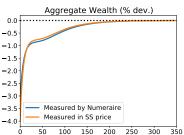


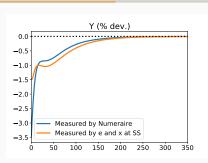




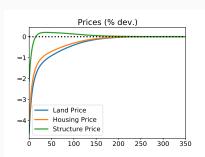


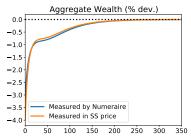


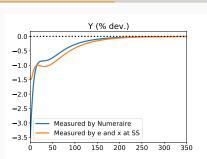


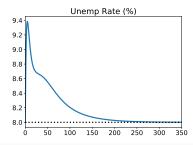












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- Recessions are Long (Aguiar and Gopinath (2007))



• A Temporary but persistent Increase in Interest Rates



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2TH EXPERIMENT: PERFECT STORM: THE GREAT RECESSION?



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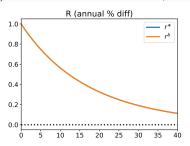
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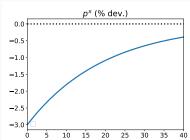
Import Elasticty .8

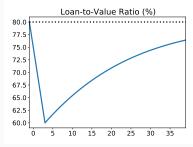
2. Exogenous Shifters: r moves 1% and p^{x} 5%



 p^{\times} Much more because of devaluation; LTV Does Not



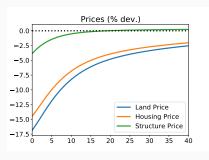


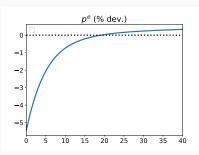




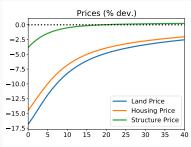


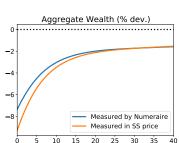


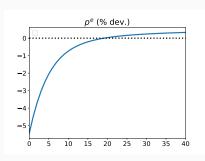




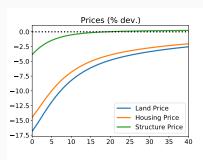


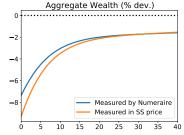


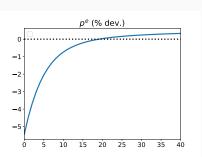


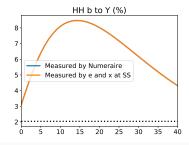




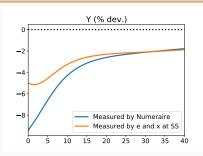




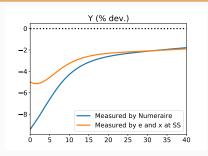


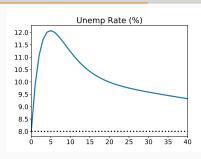




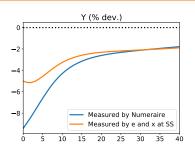


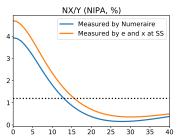


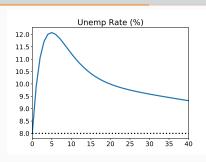




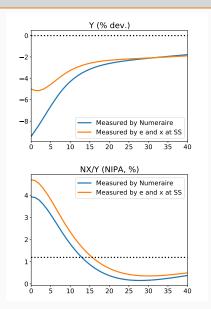


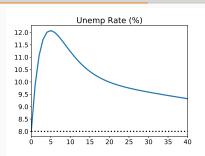


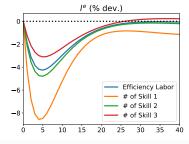




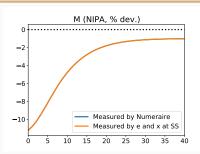




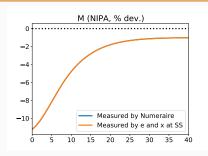


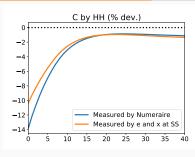




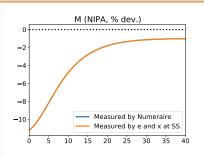


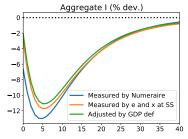


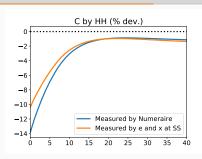




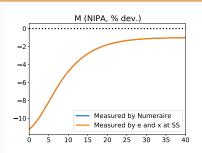


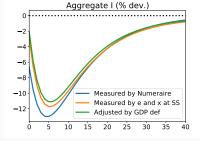


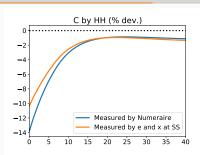


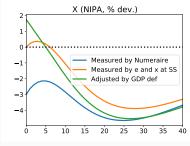














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- Very Large Devaluation relative to price decrease



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- $\bullet\,$ Huge Drop of Consumption, Investment and Exports



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- Huge Drop of Consumption, Investment and Exports
- Huge Reduction in Employment

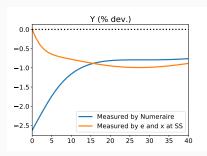


- Everything Larger
- Very Large Devaluation relative to price decrease
- Huge Drop of Consumption, Investment and Exports
- Huge Reduction in Employment
- Humongous reduction of imports: Sizeable Improvement in Balance of Payments.

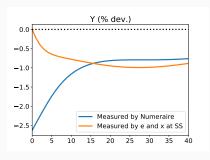


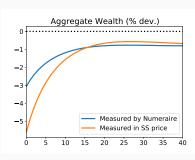
- Everything Larger
- Very Large Devaluation relative to price decrease
- Huge Drop of Consumption, Investment and Exports
- Huge Reduction in Employment
- Humongous reduction of imports: Sizeable Improvement in Balance of Payments.
- Not consistent world wide. Need much larger drop in foreign demand.



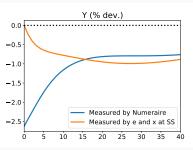


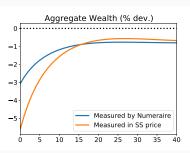




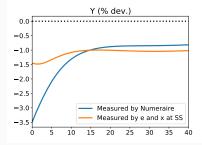




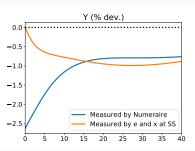


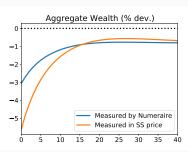


Comparing with Baseline

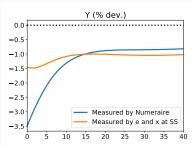


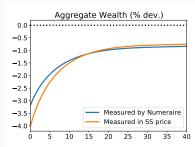






Comparing with Baseline





4TH: INSUFFICIENT DEVALUATION



• Elastic Non-tradable price no market clearing on non-tradables, demand determined quantities

4TH: Insufficient Devaluation



- A Temporary but persistent Increase in Interest Rates
- Elastic Non-tradable price no market clearing on non-tradables, demand determined quantities
- Reduction in Max LTV from 80% to 60%
- With TFP Externality
 - TFP Elasticity wrt expenditures .5
 - Wage Adjustments ($\psi^w = .5$)

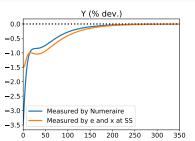
$$\log w_t - \log w^{ss} = \psi^w \left(\log Y_t - \log Y^{ss} \right)$$

• Import Elasticty .8



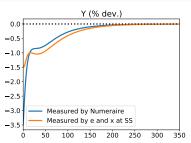


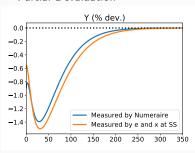
TION





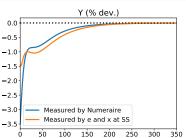


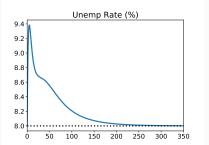


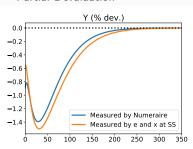








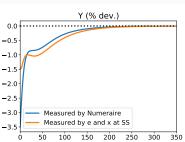


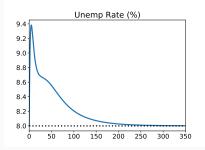


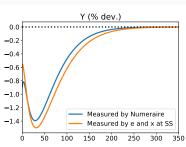


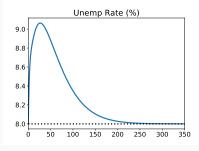


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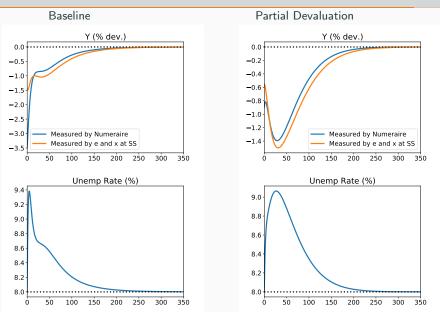






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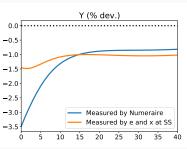


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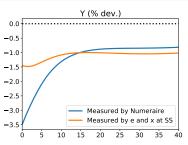


Perfect Storm

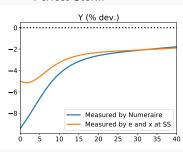






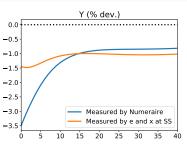


Perfect Storm

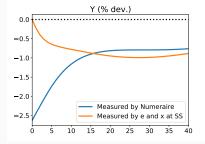




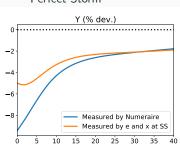




No TFP Externality



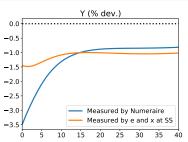
Perfect Storm



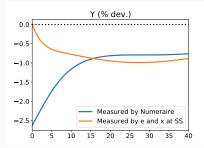
Insufficient Devaluation



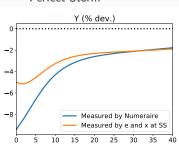




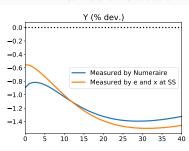
No TFP Externality



Perfect Storm



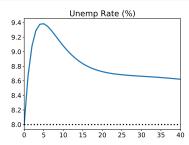
Insufficient Devaluation



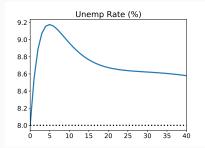
COMPARISON BETWEEN ALL ECONOMIES: UNEMPLOYMENT



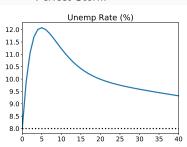




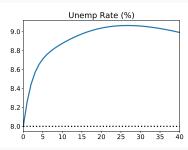
No TFP Externality



Perfect Storm



Insufficient Devaluation





• Some Technical Things



- Some Technical Things
 - Incorporate Financial Restrictions ONLY on newly born

WHAT WE WANT TO HAVE BUT DO NOT HAVE YET



- Some Technical Things
 - Incorporate Financial Restrictions ONLY on newly born
 - Loan to Value Restrictions ONLY to New Loans

WHAT WE WANT TO HAVE BUT DO NOT HAVE YET



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 - So Interest Rates are Endogenous

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 - Incorporate Financial Restrictions ONLY on newly born
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- Build this into a World Economy
 - So Interest Rates are Endogenous
 - $\bullet\,$ So Crisis are Simultaneous and Devaluations are Not Helpful



- Some Technical Things
 - Incorporate Financial Restrictions ONLY on newly born
 - Loan to Value Restrictions ONLY to New Loans
- Build this into a World Economy
 - So Interest Rates are Endogenous
 - So Crisis are Simultaneous and Devaluations are Not Helpful
- Have a modern New Keynesian structure to model the link between nominal and real interest rates

SUMMARY



 Heterogeneous Agent Models have come a long way (empirically, computationally, theroretically) to become useful tools to understand aggregate economies and to evaluate policy.



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 Wider mechanisms than just through intertemporal substitution as in Rep Agent models.

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Build more Asset prices and productivity propagation into those models.



 We need to develop models of Monetary policy that are beyond those in New Keynesian Models.



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- Financial Stability is a Concern
- Not only because financial firms are affected
- But also because Households are affected, especially in Europe where mortgages are NOT indexed.
- In other work we show how expansionary policy (with house price increases) put households more at risk for later interest rate hikes.

Thank you very much

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