

# Banking Dynamics and Capital Regulation

---

José-Víctor Ríos-Rull

*Penn, CAERP, UCL*

Tamon Takamura

*Bank of Canada*

Yaz Terajima

*Bank of Canada*

University of Minnesota,  
October 19, 2017

WORK IN PROGRESS

- A threshold of a ratio between own capital and risk weighted assets.

## CAPITAL BUFFERS AS A FORM OF REGULATION

---

- A threshold of a ratio between own capital and risk weighted assets.
- Below this threshold, bank activities are limited to not issue dividends, nor to make new loans, while the capital recovers.

## CAPITAL BUFFERS AS A FORM OF REGULATION

- A threshold of a ratio between own capital and risk weighted assets.
- Below this threshold, bank activities are limited to not issue dividends, nor to make new loans, while the capital recovers.
- If own capital gets very low (another threshold, say 2%) banks may get intervened or liquidated.

## CAPITAL BUFFERS AS A FORM OF REGULATION

- A threshold of a ratio between own capital and risk weighted assets.
- Below this threshold, bank activities are limited to not issue dividends, nor to make new loans, while the capital recovers.
- If own capital gets very low (another threshold, say 2%) banks may get intervened or liquidated.
- Rationale is to Protect the Public Purse safe when there is Deposit Insurance in the presence of moral hazard on the part of the bank.

## NEW REGULATIONS, BASEL III: COUNTER-CYCLICAL CAPITAL BUFFER

---

- To ease the regulation in recessions.

## NEW REGULATIONS, BASEL III: COUNTER-CYCLICAL CAPITAL BUFFER

- To ease the regulation in recessions.
- Why?

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.
  2. Banking Activity (lending) is more socially valuable.

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.
  2. Banking Activity (lending) is more socially valuable.
- A tight requirement would induce some banks to reduce drastically their lending to comply if adversely affected.

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.
  2. Banking Activity (lending) is more socially valuable.
- A tight requirement would induce some banks to reduce drastically their lending to comply if adversely affected.
- We want to **Measure** the trade-offs involved when taking into account many (quantitatively) relevant features.

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.
  2. Banking Activity (lending) is more socially valuable.
- A tight requirement would induce some banks to reduce drastically their lending to comply if adversely affected.
- We want to **Measure** the trade-offs involved when taking into account many (quantitatively) relevant features.
- Analyze a change in capital requirements on the onset of a recession

## NEW REGULATIONS, BASEL III: COUNTER-CYCLICAL CAPITAL BUFFER

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.
  2. Banking Activity (lending) is more socially valuable.
- A tight requirement would induce some banks to reduce drastically their lending to comply if adversely affected.
- We want to **Measure** the trade-offs involved when taking into account many (quantitatively) relevant features.
- Analyze a change in capital requirements on the onset of a recession
  - How much extra credit?

## NEW REGULATIONS, BASEL III: COUNTER-CYCLICAL CAPITAL BUFFER

- To ease the regulation in recessions.
- Why?
  1. Automatically the Recession makes the capital requirement tighter by reducing the value of assets (and hence of capital), and/or by relabeling those assets as riskier.
  2. Banking Activity (lending) is more socially valuable.
- A tight requirement would induce some banks to reduce drastically their lending to comply if adversely affected.
- We want to **Measure** the trade-offs involved when taking into account many (quantitatively) relevant features.
- Analyze a change in capital requirements on the onset of a recession
  - How much extra credit?
  - How much extra banking loses?

- Davydiuk (2017).

- Davydiuk (2017).
  - There is overinvestment due the moral hazard of investors (banks) that do not pay depositors

- Davydiuk (2017).
  - There is overinvestment due the moral hazard of investors (banks) that do not pay depositors
  - The overinvestment is larger in expansions because of decreasing returns and bailout wedge increasing in lending.

- Davydiuk (2017).
  - There is overinvestment due the moral hazard of investors (banks) that do not pay depositors
  - The overinvestment is larger in expansions because of decreasing returns and bailout wedge increasing in lending.
  - Nicely built on top of an infinitely lived RA business cycle model.

- Davydiuk (2017).
  - There is overinvestment due the moral hazard of investors (banks) that do not pay depositors
  - The overinvestment is larger in expansions because of decreasing returns and bailout wedge increasing in lending.
  - Nicely built on top of an infinitely lived RA business cycle model.
- Corbae et al. (2016) is quite similar except, single bank problem with market power, and constant interest borrowing and lending. Done to have structural models of stress testing.

## WHAT IS A BANK?

---

- A costly to start technology that has an advantage at

## WHAT IS A BANK?

---

- A costly to start technology that has an advantage at
  1. Attracting deposits at zero interest rates (provides services)

# WHAT IS A BANK?

- A costly to start technology that has an advantage at
  1. Attracting deposits at zero interest rates (provides services)
  2. Matching with borrowers and can grant long term “risky loans” at interest rate  $r$  with low, but increasing, emission costs.

# WHAT IS A BANK?

- A costly to start technology that has an advantage at
  1. Attracting deposits at zero interest rates (provides services)
  2. Matching with borrowers and can grant long term “risky loans” at interest rate  $r$  with low, but increasing, emission costs.
  3. It can borrow (issue bonds) in addition to deposits and default.

# WHAT IS A BANK?

- A costly to start technology that has an advantage at
  1. Attracting deposits at zero interest rates (provides services)
  2. Matching with borrowers and can grant long term “risky loans” at interest rate  $r$  with low, but increasing, emission costs.
  3. It can borrow (issue bonds) in addition to deposits and default.
- Its deposits are insured but its loans and its borrowing are not:  
There is a moral hazard problem.

# WHAT IS A BANK?

- A costly to start technology that has an advantage at
  1. Attracting deposits at zero interest rates (provides services)
  2. Matching with borrowers and can grant long term “risky loans” at interest rate  $r$  with low, but increasing, emission costs.
  3. It can borrow (issue bonds) in addition to deposits and default.
- Its deposits are insured but its loans and its borrowing are not:  
There is a moral hazard problem.
- Assets are long term, liabilities are short term

# WHAT IS A BANK?

- A costly to start technology that has an advantage at
  1. Attracting deposits at zero interest rates (provides services)
  2. Matching with borrowers and can grant long term “risky loans” at interest rate  $r$  with low, but increasing, emission costs.
  3. It can borrow (issue bonds) in addition to deposits and default.
- Its deposits are insured but its loans and its borrowing are not:  
There is a moral hazard problem.
- Assets are long term, liabilities are short term
- Banks cannot issue new equity or sell assets (today).

## FEATURES TO INCLUDE

---

- Banks may be worth saving even if bankrupt:

## FEATURES TO INCLUDE

---

- Banks may be worth saving even if bankrupt:
  1. New loans are partially independent of old loans.

## FEATURES TO INCLUDE

---

- Banks may be worth saving even if bankrupt:
  1. New loans are partially independent of old loans.
  2. Capacity to attract deposits is valuable.

## FEATURES TO INCLUDE

---

- Banks may be worth saving even if bankrupt:
  1. New loans are partially independent of old loans.
  2. Capacity to attract deposits is valuable.
  3. May get better over time on average.

## FEATURES TO INCLUDE

---

- Banks may be worth saving even if bankrupt:
  1. New loans are partially independent of old loans.
  2. Capacity to attract deposits is valuable.
  3. May get better over time on average.
  4. Large bankruptcy costs.

## FEATURES TO INCLUDE

---

- Banks may be worth saving even if bankrupt:
  1. New loans are partially independent of old loans.
  2. Capacity to attract deposits is valuable.
  3. May get better over time on average.
  4. Large bankruptcy costs.
- Banks may take time to develop. They grow slowly in size due to exogenous loan productivity process and need for internal accumulation of funds.

## FEATURES TO INCLUDE

- Banks may be worth saving even if bankrupt:
  1. New loans are partially independent of old loans.
  2. Capacity to attract deposits is valuable.
  3. May get better over time on average.
  4. Large bankruptcy costs.
- Banks may take time to develop. They grow slowly in size due to exogenous loan productivity process and need for internal accumulation of funds.
- Useful also for Shadow Banking

- A bank is  $\xi = [\xi_d, \xi_l]$ , exogenous, idiosyncratic, Markovian with transition  $\Gamma^{z, \xi}$ . Its access to deposits; its costs of making new loans.  $z$  is aggregate and shapes the transition of  $\xi$ .

- A bank is  $\xi = [\xi_d, \xi_\ell]$ , exogenous, idiosyncratic, Markovian with transition  $\Gamma^{z, \xi}$ . Its access to deposits; its costs of making new loans.  $z$  is aggregate and shapes the transition of  $\xi$ .
- A bank has liquid assets  $a$  that can (and are likely to) be negative and long term loans  $\ell$  (decay at rate  $\lambda$ ).

- A bank is  $\xi = [\xi_d, \xi_\ell]$ , exogenous, idiosyncratic, Markovian with transition  $\Gamma^{z, \xi}$ . Its access to deposits; its costs of making new loans.  $z$  is aggregate and shapes the transition of  $\xi$ .
- A bank has liquid assets  $a$  that can (and are likely to) be negative and long term loans  $\ell$  (decay at rate  $\lambda$ ).
- Banks make new loans  $n$ , distribute dividends  $c$  and issue risky bonds  $b'$  at price  $q(z, \xi, \ell, n, b')$ .

- A bank is  $\xi = [\xi_d, \xi_\ell]$ , exogenous, idiosyncratic, Markovian with transition  $\Gamma^{z, \xi}$ . Its access to deposits; its costs of making new loans.  $z$  is aggregate and shapes the transition of  $\xi$ .
- A bank has liquid assets  $a$  that can (and are likely to) be negative and long term loans  $\ell$  (decay at rate  $\lambda$ ).
- Banks make new loans  $n$ , distribute dividends  $c$  and issue risky bonds  $b'$  at price  $q(z, \xi, \ell, n, b')$ .
- The bank is subject to shrinkage shocks to its portfolio of loans  $\delta$ ,  $\pi_{\delta/z}$ , that may bankrupt it. Costly liquidation ensues.

## MODEL

- A bank is  $\xi = [\xi_d, \xi_\ell]$ , exogenous, idiosyncratic, Markovian with transition  $\Gamma^{z, \xi}$ . Its access to deposits; its costs of making new loans.  $z$  is aggregate and shapes the transition of  $\xi$ .
- A bank has liquid assets  $a$  that can (and are likely to) be negative and long term loans  $\ell$  (decay at rate  $\lambda$ ).
- Banks make new loans  $n$ , distribute dividends  $c$  and issue risky bonds  $b'$  at price  $q(z, \xi, \ell, n, b')$ .
- The bank is subject to shrinkage shocks to its portfolio of loans  $\delta$ ,  $\pi_{\delta/z}$ , that may bankrupt it. Costly liquidation ensues.
- New banks enter small  $\xi$  at cost  $\bar{c}^e$

## MODEL: WHAT ARE AGGREGATE SHOCKS

- Determines the distribution of  $\delta$  and may determine the transition of  $\xi$ .

## MODEL: WHAT ARE AGGREGATE SHOCKS

- Determines the distribution of  $\delta$  and may determine the transition of  $\xi$ .
- Determines the countercyclical capital requirement  $\theta(z)$ .

## MODEL: WHAT ARE AGGREGATE SHOCKS

- Determines the distribution of  $\delta$  and may determine the transition of  $\xi$ .
- Determines the countercyclical capital requirement  $\theta(z)$ .
- Note that in this version there is no interaction between banks. The distribution is not a state variable of the banks' problem.

## MODEL: WHAT ARE AGGREGATE SHOCKS

- Determines the distribution of  $\delta$  and may determine the transition of  $\xi$ .
- Determines the countercyclical capital requirement  $\theta(z)$ .
- Note that in this version there is no interaction between banks. The distribution is not a state variable of the banks' problem.
- The state of the economy is a measure  $x$  of banks that evolves over time itself via banks decisions and shocks (an extension of Hopenhayn's classic)

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$
$$W(z, \xi, a, \ell) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), \ell'(\delta')] \right\} \text{ s.t.}$$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$
$$W(z, \xi, a, \ell) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), \ell'(\delta')] \right\} \text{ s.t.}$$
$$(TL) \quad \ell' = (1 - \lambda) (1 - \delta') \ell + n$$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$
$$W(z, \xi, a, \ell) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), \ell'(\delta')] \right\} \text{ s.t.}$$

$$(TA) \quad a' = (\lambda + r)(1 - \delta')\ell + r n - \xi_d - b'$$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$
$$W(z, \xi, a, \ell) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), \ell'(\delta')] \right\} \text{ s.t.}$$

$$(BC) \quad c + \bar{c}^f + n + \xi_n(n) \leq a + q(z, \xi, n, \ell, b')b' + \xi_d$$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, l) = \max \{0, W(z, a, l, \xi)\}$$
$$W(z, \xi, a, l) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), l'(\delta')] \right\} \text{ s.t.}$$

$$(KR) \quad \frac{n + l - \xi_d - q(z, \xi, l, n, b')b'}{\omega^r(n + l) + \omega^s \mathbf{1}_{b' < 0} b' q(z, \xi, l, n, b')} \geq \theta(z) \quad \text{or}$$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, l) = \max \{0, W(z, a, l, \xi)\}$$
$$W(z, \xi, a, l) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), l'(\delta')] \right\} \text{ s.t.}$$

(KR)  $c = n = 0$  and capital ratio  $> .02$

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$
$$W(z, \xi, a, \ell) = \max_{n \geq 0, c \geq b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), \ell'(\delta')] \right\} \text{ s.t.}$$

Note that the bank can lend  $b' < 0$ , it has operating costs  $\bar{c}^f$  (nonlinear

## MODEL: BANK'S PROBLEM

$$V(z, \xi, a, \ell) = \max \{0, W(z, a, \ell, \xi)\}$$
$$W(z, \xi, a, \ell) = \max_{n \geq 0, c \geq 0, b'} \left\{ u(c) + \beta \sum_{z', \xi', \delta'} \Gamma_{z\xi, z'\xi'} \pi_{\delta'|z'} V[z', \xi', a'(\delta'), \ell'(\delta')] \right\} \text{ s.t.}$$

$$(TL) \quad \ell' = (1 - \lambda)(1 - \delta')\ell + n$$

$$(TA) \quad a' = (\lambda + r)(1 - \delta')\ell + r n - \xi_d - b'$$

$$(BC) \quad c + \bar{c}^f + n + \xi_n(n) \leq a + q(z, \xi, n, \ell, b')b' + \xi_d$$

$$(KR) \quad \frac{n + \ell - \xi_d - q(z, \xi, \ell, n, b')b'}{\omega^r(n + \ell) + \omega^s \mathbf{1}_{b' < 0} b' q(z, \xi, \ell, n, b')} \geq \theta(z) \quad \text{or}$$

$$(KR) \quad c = n = 0 \quad \text{and capital ratio} > .02$$

Note that the bank can lend  $b' < 0$ , it has operating costs  $\bar{c}^f$  (nonlinear

## MODEL: SOLUTION OF BANKS PROBLEM GIVEN $q(\xi', \ell, n, b')$

---

- The solution to this problem is a set of functions

## MODEL: SOLUTION OF BANKS PROBLEM GIVEN $q(\xi', \ell, n, b')$

- The solution to this problem is a set of functions
  - $b'(z, \xi, a, \ell)$  bonds borrowing (or safe lending)

## MODEL: SOLUTION OF BANKS PROBLEM GIVEN $q(\xi', \ell, n, b')$

- The solution to this problem is a set of functions
  - $b'(z, \xi, a, \ell)$  bonds borrowing (or safe lending)
  - $n(z, \xi, a, \ell)$  new loans

## MODEL: SOLUTION OF BANKS PROBLEM GIVEN $q(\xi', \ell, n, b')$

- The solution to this problem is a set of functions
  - $b'(z, \xi, a, \ell)$  bonds borrowing (or safe lending)
  - $n(z, \xi, a, \ell)$  new loans
  - $c(z, \xi, a, \ell)$  dividends

## MODEL: SOLUTION OF BANKS PROBLEM GIVEN $q(\xi', \ell, n, b')$

- The solution to this problem is a set of functions
  - $b'(z, \xi, a, \ell)$  bonds borrowing (or safe lending)
  - $n(z, \xi, a, \ell)$  new loans
  - $c(z, \xi, a, \ell)$  dividends
  
- The solution yields a probability of a bank failing

## MODEL: SOLUTION OF BANKS PROBLEM GIVEN $q(\xi', \ell, n, b')$

- The solution to this problem is a set of functions
  - $b'(z, \xi, a, \ell)$  bonds borrowing (or safe lending)
  - $n(z, \xi, a, \ell)$  new loans
  - $c(z, \xi, a, \ell)$  dividends
- The solution yields a probability of a bank failing
  - $\delta^*(z, \xi, \ell, n, b')$

The only relevant equilibrium condition is

1. Zero profit in the bonds markets:

$$q(z, \xi, \ell, n, b') = \frac{1 - \delta^*(z, \xi, \ell, n, b')}{1 + \bar{r}}$$

## MODEL: AGGREGATE STATE, $\{z, x\}$

- The choices of the bank  $\{n(z, \xi, a, \ell), b'(z, \xi, a, \ell), c(z, \xi, a, \ell)\}$  and the exogenous shocks  $\{z', \xi', \delta'\}$  generate a transition for the state of each bank and in turn of the distribution of banks..

## MODEL: AGGREGATE STATE, $\{z, x\}$

- The choices of the bank  $\{n(z, \xi, a, \ell), b'(z, \xi, a, \ell), c(z, \xi, a, \ell)\}$  and the exogenous shocks  $\{z', \xi', \delta'\}$  generate a transition for the state of each bank and in turn of the distribution of banks..

## MODEL: AGGREGATE STATE, $\{z, x\}$

- The choices of the bank  $\{n(z, \xi, a, \ell), b'(z, \xi, a, \ell), c(z, \xi, a, \ell)\}$  and the exogenous shocks  $\{z', \xi', \delta'\}$  generate a transition for the state of each bank and in turn of the distribution of banks..

### Definition

A, equilibrium is a function  $x' = G(z, x)$ , a price of bonds  $q$ , and decisions for  $\{n, b', c\}$  such that banks maximize profits, lenders get the market return, and the measure is updated consistently with decisions and shocks.

## PUTTING THE MODEL TO USE

---

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.

## PUTTING THE MODEL TO USE

---

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:

## PUTTING THE MODEL TO USE

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:
  1. No Countercyclical Capital Requirement and adjusted  $\omega^r$  to reflect that the loans are riskier.

## PUTTING THE MODEL TO USE

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:
  1. No Countercyclical Capital Requirement and adjusted  $\omega^r$  to reflect that the loans are riskier.
    - More loans are destroyed

## PUTTING THE MODEL TO USE

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:
  1. No Countercyclical Capital Requirement and adjusted  $\omega^r$  to reflect that the loans are riskier.
    - More loans are destroyed
    - Outlook of loans is worse

## PUTTING THE MODEL TO USE

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:
  1. No Countercyclical Capital Requirement and adjusted  $\omega^r$  to reflect that the loans are riskier.
    - More loans are destroyed
    - Outlook of loans is worse
  2. No Countercyclical Capital Requirement but no adjustment in  $\omega^r w$ .

## PUTTING THE MODEL TO USE

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:
  1. No Countercyclical Capital Requirement and adjusted  $\omega^r$  to reflect that the loans are riskier.
    - More loans are destroyed
    - Outlook of loans is worse
  2. No Countercyclical Capital Requirement but no adjustment in  $\omega^r w$ .
  3. Countercyclical Capital Requirement to 1.

## PUTTING THE MODEL TO USE

- We pose an economy that (after many periods in good times) resembles a current distribution of banks.
- Then explore what happens upon the economy entering a recession, under various scenarios:
  1. No Countercyclical Capital Requirement and adjusted  $\omega^r$  to reflect that the loans are riskier.
    - More loans are destroyed
    - Outlook of loans is worse
  2. No Countercyclical Capital Requirement but no adjustment in  $\omega^r w$ .
  3. Countercyclical Capital Requirement to 1.
  4. Countercyclical Capital Requirement to 2.

- Describe Targets

- Describe Targets
- Describe properties of the stationary allocation in good times.

- Describe Targets
- Describe properties of the stationary allocation in good times.
- Describe the transition when the economy switches to a recession.

- We have the following industry properties

	(Canadian) Data	Model
Bank failure rate	0.22%	0.23%
Capital ratio	14.4%	16.7%
Wholesale Funding	27.0%	20.3%

- We have the following industry properties

	(Canadian) Data	Model
Bank failure rate	0.22%	0.23%
Capital ratio	14.4%	16.7%
Wholesale Funding	27.0%	20.3%

- We have the following industry properties

	(Canadian) Data	Model
Bank failure rate	0.22%	0.23%
Capital ratio	14.4%	16.7%
Wholesale Funding	27.0%	20.3%

## Normalized T-Account of Banking Industry

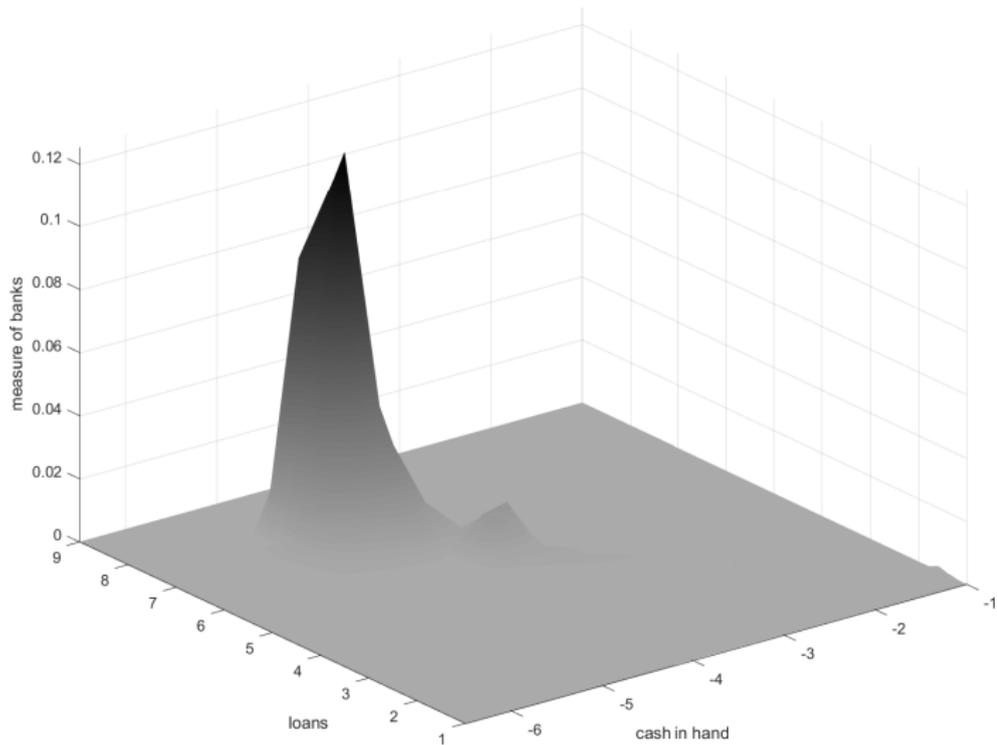
Canadian Data			
New Loans	1.07	Deposits	3.31
Existing Loans	4.87	Wholesale Funding	1.63
		Own Capital	1.00

Model			
New Loans	1.09	Deposits	3.80
Existing Loans	4.93	Wholesale Funding	1.22
		Own Capital	1.00

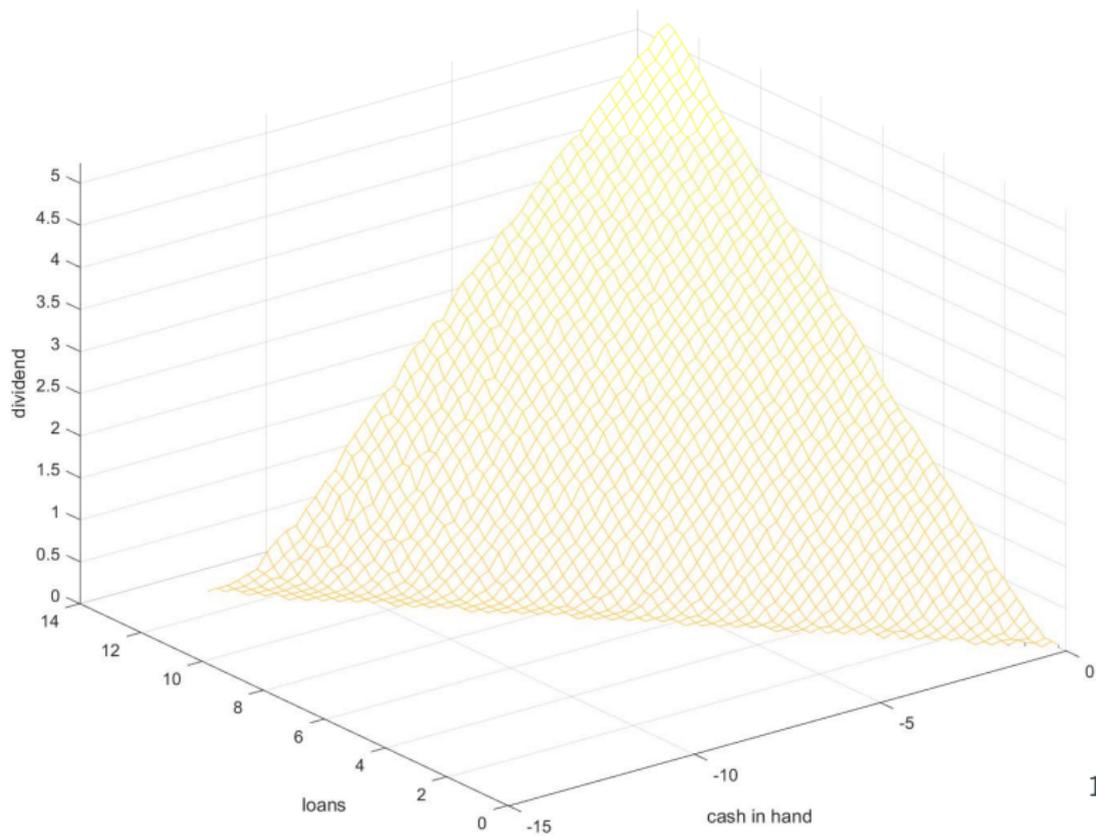
## MODEL PARAMETERS

Parameter	Value	Description
$\xi_n$	0.2	Loan issuance cost: $\chi(n, \xi_n) = 0.5 \xi_n n^2$
$\xi_d$	5	Deposits
$\beta$	0.95	Subjective discount factor
$\lambda$	0.2	Maturity rate of long-term loans
$r$	0.1	Bank lending rate
$r_f$	0.005	Risk-free rate
$\sigma$	0.9	$u(c) = c^\sigma$
$\omega_r$	1	Risk weight on risky loans
$\omega_s$	0	Risk weight on safe assets
$\Gamma_{z=G, z'=G}$	0.99	$\Pr(z' = G   z = G)$
$\Gamma_{z=B, z'=B}$	0.80	$\Pr(z' = B   z = B)$
$E(\delta   z = G)$	0.025	$\Sigma_\delta \delta \cdot \pi(\delta   z = G)$
$V(\delta, Z = G)$	0.0017	$\alpha(Z = G) = 0.3334, \beta(Z = G) = 13.0015$
$E(\delta   z = B)$	0.040	$\Sigma_\delta \delta \cdot \pi(\delta   z = B)$

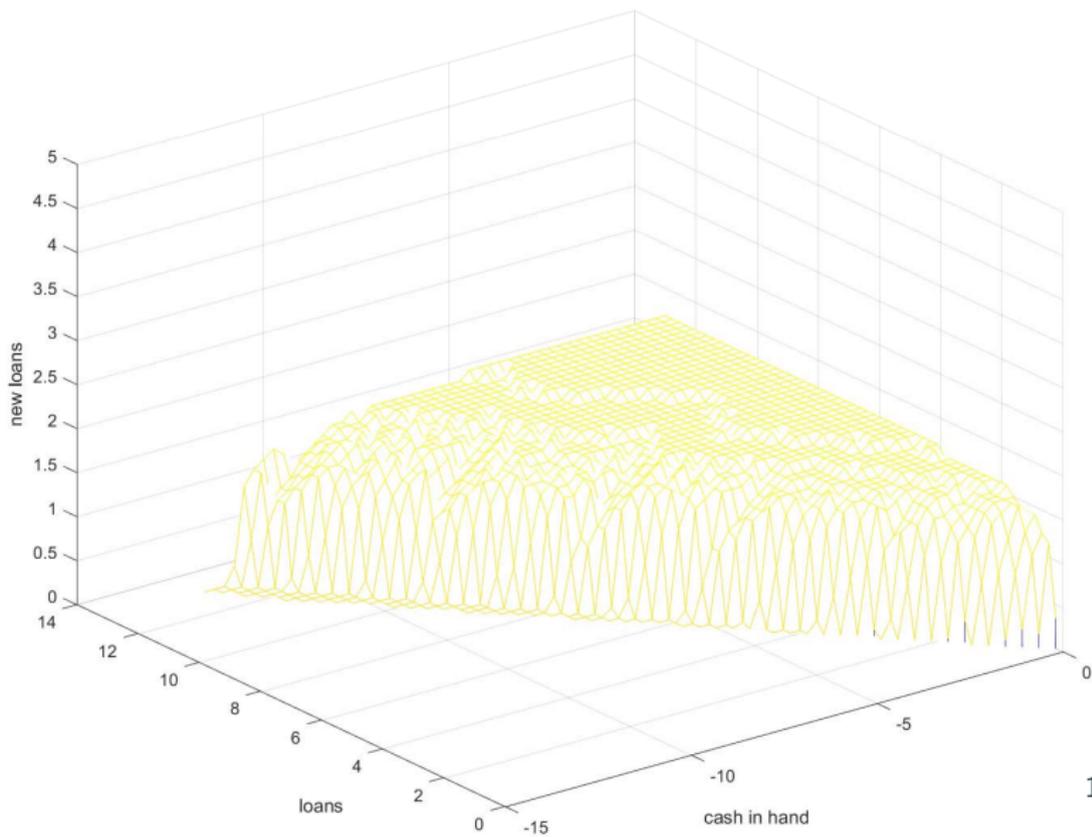
# DISTRIBUTION OF BANKS



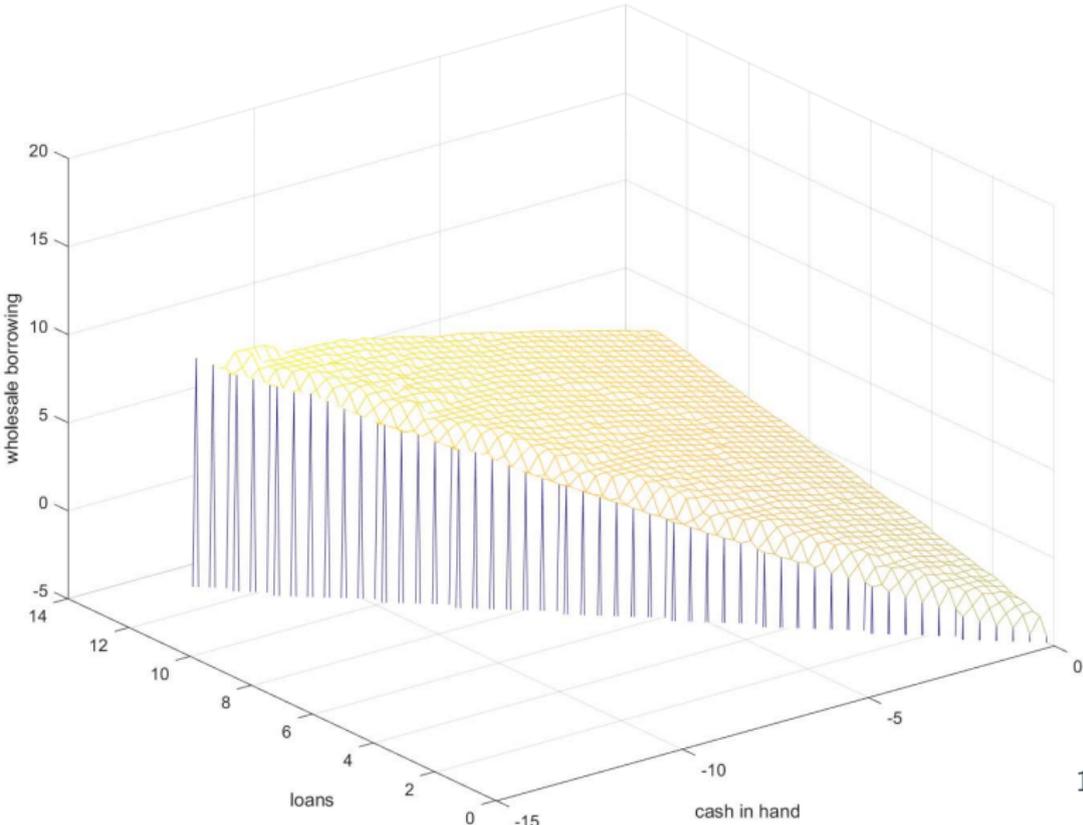
# BANKS DIVIDENDS



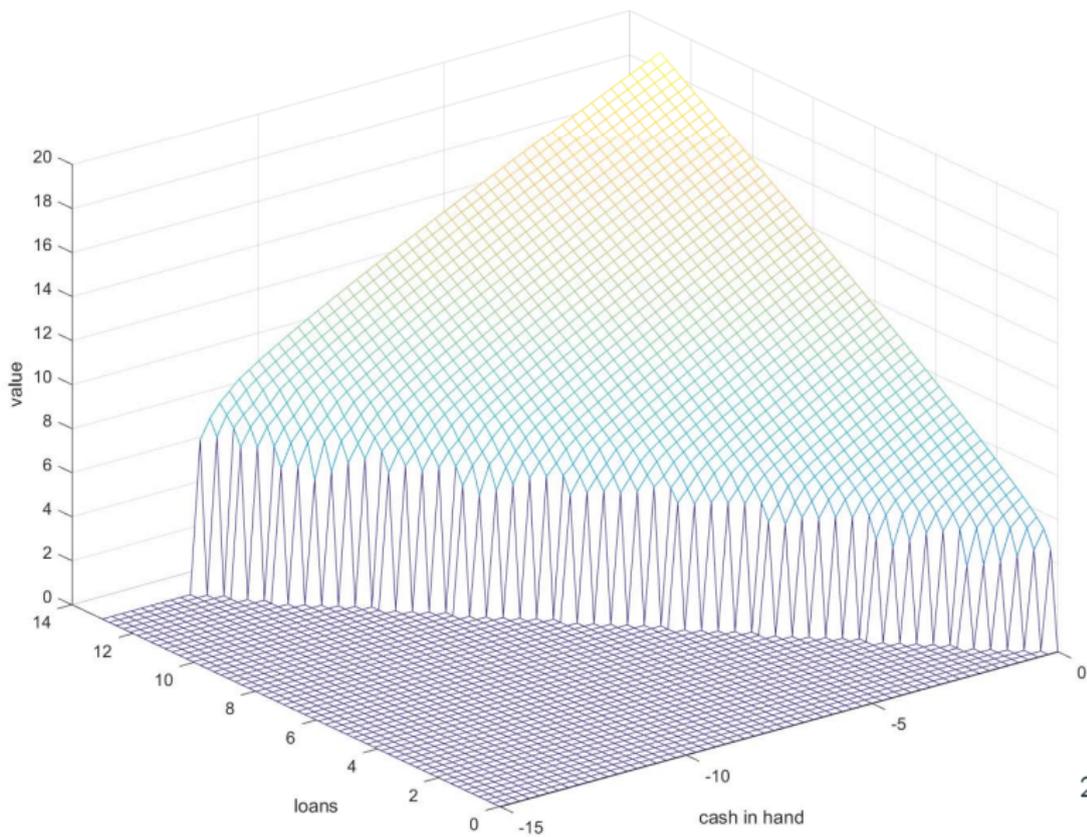
# BANKS NEW LOANS ISSUE



# BANKS WHOLESALE FUNDING (DEPOSITS PLUS BONDS)

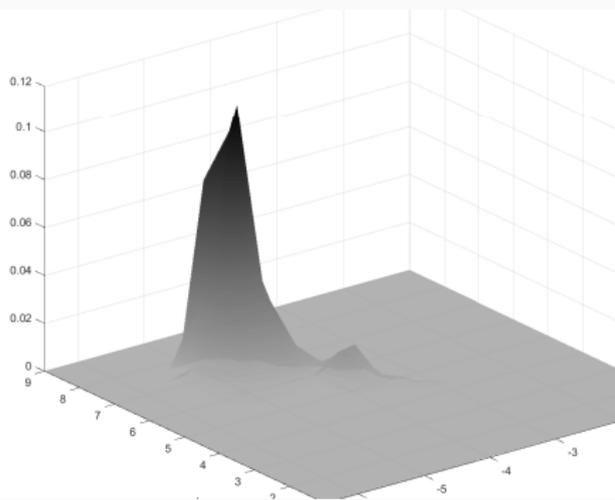
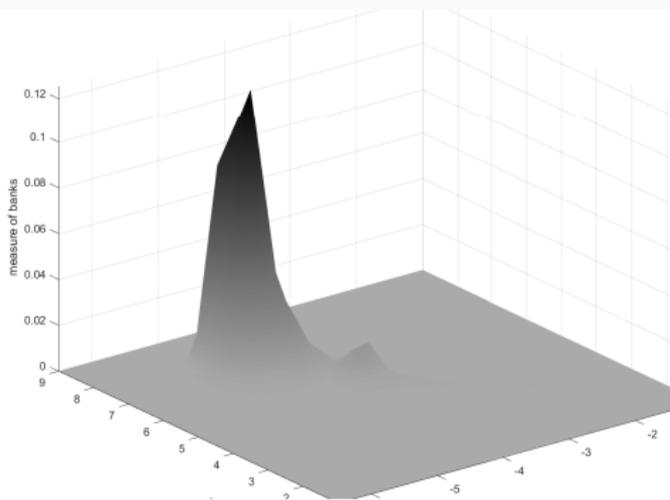


# BANKS VALUE FUNCTION

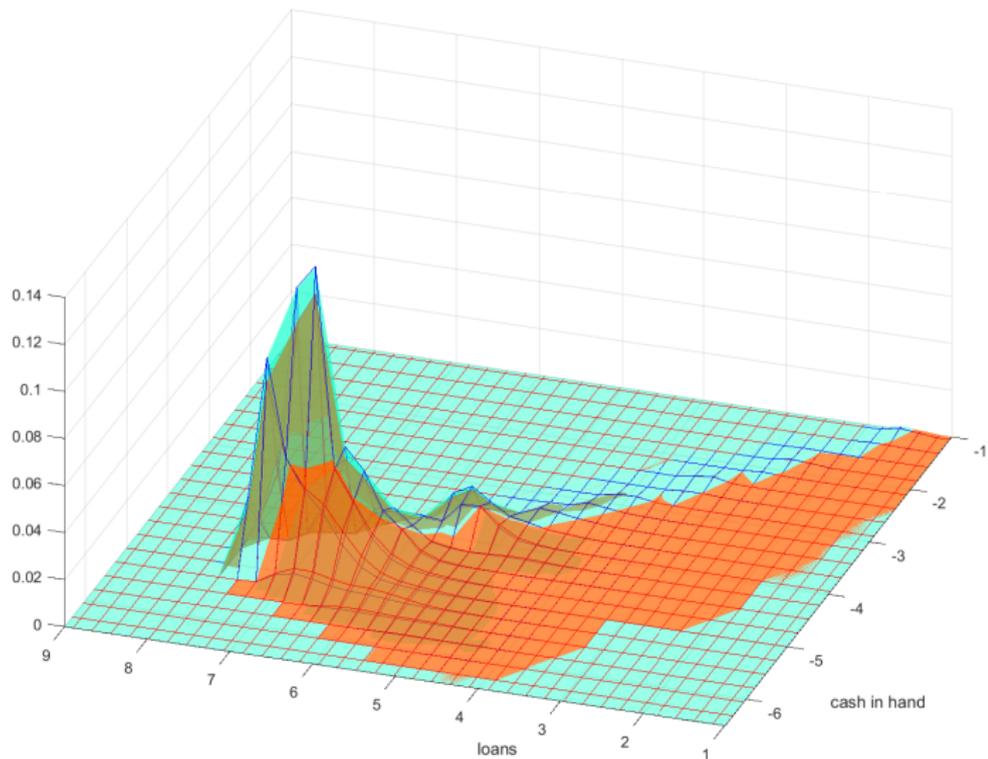


- Imagine the shock  $\Delta(\delta) = 0.015$  (from .025 to .04) hits all banks, which happens with a very small probability, 0.01. The crisis continues for two periods and ends to go back to the good aggregate state thereafter.
- Some banks are in better financial shape than others.
- We explore the recovery of the Banking sector under the four scenarios.
- What happens upon

# A NASTY CRISIS WITH AND WITHOUT CCyB



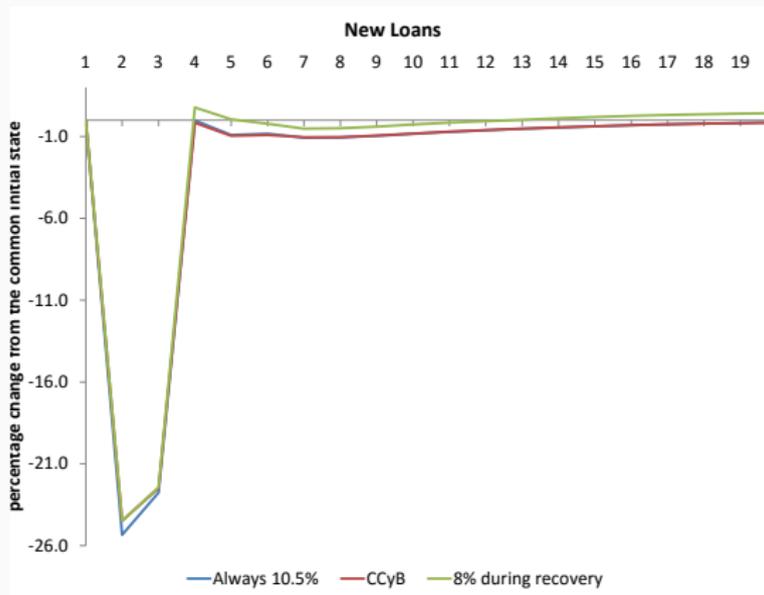
# A NASTY CRISIS WITH AND WITHOUT CCyB



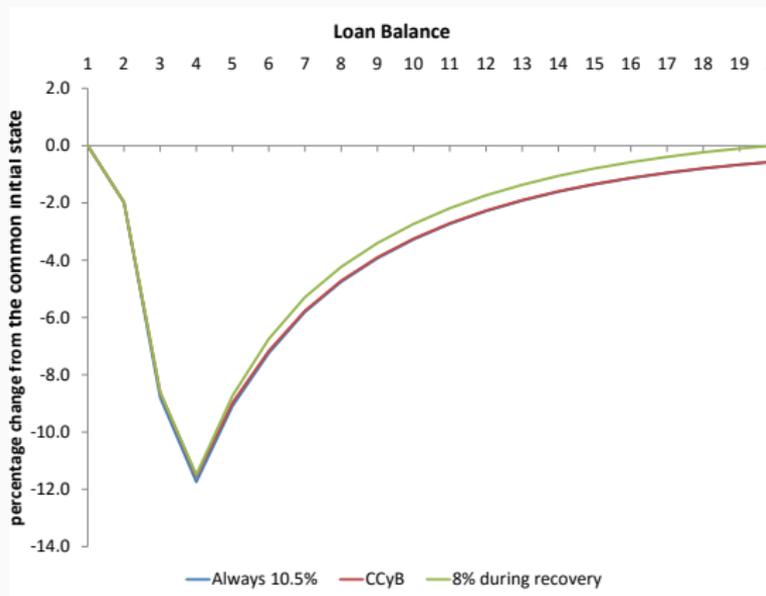
- Recall that it is a recession for two periods and then we have a recovery.
- We compare Countercyclical Capital Requirement with a constant weight to risk assets (left )and with a variable weight (right)
- We look at impulse responses

## NEW LENDING

Small difference between non-contingent policy and CCyB during the downturn. CCyB (if low capital requirement extends for a longer period) provides some help during the recovery.

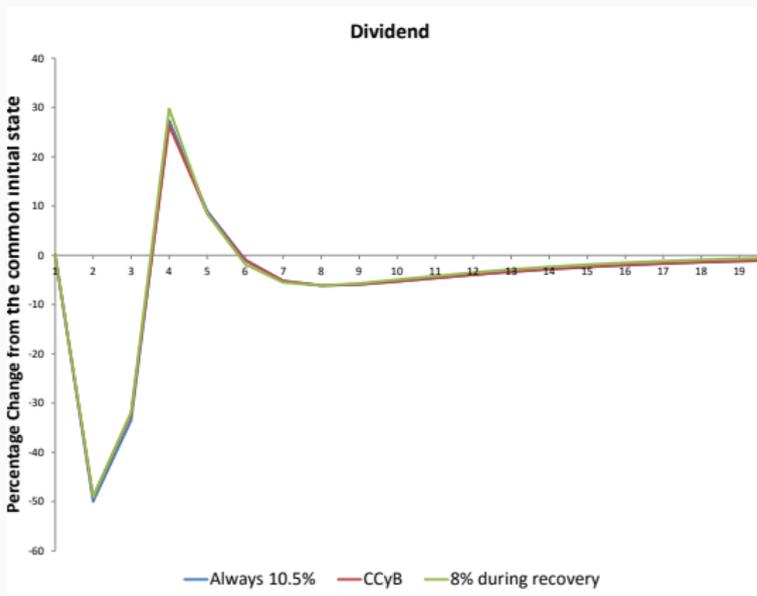


# STOCK OF LOANS



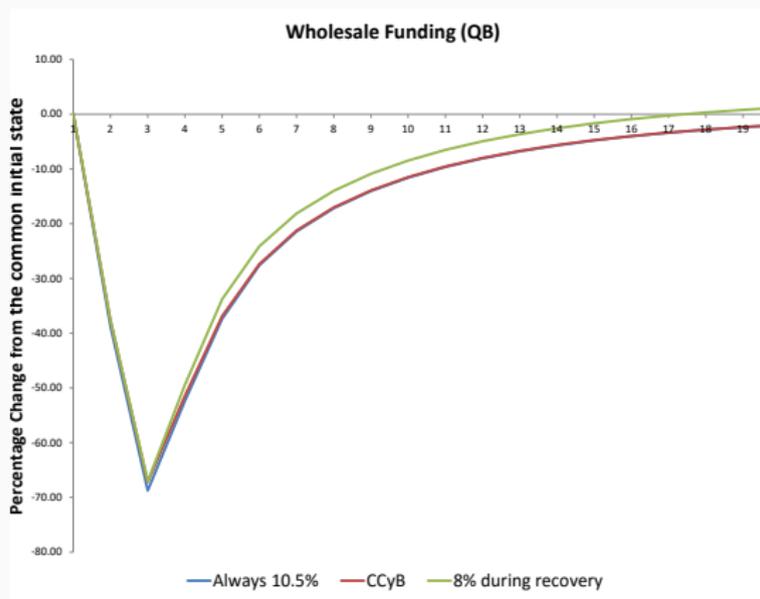
- Almost no difference between non-contingent policy and CCyB

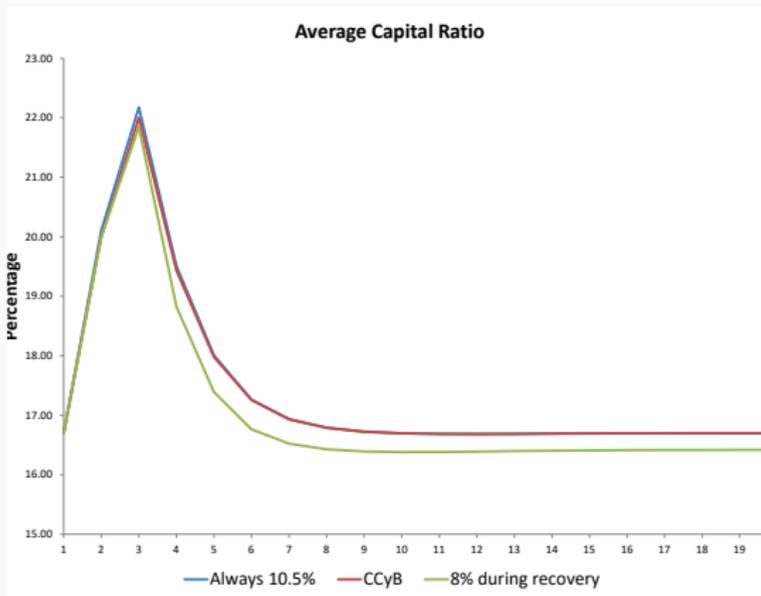
# DIVIDENDS



- Again almost no difference

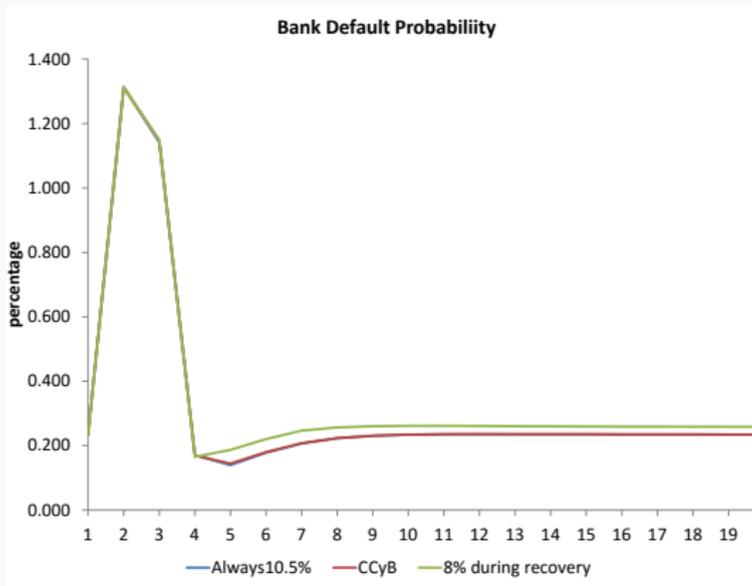
# WHOLESALE FUNDING



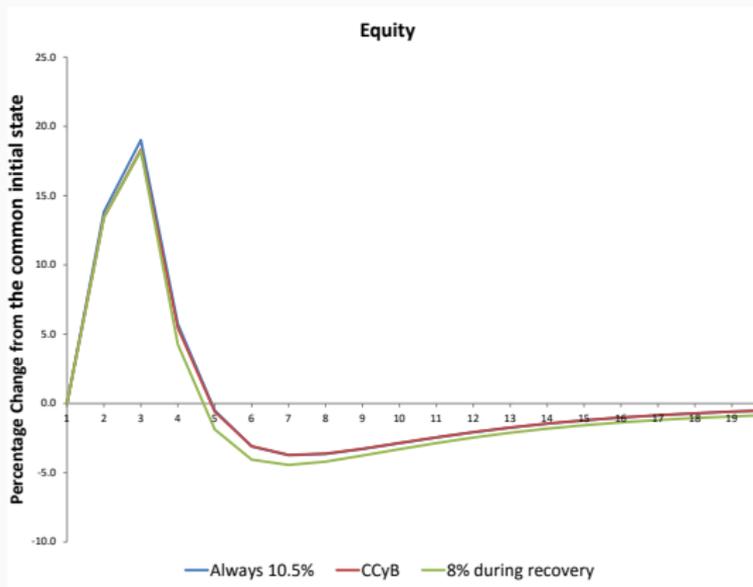


- Almost no difference, the capital ratios go up under both non-contingent and CCyB.

# BANK FAILURE RATES

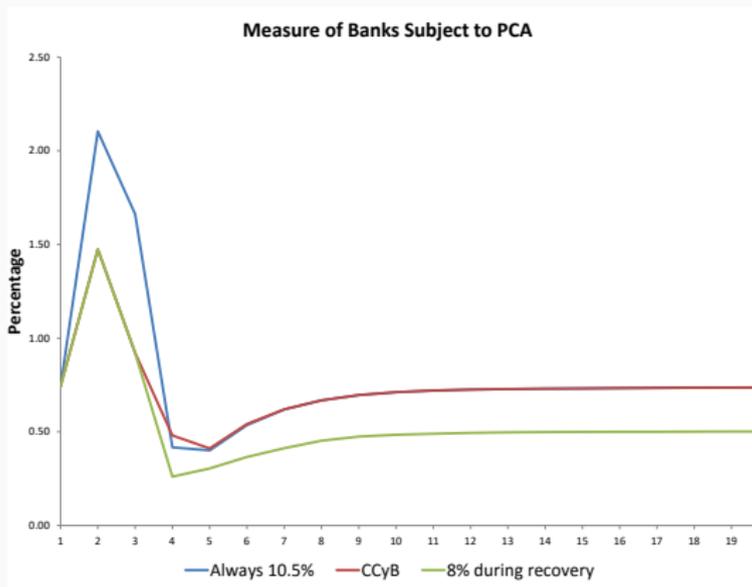


# BANK EQUITY



- Own capital is somewhat affected.

# FRACTION OF CAPITAL REQUIREMENT VIOLATION



- This is what the Counter Cyclical Capital Requirement directly does.

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.
- Need to pose this industry into a GE framework so ALL interest rates can be determined endogenously. Hard. We are doing it.

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.
- Need to pose this industry into a GE framework so ALL interest rates can be determined endogenously. Hard. We are doing it.
- Bank Runs:

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.
- Need to pose this industry into a GE framework so ALL interest rates can be determined endogenously. Hard. We are doing it.
- Bank Runs:
  - Can be interpreted as a low probability state with  $\xi_d = 0$

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.
- Need to pose this industry into a GE framework so ALL interest rates can be determined endogenously. Hard. We are doing it.
- Bank Runs:
  - Can be interpreted as a low probability state with  $\xi_d = 0$
  - For shadow banking we need some multiple equilibrium notions á la Cole and Kehoe (2000)

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.
- Need to pose this industry into a GE framework so ALL interest rates can be determined endogenously. Hard. We are doing it.
- Bank Runs:
  - Can be interpreted as a low probability state with  $\xi_d = 0$
  - For shadow banking we need some multiple equilibrium notions á la Cole and Kehoe (2000)
- Notion of “systemic” banks. It needs a good theory of drops in

- Competitive Theory of Lending (Corbae and D'Erasmus (2016))
- Firms have zero measure. That is not a problem. We can wipe out a positive measure of financial institutions and call it one bank.
- Need to pose this industry into a GE framework so ALL interest rates can be determined endogenously. Hard. We are doing it.
- Bank Runs:
  - Can be interpreted as a low probability state with  $\xi_d = 0$
  - For shadow banking we need some multiple equilibrium notions á la Cole and Kehoe (2000)
- Notion of “systemic” banks. It needs a good theory of drops in

## TEMPORARY CONCLUSIONS

---

- A model to measure effects of countercyclical capital requirements.

## TEMPORARY CONCLUSIONS

---

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:

## TEMPORARY CONCLUSIONS

---

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard

## TEMPORARY CONCLUSIONS

---

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard
  2. Bank's risk taking that can lead to its failure

## TEMPORARY CONCLUSIONS

---

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard
  2. Bank's risk taking that can lead to its failure
  3. Endogenous bank funding risk premium

## TEMPORARY CONCLUSIONS

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard
  2. Bank's risk taking that can lead to its failure
  3. Endogenous bank funding risk premium
  4. Maturity mismatch between long-term loans & short-term funding

## TEMPORARY CONCLUSIONS

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard
  2. Bank's risk taking that can lead to its failure
  3. Endogenous bank funding risk premium
  4. Maturity mismatch between long-term loans & short-term funding
- Lowering capital requirements has little effect because banks are already concerned.

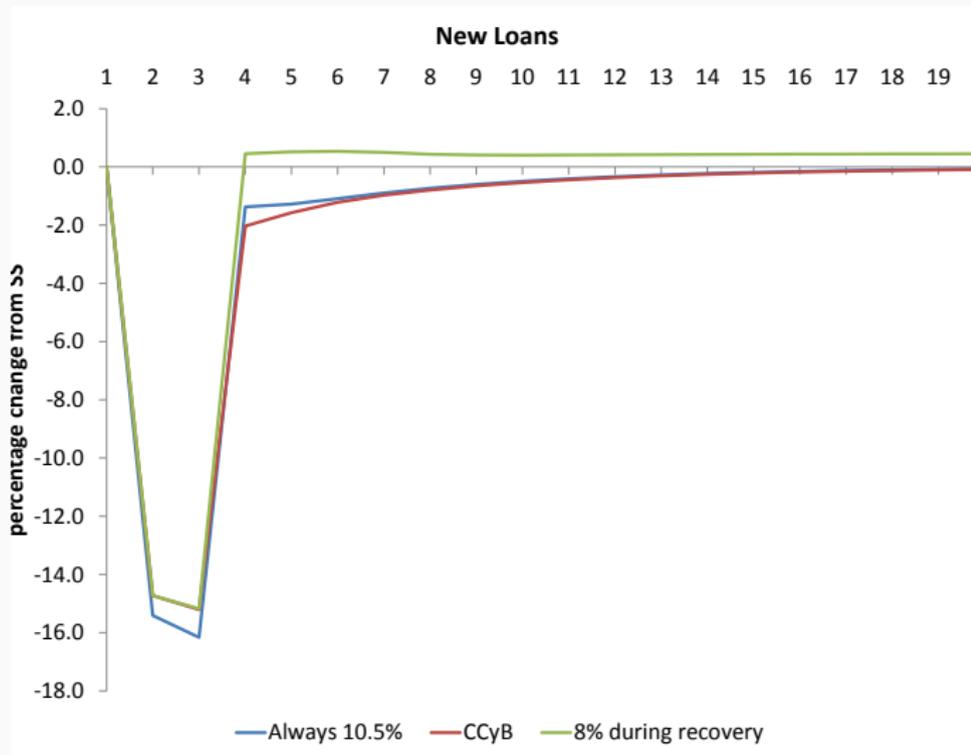
## TEMPORARY CONCLUSIONS

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard
  2. Bank's risk taking that can lead to its failure
  3. Endogenous bank funding risk premium
  4. Maturity mismatch between long-term loans & short-term funding
- Lowering capital requirements has little effect because banks are already concerned.
- There is a rationale for delaying the tightening of capital requirement when the recession ends.

## TEMPORARY CONCLUSIONS

- A model to measure effects of countercyclical capital requirements.
- We insist in the model capturing certain margins that we deem important:
  1. Moral Hazard
  2. Bank's risk taking that can lead to its failure
  3. Endogenous bank funding risk premium
  4. Maturity mismatch between long-term loans & short-term funding
- Lowering capital requirements has little effect because banks are already concerned.
- There is a rationale for delaying the tightening of capital requirement when the recession ends.
- Perhaps our findings will change when we fine tune the

# NEW LENDING BY BANKS: WITH 8% CAPITAL REQUIREMENT DURING RECOVERY



- Consider a household with per period utility function  $u(c, d)$ , where  $d$  stands for deposits' services.

- Consider a household with per period utility function  $u(c, d)$ , where  $d$  stands for deposits' services.
- Deposits are created via matches with banks. Total (and per capita) deposits are the aggregate of bank services. We can think of a matching function with banks.

$$D = \int \xi_d dx$$

- Consider a household with per period utility function  $u(c, d)$ , where  $d$  stands for deposits' services.
- Deposits are created via matches with banks. Total (and per capita) deposits are the aggregate of bank services. We can think of a matching function with banks.

$$D = \int \xi_d dx$$

- Households own shares of a mutual fund

# References

---

- Cole, Harold L. and Timothy J. Kehoe. 2000. "Self-Fulfilling Debt Crises." *The Review of Economic Studies* 67 (1):91–116. URL <http://www.jstor.org/stable/2567030>.
- Corbae, Dean and Pablo D'Erasmus. 2016. "A Simple Quantitative General Equilibrium Model of Banking Industry Dynamics." Mimeo University of Wisconsin  
<https://sites.google.com/site/deancorbae/system/errors/NodeNotFound?suri=wuid:gx:269f9ebf1dc6b8aa&attredirects=0>.
- Corbae, Dean, Pablo D'Erasmus, Sigurd Galaasen, Alfonso Irarrazabal, and Thomas Siemsen. 2016. "Structural Stress Tests." Mimeo, University of Wisconsin.
- Davydiuk, Tetiana. 2017. "Dynamic Bank Capital Requirements."  
<https://drive.google.com/file/d/0B90xWOjYKvFlbHg3WW56b0NHeTA/view?usp=sharing>.

# Representative Bank-Representative Household version of Dynamics and Capital Regulation

---

José-Víctor Ríos-Rull

*University of Pennsylvania*

Tamon Takamura

*Bank of Canada*

Yaz Terajima

*Bank of Canada*

May 25, 2017

# 1 Linear Costs for Banks

# GENERAL EQUILIBRIUM MODEL

- There is a household sector with indivisible labor (many workers in a household).
- There is a banking sector that produces deposits' services and make loans with CRS.
- There is a productive sector with a putty clay technology.
- Otherwise it is a growth model.
- There may be shocks to TFP, to the destruction of new and old firms, and to the banking management losses.
- But we start looking at a steady state

# HOUSEHOLDS

- Period utility  $u(c, n, d)$ , where  $n$  is the fraction employed and  $d$  stands for deposits' services. Discount rate  $\beta$ .
- Deposits are created via matches with banks. We can think of a matching function with banks.
- A household has a measure one of workers that may or may not have a job. Employment in loan firms is  $n^l$  while employment in equity firms is  $n^e$ ,  $n^l + n^e \leq 1$ . A household member that does not work gets  $\bar{c}$  units of utility consumption.

$$u(c, n, d) = \log c + (1 - n)b + v(d)$$

## INVESTMENT AND FIRMS: PUTTY-CLAY

- Firms create plants with one worker using loans in a putty-clay fashion  $y = A k^\alpha$ .
- There is free entry of these firms. Upon entry, firms (which are worth zero) join a mutual fund with their liabilities.
- With prob  $\lambda$  loans are paid off.
- All firms get destroyed with probability  $\delta \sim \gamma_\delta$ .
- Extensive margin: There are  $N^n$  new firms each period.
- Intensive margin: Each period firms invest  $k$  units.
- Total amount of new loans is  $L^n = k * N^n$ .
- The whole distribution of firms can be summarized by two aggregates (as in Choi and Ríos-Rull (2010) and others)
- Employment or the number of plants is

$$N' = (1 - \delta)N + N^n.$$

- Output is

$$Y' = (1 - \delta')Y + N^n A k^\alpha.$$

## INVESTMENT AND FIRMS

- Firms borrow at rate  $r^\ell$ .
- The value a newly opened firm with capital  $k$  using the effective household interest rate  $r^b$  is

$$\frac{\Pi^f(k)}{1+r^b} = \frac{[Ak^\alpha - w(k) + \frac{1-\delta'}{1+r^b}\Pi^f(k)]}{1+r^b}$$

where  $w(k)$  are wages and  $r^b$  is the market discount rate. So

$$\Pi^f(k) = \frac{1+r^b}{r^b+\delta} [Ak^\alpha - w(k)].$$

- The cost of a loan of size  $k$  is

$$\sum_{t=1}^{\infty} k \left[ r^\ell + \frac{\lambda}{1-\lambda} \right] \left( \frac{1-\lambda}{1+r^b} \right)^t = k \left[ r^\ell + \frac{\lambda}{1-\lambda} \right] \frac{1-\lambda}{r^b+\lambda}.$$

## INVESTMENT DECISION

- So the optimal size satisfies

$$\max_k \frac{Ak^\alpha - w(k)}{r^b + \delta} - k \left[ r^\ell + \frac{\lambda}{1 - \lambda} \right] \frac{1 - \lambda}{r^b + \lambda}.$$

- With FOC

$$A \alpha k^{\alpha-1} - w_k(k) = [(1 - \lambda)r^\ell + \lambda] \frac{r^b + \delta}{r^b + \lambda}.$$

- Firms enter until there are zero profits from doing so

$$\frac{Ak^\alpha - w(k)}{r^b + \delta} = k \left[ r^\ell + \frac{\lambda}{1 - \lambda} \right] \frac{1 - \lambda}{r^b + \lambda}.$$

## FIRMS PROFITS AND LOSSES

- Because upon creation firms are worth zero there is no need to worry about their value.
- Once created, firm's profits or losses go to the households who do not buy and sell firms and take those profits as given.
- Profits of all firms are

$$\pi^f = Y - W N - L[(1 - \lambda)r^\ell + \lambda]$$

# WAGE DETERMINATION

- A bargaining process between the firm and the worker.  $V$ : (We may change this to get more wage rigidity and avoid the Shymer puzzle)
- The bargaining process is repeated every period and if unsuccessful neither firm nor worker can partner with anybody else within a period. Let  $\mu$  be the bargaining weight of the worker. Then, because of log utility, we have

$$w(k) = \mu A k^\alpha + (1 - \mu) \frac{b}{C}$$

- Total (per capita) Labor Income paid in the Economy are

$$W N = N \left[ \mu A k^\alpha + (1 - \mu) \frac{b}{C} \right] = \mu Y + (1 - \mu) \frac{Nb}{C}$$

# BANKING INDUSTRY I

- A CRS banking industry uses output to produce deposits and to make loans
- Loans are long term and decay at rate  $\lambda$ . Deposits are short term.
- It borrows and lends short term bonds  $B'$  at interest rate  $r^b$ .
- A fraction  $\delta^\ell$  of the loans are destroyed **V: (Still have to discuss the relation between  $\delta$  and  $\delta^\ell$ )**

$$D' = \kappa_d Y^d$$

$$L^n = \kappa_\ell Y^\ell$$

$$L' = (1 - \delta'^\ell)(1 - \lambda)L + L^n$$

- Banks cash position

$$A' = (\lambda + r^\ell(1 - \lambda))(1 - \delta'^\ell)L + r^\ell L^n - D'(1 + r^d) - B'(1 + r)$$

- Bank's Budget Constraint ( $\pi^B$  are dividends)

$$\pi^B + L^n \left( 1 + \frac{1}{\kappa_\ell} \right) = A + B' + D' \left( 1 - \frac{1}{\kappa_d} \right)$$

- Due to linearity of technology banks have zero steady state profits.  
 $\pi^B = 0$ .
- This is not the case outside steady state.

- Let  $r^\ell(r^b)$  and  $r^b(r^b)$  be the interest rates of bonds and deposits when the Capital Requirement constraint is not binding.

$$1 + \frac{1}{\kappa_\ell} = \sum_{t=1}^{\infty} \left[ \frac{(1-\lambda)(1-\delta)}{1+r^b} \right]^{t-1} [(1-\lambda)r^\ell + \lambda]$$

$$r^d = r^b - \kappa_d$$

$$r^\ell = \left[ \left( 1 + \frac{1}{\kappa_\ell} \right) \frac{r^b + \lambda + \delta - \lambda\delta}{(1+r^b)} - \lambda \right] \frac{1}{1-\lambda}$$

- Households lend funds to banks at rate  $r^b$ . We call them bonds,  $B$ .

- Budget constraint of households

$$c + d' + b' = b(1 + r^b) + d(1 + r^d) + Wn + \pi^f + \pi^b$$

## DEFINITION OF A STEADY-STATE EQUILIBRIUM

- Stocks:  $Y, N, \Pi, A, B, L, D,$
- Choices:  $K, C, A', B', D', L^N, N^n,$  s.t.
- Prices  $r^\ell, r^b, r^d, W, w(k)$
- Profits  $\pi^f, \pi^B$ 
  1. Plant sizes are optimal
  2. Entry yields zero profits
  3. Households solve their problem  $r^b = \beta^{-1}, u_c = u_d \frac{1}{\kappa_d}$
  4. Wages are determined by Nash bargaining
  5. The choices imply that the stocks repeat themselves

## NON-STEADY-STATE EQUILIBRIUM: SHOCKS FOR $\eta = \{z, \delta, \delta^\ell\}$

- As is standard in putty-clay models, there is no need to keep track of the whole distribution of firms. Only of output and number of plants/workers. The aggregate state vector  $S$  consists of
  - The shocks  $\eta$
  - $Y$  Output
  - $N$  Employment or number of plants
  - $A$  Banks Cash
  - $B$  Bonds
  - $D$  Deposits
  - $L$  Loans
- Households also have an idiosyncratic state vector  $s = \{b, d, n\}$ .

# HOUSEHOLD PROBLEM

$$v(S, s) = \max_{c, b', d'} u(c, d, n) + \beta E \{v(S', s') | S, s\} \quad \text{s.t.}$$

$$c + d' + b' = b[1 + r^b(S)] + d[1 + r^d(S)] + W(S)n + \pi^f(S) + \pi^b(S)$$

$$N'(S) = (1 - \delta')N + N^n(S)$$

$$n'(S, s) = (1 - \delta')n(S, s) + N^n(S)$$

$$Y'(S) = (1 - \delta')Y + N^n(S) z A k(S)^\alpha$$

$$L'(S) = (1 - \delta'^\ell)(1 - \lambda)L + L^n(S)$$

$$A'(S) = A'(S)$$

$$B'(S) = B'(S)$$

$$D'(S) = D'(S)$$

- With solution  $d'(S, s)$  and  $b'(S, s)$ , as well as  $v(S, s)$

## FIRMS' PROBLEM

- The value of firms with loans  $\Pi^\ell$  and of firms without loans  $\Pi^e$  is

$$\Pi^\ell(S, k) = zAk^\alpha - w(S, k) - kr^\ell(S) + \mathbb{E} \left\{ (1 - \delta') \frac{(1 - \lambda)\Pi^\ell(S', k) + \lambda[\Pi^e(S', k) - k]}{1 + r^b(S')} \mid S \right\}$$

$$\Pi^e(S, k) = zAk^\alpha - w(S, k) + \mathbb{E} \left\{ (1 - \delta') \frac{\Pi^e(S', k)}{1 + r^b(S')} \mid S \right\}$$

- The cost of a loan of size  $k$  is  $\mathbb{E} \left\{ \frac{kr^\ell(S') + \frac{\Phi(S', k)}{1 + r^b(S')}}{1 + r^b(S')} \mid S \right\}$

$$\Phi(S, k) = k[(1 - \lambda)r^\ell + \lambda] + (1 - \lambda) \mathbb{E} \left\{ \frac{(1 - \delta')\Phi(S', k)}{1 + r^b(S')} \mid S \right\}$$

## FIRMS' PROBLEM II

- So the optimal size satisfies

$$\max_k E \left\{ \frac{\Pi^\ell(S', k)}{1 + r^b(S')} - \frac{kr^\ell(S') + \frac{\Phi(S'', k)}{1 + r^b(S'')}}{1 + r^b(S')} \mid S \right\}$$

- **V: COMPUTE THE FOC**
- Firms enter until there are zero profits from doing so

$$E \left\{ \frac{\Pi^\ell(S', k)}{1 + r^b(S')} \mid S \right\} = E \left\{ \frac{kr^\ell(S') + \frac{\Phi(S'', k)}{1 + r^b(S'')}}{1 + r^b(S')} \mid S \right\}$$

# RECURSIVE COMPETITIVE EQUILIBRIUM

- Laws of motion  $N'(S), Y'(S), L'(S), B'(S), D'(S)$ ,
  - Decision rules and value functions for households  $d'(S, s), b'(S, s)$ , and  $v(S, s)$ , and firms  $k(S), N^n(S), \Pi^\ell(S), \Pi^e(S)$ .
  - Prices  $r^b(S), r^\ell(S), r^d(S), w(S, k), W(S)$ , and Profits  $\pi^f(S), \pi^B(S)$
1. Households and Firms solve their problems
    - 1.1 Euler equation of Households  $u_c(S) = E\{\beta(1 + r^b(S'))u_c(S') \mid S\}$ .
    - 1.2 Marginal utility of deposits equals  $E\left\{\frac{r^b(S') - r^d(S')}{1 + r^b(S')} \mid S\right\}$
    - 1.3 Optimal choice of  $k$
  2. Rep Agent:  $B'(S) = b'(S, s(S)), D'(S) = D'(S, s(S)), n'(S, s(S)) = N'(S)$ .
  3. Interest rates yield zero expected profits to banks
  4. Realized profits are

$$\begin{aligned}\pi^f(S) &= zY - NW - L[(1 - \lambda)r^b + \lambda L] \\ \pi^B(S) &= A - (1 - \lambda)(1 - \delta)L\end{aligned}$$

5. Wages are set by Nash bargaining.

## 2 Non-linear Costs for Banks

# BANKING INDUSTRY I

- Banks use output to produce deposits and to make loans,  $d' = \kappa_d y^d$  and  $\ell^n = \kappa_\ell y^\ell$ .
- Loans are long term and decay at rate  $\lambda$ . Deposits are short term.
- It borrows and lends short term bonds  $B'$  at interest rate  $r^b$ .
- A random fraction  $\delta^\ell$  of the loans are destroyed. There are increasing costs with that destruction:  $\ell' = (1 - \delta'^\ell)(1 - \lambda)\ell + \ell^n$
- Banks cash position

$$a' = (\lambda + r^\ell(1 - \lambda))(1 - \delta^\ell)\ell + r^\ell \ell^n - d'(1 + r^d) - b'(1 + r^b) - \xi(\delta^\ell)\ell$$

- There is a capital requirement

$$\frac{\ell + \ell^n - d' - b'}{\ell + \ell^n} \geq \theta$$

- There is curvature in the bank's dividends  $\Phi(m)$

## BANKING INDUSTRY: BANKS PROBLEM

$$\Omega(S, a, \ell) = \max_{d', b', \ell^n} \Phi \left[ a - \ell^n \left( 1 + \frac{1}{\chi \ell} \right) + d' \left( 1 - \frac{1}{\chi \ell} \right) + b' \right] + \\ + E \left\{ \frac{\Omega[S', a'(S'), \ell'(S')]}{1 + r^b(S')} \mid S \right\} \quad \text{s.t.}$$

$$a'(S') = (\lambda + r^\ell(S')(1 - \lambda))(1 - \delta^\ell)\ell + r^\ell(S')\ell^n - \\ d'[1 + r^d(S')] - b'[1 + r^b(S')] - \xi(\delta^\ell)\ell$$

$$\ell'(S') = (1 - \delta^\ell)(1 - \lambda)\ell + \ell^n$$

$$\theta \leq \frac{\ell + \ell^n - d' - b'}{\ell + \ell^n}$$

## FIRST ORDER CONDITIONS

- Dividends and bonds interest rates are linked mechanically as they are perfect substitutes for banks. Wrt new loans  $\ell^n$  we have

$$-\phi_m \left(1 + \frac{1}{\chi_\ell}\right) + E \left\{ \frac{r^\ell \Omega'_2 + \Omega'_3}{1 + r^b(S')} \right\} + \mu(KREQ) = 0$$

- WRT bonds we have

$$\phi_m - E\{\Omega'_2\} - \mu(KREQ) = 0$$

- The envelope conditions tell us that

$$\begin{aligned}\Omega_2 &= \phi_m + \frac{\partial \ell^n}{\partial a} \left[ \phi_m \left(1 + \frac{1}{\chi_\ell}\right) + E \left\{ \frac{r^\ell \Omega'_2 + \Omega'_3}{1 + r^b(S')} \right\} + \mu(KREQ) \right] \\ \Omega_3 &= E\{(\lambda + r^\ell(S')(1 - \lambda))(1 - \delta^\ell) - \xi(\delta^\ell)\} + E\{(1 - \delta'^\ell)(1 - \lambda)\Omega'_3\}\end{aligned}$$

- Let  $r^\ell(r^b)$  and  $r^b(r^b)$  be the interest rates of bonds and deposits when the Capital Requirement constraint is not binding.

$$1 + \frac{1}{\kappa_\ell} = \sum_{t=1}^{\infty} \left[ \frac{(1-\lambda)(1-\delta)}{1+r^b} \right]^{t-1} [(1-\lambda)r^\ell + \lambda]$$

$$r^d = r^b - \kappa_d$$

$$r^\ell = \left[ \left( 1 + \frac{1}{\kappa_\ell} \right) \frac{r^b + \lambda + \delta - \lambda\delta}{(1+r^b)} - \lambda \right] \frac{1}{1-\lambda}$$

- 
-

## MODEL: AN EXTENSION SHADOW BANKING

- Brought to center stage by the troubles of Home Capital in Canada

## MODEL: AN EXTENSION SHADOW BANKING

- Brought to center stage by the troubles of Home Capital in Canada
- No deposits ( $\xi_d = 0$ ), just bonds, but particularly good at issuing high risk loans.

## MODEL: AN EXTENSION SHADOW BANKING

- Brought to center stage by the troubles of Home Capital in Canada
- No deposits ( $\xi_d = 0$ ), just bonds, but particularly good at issuing high risk loans.
- The only thing to add is a distinction between low and high risk loans.

## MODEL: AN EXTENSION SHADOW BANKING

- Brought to center stage by the troubles of Home Capital in Canada
- No deposits ( $\xi_d = 0$ ), just bonds, but particularly good at issuing high risk loans.
- The only thing to add is a distinction between low and high risk loans.
  - Because financial institutions specialize, this does not add state variables.

## MODEL: AN EXTENSION SHADOW BANKING

- Brought to center stage by the troubles of Home Capital in Canada
- No deposits ( $\xi_d = 0$ ), just bonds, but particularly good at issuing high risk loans.
- The only thing to add is a distinction between low and high risk loans.
  - Because financial institutions specialize, this does not add state variables.
  - Still need a theory of why are they trouble.