A Second Look at The U.S. Great Depression
From a Neoclassical Perspective*

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ABSTRACT

Can neoclassical theory account for the Great Depression in the United States—both the downturn in output between 1929 and 1933 and the recovery between 1934 and 1939? Yes and no. Given the large real and monetary shocks to the U.S. economy during 1929–33, neoclassical theory does predict a long, deep downturn. However, theory predicts a much different recovery from this downturn than actually occurred. Given the period’s sharp increases in total factor productivity and the money supply and the elimination of deflation and bank failures, theory predicts an extremely rapid recovery that returns output to trend around 1936. In sharp contrast, real output remained between 25 and 30 percent below trend through the late 1930s. We conclude that a new shock is needed to account for the Depression’s weak recovery. A likely culprit is New Deal policies toward monopoly and the distribution of income.

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1. Introduction

Between 1929 and 1933, employment fell about 25 percent and output fell about 30 percent in the United States. By 1939, employment and output remained well below their 1929 levels. Why did employment and output fall so much in the early 1930s? Why did they remain so low a decade after the contraction began?

This article addresses these two questions about the Great Depression using neoclassical growth theory. By neoclassical growth theory, we mean the theory in Cass 1965 and Koopmans 1965, augmented with certain shocks that cause employment and output to deviate from their deterministic growth paths as in Kydland and Prescott 1982. Traditionally, growth theory has not been used to study depressions, and in the past it probably would have been considered bizarre to use a market-clearing framework to analyze episodes that seemed to defy an equilibrium explanation. Our view is that growth theory can significantly advance our understanding of Depressions by systematically assessing which data are consistent with the theory and which observations are puzzling. We therefore analyze both the decline in U.S. economic activity (1929-33) and the recovery from the Depression (1934-39) using the same analytical framework. This analysis draws on our 1999 paper, and also includes discussions of subsequent analyses.

We focus our analysis on the shocks that could plausibly account for the large declines in output and employment between 1929-39. Since the Depression was much more severe and lasted so much longer than an ordinary business cycle, the shocks that caused the Depression must have differed significantly from the shocks that drive postwar business cycles. One possibility is that the shocks that caused the Depression were just much larger and more persistent versions of the same shocks that cause postwar fluctuations. An alternative
possibility is that the shocks that caused the Depression were fundamentally different than the shocks that cause postwar fluctuations.

We evaluate these two possibilities by testing whether the shocks that are considered important for understanding normal business cycle fluctuations - productivity shocks, fiscal policy shocks, monetary policy shocks, financial intermediation shocks, and trade shocks - quantitatively account for macroeconomic activity during the 1930s. Our two main findings are surprising. The first is that productivity shocks - even after correcting for possible input mismeasurement and compositional shifts - may account for over half of the 1929-33 downturn. The second finding is that none of the shocks we consider can plausibly account for the weak recovery. Growth theory robustly predicts that employment and output should have returned to their normal levels by the late 1930s, because most of the shocks we consider become large and positive after 1933. The weak recovery is a major puzzle from the perspective of neoclassical theory.

We then search for clues to this puzzle by examining deviations in the first order conditions of the model. Large deviations in these conditions shed light on the factors that prevented a full recovery by telling us what dimensions of the model are significantly at variance with the data. We conduct this deviation analysis by first parameterizing the model so that all the first order conditions in the model are satisfied in 1929, and then measuring the deviations in these conditions in 1939. This analysis shows that a labor market distortion that raised the real wage above its competitive level is a leading candidate explanation of the weak recovery. This is because the real wage is more than 20 percent above its normal level and also is more than 20 percent above the marginal product of labor, and is more than 100 percent above the household’s marginal rate of substitution (MRS) between consumption
and leisure.

An abnormally high real wage suggests a non-competitive explanation because normal competitive forces should have reduced the real wage and increased employment and consumption. We conclude our study by summarizing our recent work (Cole and Ohanian (2004)) that argues that President Roosevelt’s non-competitive policies that raised real wages and sanctioned monopoly account for about 60 percent of the weak recovery. Roosevelt’s National Industrial Recovery Act (NIRA) of 1933 allowed much of the economy to cartelize, provided that industry immediately raise wages and engage in collective bargaining with independent labor unions, and the National Labor Relations Act (NLRA) of 1935 significantly increased labor bargaining power. These policies fostered cartelization, high real wages, and the inability of households to equate their MRS with the real wage.

**The Data Through the Lens of the Theory**

We begin our study by using growth theory to examine some key macroeconomic variables during the 1930s. Neoclassical growth theory has two cornerstones: the aggregate production technology, which describes how labor and capital services are combined to create output, and the willingness and ability of households to substitute commodities over time, which govern how households allocate their time between market and nonmarket activities and how they allocate their income between consumption and savings. Viewed through the lens of this theory, the key variables are the allocation of output between consumption and investment, the allocation of time (labor input) between market and nonmarket activities, and the productivity of capital and labor.²

*Output*
Table 1 shows consumption, investment and the other components of real gross national product (GNP) for the 1929–39 period. Data are from the national income and product accounts published by the Bureau of Economic Analysis of the U.S. Department of Commerce. All data are divided by the working-age (16 years and older) population. Since the theory indicates that these variables can be expected to grow, on average, at the trend rate of technology, they are also detrended, that is, adjusted for trend growth. With these adjustments, the data can be directly compared to their peak values in 1929. Note that we do not follow the standard business cycle detrending procedure of Hodrick and Prescott (HP). This is because the standard parameterization of the HP procedure focuses on measuring much shorter fluctuations, such as post-World War II U.S. fluctuations, and consequently would treat much of the Great Depression as a change in the trend, rather than as a deviation from trend.

The table shows that all the components of real output (GNP in base-year prices), except government purchases of goods and services, fell considerably during the 1930s. The general pattern is a very large drop between 1929 and 1933 followed by only a small rise from the 1933 trough. Output fell more than 38 percent between 1929 and 1933. By 1939, output remained nearly 27 percent below its 1929 detrended level. This detrended decline of 27 percent consists of a raw 11 percent drop in per capita output and a further 16 percent drop representing trend growth that would have normally occurred over the 1929–39 period.

The largest decline occurred in business investment, which fell nearly 80 percent between 1929 and 1933. Consumer durables, which represent household, as opposed to business, investment, followed a similar pattern, declining more than 55 percent between 1929 and 1933. Consumption of nondurables and services declined almost 29 percent between 1929 and 1933.
Foreign trade (exports and imports) also fell considerably between 1929 and 1933. The impact of the decline between 1929 and 1933 on government purchases was relatively mild, and government spending even rose above its trend level in 1930 and 1931.

Table 1 also establishes that the economy did not recover much from the 1929–33 decline. In 1933, consumption of nondurables and services was about 28 percent below its 1929 detrended level, and remained about 25 percent below this level in 1939. Business investment remained 59 percent below its 1929 detrended level in 1939, and consumer durables remained 36 percent below their 1929 detrended level in 1939. The lack of recovery in consumption, combined with persistently low levels of investment, suggest the possibility that the economy was converging to a new, lower, steady state growth path. Consumption is a good barometer of a change in the economy’s steady state because household dynamic optimization implies that all future expectations of income should be factored into current consumption decisions.6 Figure 1 clearly shows the flat time profile of consumption after the Depression trough in 1933.

These unique and large changes in economic activity during the Depression also changed the composition of output—the shares of output devoted to consumption, investment, government purchases, and exports and imports. Table 2 shows these data. The share of output consumed rose considerably during the early 1930s, while the share of output invested, including consumer durables, declined sharply, falling from 25 percent in 1929 to just 8 percent in 1932. During the 1934–39 recovery, the share of output devoted to investment averaged about 15 percent, compared to its postwar average of 20 percent. This low rate of investment led to a decline in the capital stock—the gross stock of fixed reproducible private capital declined more than 6 percent between 1929 and 1939, representing a decline of more than 25 percent relative to trend. Foreign trade comprised a small share of economic activ-
ity in the United States during the 1929–39 period. Both exports and imports accounted for about 4 percent of output during the decade. The increase in government purchases, combined with the decrease in output, increased the government’s share of output from 13 percent to about 20 percent by 1939.

We now turn from final expenditure to productive inputs and the efficiency of production.

**Labor Input**

Data on labor input are presented in Table 3, which are taken from Kendrick (1961). We present five measures of labor input, each divided by the working-age population. We don’t detrend these ratios because theory implies that they will be constant along the steady-state growth path. Here, again, data are expressed relative to their 1929 values.

The three aggregate measures of labor input declined sharply from 1929 to 1933. *Total employment*, which consists of private and government workers, declined about 21 percent between 1929 and 1933 and remained 13 percent below its 1929 level in 1939. *Total hours*, which reflect changes in employment and changes in hours per worker, declined more sharply than total employment, and the trough didn’t occur until 1934. Total hours remained 21 percent below their 1929 level in 1939. *Private hours*, which don’t include the hours of government workers, declined more sharply than total hours, reflecting the fact that government employment did not fall during the 1930s. Private hours fell more than 25 percent between 1929 and 1939.

These large declines in aggregate labor input reflect different changes across sectors of the economy. *Farm hours* and *manufacturing hours* are shown in the last two columns of Table 3. In addition to being divided by the working-age population, the farm hours measure
is adjusted for an annual secular decline in farm employment of about 1.8 percent per year. In contrast to the other measures of labor input, farm hours remained near trend during much of the decade. Farm hours were virtually unchanged between 1929 and 1933, a period in which hours worked in other sectors fell sharply. Farm hours did fall about 10 percent in 1934 and were about 7 percent below their 1929 level by 1939. A very different picture emerges for manufacturing hours, which plummeted more than 40 percent between 1929 and 1933 and remained 29 percent below their detrended 1929 level at the end of the decade.

These data raise questions about differences between the farm and manufacturing sectors during the Depression. Why didn’t farm hours decline more during the Depression? Why did manufacturing hours decline so much? We will return to these questions later.

Finally, note that the changes in nonfarm labor are similar to changes in consumption during the 1930s. After falling sharply between 1929 and 1933, labor remained well below 1929 levels in 1939. These data also suggest that the economy was converging to a lower steady state growth path than the 1929 growth path.

Productivity

Table 4 shows three measures of productivity: labor productivity (output per hour) and total factor productivity (TFP) for both the private domestic economy and for the private non-farm economy. These data are also taken from Kendrick (1961). These measures are detrended and expressed relative to 1929 measures. All three series show similar changes during the 1930s. Labor productivity and both measures of TFP declined sharply in 1932 and 1933, falling about 12 percent, 13 percent, and 16 percent, respectively, below their 1929 detrended levels. After 1933, however, all three measures rose quickly relative to trend and, in fact,
returned to trend by 1936. When we compare 1939 data to 1929 data, we see that the 1930s were a decade of normal productivity growth. Labor productivity grew more than 22 percent between 1929 and 1939, and both measures of TFP grew more than 20 percent in the same period. These data also suggest that the economy should have returned to its original steady state growth path, rather than settling on a lower growth path.

An alternative interpretation of the weak recovery is that recoveries are naturally slow. Table 5 assesses whether there is empirical support for this alternative view by showing average detrended levels of output, consumption, and investment from postwar recoveries. The data are reported relative to the respective business cycle peak, and are measured from the trough. These data do not support this alternative view. A comparison of Tables 1 and 4 shows that the recovery from a typical postwar recession differs considerably from the 1934–39 recovery. First, output rapidly recovers to trend following a typical postwar recession. Second, consumption grows smoothly following a typical postwar recession. This contrasts to the flat time path of consumption during the 1934–39 recovery. Third, investment recovers to trend following a typical postwar recession. During the Depression, however, the recovery in investment was much slower, remaining well below the recovery in output.

These data show that the 1934–39 recovery was quantitatively and qualitatively different than the recovery from a typical postwar recession. This is also consistent with the view that the economy was not returning to its pre-1929 steady-state growth path, but was settling on a considerably lower steady-state growth path.

We now compare the U.S. Depression to depressions in other countries that occurred at the same time. This comparison also suggests that the U.S. should have recovered much more quickly than it actually did.
An International Comparison

How much of the U.S. Great Depression was caused by international shocks, rather than domestic shocks? We suspect that most of the depression was due to domestic shocks. Many countries suffered economic declines during the 1930s, but there are two important distinctions between the U.S. Depression and depressions in other countries during the 1930s. The decline in the United States was much more severe, and the recovery from the decline was much weaker. To see this, we examine average real per capita output relative to its 1929 level for Belgium, Britain, France, Germany, Italy, Japan, and Sweden. The data are from Maddison 1991 and are normalized for each country so that per capita output is equal to 100 in 1929. Since there is some debate over the long-run growth rate in some of these countries, we have not detrended the data.

Table 6 shows the U.S. data and the mean of the normalized data for other countries. The total drop in output is relatively small in other countries: an 8.8 percent drop compared to a 30 percent drop in the United States. The international economies recovered quickly: output in almost all the countries returned to 1929 levels by 1935 and was well above those levels by 1938. Employment also generally recovered to its 1929 level by 1938.8

We draw two conclusions from this comparison. First, the larger decline in the United States is consistent with the view that the shocks that caused the decline in the United States were larger than the shocks that caused the decline in the other countries. Second, the weak recovery in the United States is likely caused by a U.S. domestic shock, rather than an international shock.

The data shows that inputs and output in the United States fell considerably during the 1930s and did not recover much relative to the increase in productivity. Moreover, the
decline was much more severe and the recovery much weaker in the United States than in other countries. To account for the decade-long Depression in the United States, we conclude that we should focus on domestic, rather than international, factors. We turn to this task in the next section.

**The Role of Real Shocks**

We first analyze three classes of real shocks considered important for understanding business cycle fluctuations: productivity shocks, fiscal policy shocks, and trade shocks.

*Productivity Shocks? Perhaps Important for the downturn, but can’t explain the weak recovery*

First we consider productivity shocks, defined as any exogenous factor that changes the efficiency with which business enterprises transform inputs into output. Under this broad definition, changes in productivity reflect not only true changes in technology and knowledge, but also such other factors as changes in work rules and practices or government regulations that affect the efficiency of production but are exogenous from the perspective of business enterprises. The key element that leads to a decline in economic activity in models with productivity shocks is a negative shock that reduces the marginal products of capital and labor. These negative shocks lead households to substitute out of market activities into nonmarket activities and result in lower output. Recent research has identified these shocks as important factors in postwar business cycle fluctuations. Prescott (1986), for example, shows that a standard one-sector neoclassical model with a plausibly parameterized stochastic process for productivity shocks can account for 70 percent of postwar business cycle fluctuations. How much of the Great Depression can be accounted for by the negative productivity shocks of the early 1930s?
To address this question, we feed in the actual productivity shocks into a real business cycle model and compute the time path of output from that model. (See Hansen 1985, Prescott 1986, or King, Plosser, and Rebelo 1988 for a discussion of this model.) Our model consists of equations (A1)–(A5) and (A9) in the Appendix, along with the following:

(1) \[ u(c_t, l_t) = \log(c_t) + \phi \log(l_t). \]

We use the Cobb-Douglas production function specification:

(2) \[ z_t f(k_t, n_t) = z_t k_t^\theta (x_t n_t)^{1-\theta}. \]

The household has one unit of time available each period:

(3) \[ 1 = l_t + n_t. \]

And we use the following specification of the stochastic process for the technology shock:

(4) \[ z_t = (1 - \rho) + \rho z_{t-1} + \varepsilon_t, \varepsilon_t \sim N(0, \sigma^2). \]

With parameter values, we use numerical methods to compute an approximate solution to the equilibrium of this economy. We set \( \theta = 0.33 \) to conform to the observation that capital income is about one-third of output. We set \( \sigma = 1.7 \) percent and \( \rho = 0.95^4 \) to conform to the observed standard deviation and serial correlation of total factor productivity. We choose the value for the parameter \( \phi \) so that households spend about one-third of their discretionary time working in the deterministic steady state. Labor-augmenting technological change \( (x_t) \) grows at a rate of 1.9 percent per year. The population \( (n_t) \) grows at a rate of 1 percent per year. We set the depreciation rate at 6 percent per year.
We conduct the analysis by assuming that the capital stock in 1929 is equal to its steady-state value, and then we feed in the sequence of observed levels of total factor productivity as measures of the technology shock. Given the initial condition and the time path of technology, the model generates labor input, output, consumption, and investment for each year during the 1930s. Chart 2, compares the detrended level of output from the model to the actual detrended level of output. The measured decrease in productivity between 1929-33 generates a Depression in the model that is similar to the actual data - output in the model falls about 23 percent relative to trend in 1933, compared to the actual 38 percent decline.\(^\text{10}\) This similarity disappears after 1933. As a consequence of rapid productivity growth, output in the model is almost back to its trend level by 1936. In contrast, actual output remained 25-30 percent below trend during the recovery. These findings suggest that productivity, or a productivity-related factor, may have played a role during the decline phase of the Great Depression, but that it cannot account for the weak recovery.\(^\text{11}\)

A productivity explanation of the decline phase of the Great Depression is a very different way of thinking about this episode, and it is natural to ask whether these large negative productivity shocks are proxying for some other factor. One possibility is that these shocks are the consequence of capital and labor input mismeasurement, because total factor productivity change is defined residually as the percentage change in output minus a weighted average of the percentage change in inputs. Ohanian (2001) analyzed the quantitative implications of input mismeasurement and other possible factors affecting productivity measurement during the early 1930s, and found that these factors did not reverse the conclusion that there were big negative productivity shocks in the early 1930s. He corrected the productivity measure for changes in capital utilization, changes in the average quality of
workers, changes in the composition of production across sectors, and increasing returns to scale. He found that these factors can account for only about one-third of the measured decrease in productivity. The fact that a big productivity shock remains after these corrections suggests that some efficiency-related factor may have played a quantitatively significant role during the decline phase of the U.S. Great Depression.

We will focus the remainder of the paper around two questions. Can any of the other factors that we assess shed light on the large, negative productivity shocks between 1929-33? Can they account for the puzzling weak recovery?


We now consider fiscal policy shocks—changes in government purchases or tax rates. Christiano and Eichenbaum (1992) argue that government purchase shocks are important in understanding postwar business cycle fluctuations, and Braun (1994) and McGrattan (1994) argue that shocks to distorting taxes have had significant effects on postwar cyclical activity.

Fluctuations in government spending can affect economic activity through income and substitution effects. A decrease in government spending will tend to increase private consumption and, consequently, lower the marginal rate of substitution between consumption and leisure, which will lead households to work less and take more leisure. Conversely, an increase in government purchases will tend to decrease private consumption and reduce the marginal rate of substitution between consumption and leisure. In this case, theory predicts that this will lead households to work more and take less leisure.

Historically, changes in government purchases have had large effects on economic activity. Ohanian (1997) shows that the increase in government purchases during World War
II can account for much of the 60 percent increase in output during the 1940s. Can changes in government purchases also account for the decrease in output in the 1930s?

If government purchase shocks were a key factor in the decline in employment and output in the 1930s, government purchases should have declined considerably during the period. This did not occur. Government purchases declined modestly between 1929 and 1933 and then rose sharply during the rest of the decade, rising about 12 percent above trend by 1939. These data are inconsistent with the view that government purchase shocks were a key factor in either the downturn or the weak recovery.

Although changes in government purchases are not important in accounting for the Depression, the way they were financed may be. Government purchases are largely financed by distorting taxes—taxes that affect the marginal conditions of households or firms. Most government revenue is raised by taxing factor incomes. Changes in factor income taxes change the net rental price of the factor. Increases in labor and capital income taxes reduce the returns to these factors and, thus, can lead households to substitute out of taxed activities by working and saving less.

If changes in factor income taxes were a key factor in the 1930s economy, these rates should have increased considerably in the 1930s. Tax rates on both labor and capital changed very little during 1929–33, which implies that they were not important for the decline. However, these rates rose during the rest of the decade. Joines (1981) calculates that between 1929 and 1939 the average marginal tax rate on labor income increased from 3.5 percent to 8.3 percent and the average marginal tax rate on capital income increased from 29.5 percent to 42.5 percent. How much should these increases have depressed economic activity? To answer this question, we use deterministic version of the model we used earlier to analyze the
importance of technology shocks, and augment this model to allow for distortionary taxes on labor and capital income. We then compare the deterministic steady state of the model with 1939 tax rates to the deterministic steady state of the model with 1929 tax rates. With these differences in tax rates, we find that steady-state labor input falls by 4 percent. This suggests that higher taxes played a relatively minor role, accounting for less than 20 percent of the weak recovery.

Finally, neither government spending changes nor tax rate changes shed any light on the 1929-33 productivity decrease. This is because these fiscal changes are small during this period, and because there is no theoretical presumption that changes in government spending or tax rates change production efficiency.

Trade Shocks? No

Finally, we consider trade shocks. In the late 1920s and early 1930s, tariffs—domestic taxes on foreign goods—rose in the United States and in other countries. Tariffs raise the domestic price of foreign goods and, consequently, benefit domestic producers of goods that are substitutes with the taxed foreign goods. Higher tariffs almost certainly contributed the 65 percent decline in world trade that occurred between 1929-32. But how much did higher tariffs contribute to the decline in income and employment in the United States?

Probably very little, because trade was a very small fraction of U.S. output during that time. Imports and exports were both equal to about five percent of GNP, which led Lucas (1994) to conjecture that the quantitative effects of the world trade contraction during the 1930s are likely to have been “trivial.”12 Crucini and Kahn (1996) quantified this factor in a model that plausibly maximized the impact of the trade shock on output. They modeled
imports primarily as intermediate inputs, rather than as final goods, and they assumed an
elasticity of substitution between imported inputs and domestic inputs of 2/3, which is below
standard estimates between 1 and 2 (see Stern, Francis, and Schumacher 1976.) Both of
these modeling choices increase the impact of a trade disruption on output. Crucini and
Kahn estimate that the tariff increases reduced output by only two percent between 1929-33.
Moreover, the importance of the trade factor likely declined over time as domestic producers
increased production of previously imported inputs. We conclude that tariffs were not an
important factor for either the decline phase or the weak recovery. We also conclude that the
trade factor was too small to shed light on the 1929-33 productivity decline.

The Role of Monetary Shocks

Monetary shocks—unexpected changes in the stock of money—are considered an alternative
and/or complementary factor to real shocks for understanding business cycles, and many
economists argue that monetary shocks were a key factor in the 1929–33 decline. Much of
the attraction to monetary shocks as a source of business cycles comes from the influential
narrative monetary history of the United States by Friedman and Schwartz (1963), who
present evidence that declines in the money supply tend to precede declines in nominal
income. They also show that some measures of the money supply fell sharply during the
1929–33 decline. Friedman and Schwartz (1963, pp. 300–301) conclude from these data that
the money supply decline was an important cause of the 1929–33 decline (contraction):

The contraction is in fact a tragic testimonial to the importance of monetary forces

. . . . Prevention or moderation of the decline in the stock of money, let alone the
substitution of monetary expansion, would have reduced the contraction’s severity
and almost as certainly its duration.
Perhaps Important for the Decline, But not for the Recovery . . .

We begin by presenting data on money, prices, and interest rates. Table 7 shows these data. There are two measures of money: the monetary base (currency and reserves), which is the monetary aggregate controlled by the Federal Reserve, and M₁, which is currency plus checkable deposits, and two interest rates: the average annual rate on three-month U.S. Treasury bills and the average annual rate on commercial paper. The money supply data are expressed in per capita terms by dividing by the working-age population, and are also expressed relative to their 1929 values.

These money supply data can be used to estimate the monetary shock. Estimating the shock requires choosing a monetary aggregate, then identifying the exogenous component of that aggregate, and then measuring the innovation to the exogenous component. The size of the monetary shock depends on the specific monetary aggregate, as M₁ falls 35 percent between 1929-33, while the monetary base grows during this period. We therefore report measures of the shock using both of these aggregates.

Table 8 shows estimates of the monetary shock using M₁ and the base. The shock is the residual from an autoregressive forecasting model for the first difference of the log of each of the aggregates. The statistical model includes a constant and two lags.¹³ A caveat about the estimated M₁ shocks is that this M₁ has a large endogenous component (demand deposits) that is positively correlated with the level of general economic activity. Since our statistical model does not account for this endogenous component, estimating the shock using M₁ will generate a shock that will tend to be too large in absolute value.

It is unlikely that monetary shocks kept the economy depressed after 1933. Most of the M₁ shocks are positive after 1933, and all the monetary base shocks are positive after this
date. These post-1933 positive monetary shocks are the key reason why Lucas and Rapping (1972) found the weak recovery so puzzling. Their monetary business cycle model predicts that the economy should have fully recovered by 1936, rather than remaining 30 percent below trend. We agree with Lucas and Rapping that monetary shocks don’t plausibly account for the weak recovery, and we focus instead on the role of monetary shocks for the downturn phase of the Depression. Between 1929-33, the alternative measures of the monetary shock are quite different. The monetary base shock is significantly negative only in 1930, and afterwards is close to zero. In contrast, there are large negative M1 shocks during the downturn phase. As discussed above, however, the significant endogenous component in M1 raises questions about the size of this shock. In particular, these large negative shocks partially reflect the endogenous response of M1 to the decline in economic activity.

If monetary shocks were a key factor, understanding the impact of monetary shocks during the downturn requires specifying a channel of monetary nonneutrality. Imperfectly flexible wages is perhaps the most highly cited source of nonneutrality for the Depression (see Eichengreen and Sachs, Bernanke and Carey, Bordo, Erceg, and Evans). We have analyzed the sticky wage hypothesis for 1929-33 in the US, and found that this factor contributed to the Great Depression, but was not a major factor. This is because real wages were not particularly high, because this factor cannot account for the large negative productivity shocks observed during this period, and because there is no theory for understanding why wage stickiness would be so important after 1930. We summarize each of these in turn, and conclude that if monetary shocks were important, their main effect came through some other channel.

Regarding real wages, Cole and Ohanian (2001) focused on manufacturing wages because these data are relatively high quality, and because President Hoover intervened in this
sector to prevent nominal wage cuts. In particular, President Hoover jawboned the leaders of major manufacturing firms at a White House meeting in late 1929 to keep nominal wages fixed. Despite Hoover’s intervention, which did have an impact on nominal wages very early in the Depression, the average manufacturing wage divided by the GNP deflator was only about 5 percent above trend, on average, between 1930-33. (Table 10 presents these data between 1930-39). However, even this relatively small increase is biased upwards because the average quality of employees rose during the Depression, as firms concentrated employment among the most experienced and productive workers. Firm-level evidence shows that this type of compositional change in employees generates quantitatively important upward bias in aggregate wage measures. For example, Westinghouse and General Electric, which comprised about 90 percent of the electrical equipment industry, cut wages by 10 percent in between 1929 and 1931, laid off the least productive workers, and assigned the longest workweeks to the most productive workers. Despite these nominal wage cuts, this large compositional change in employees resulted in the average industry wage remaining unchanged during this period. Cole and Ohanian (2001) estimated the size of this compositional bias for aggregate wages and found that aggregate measured wages may be overstated by 15-18 percent at the trough of the Depression. Correcting the aggregate real wage for this bias implies that real wages were below normal, not above normal.

Another drawback to the sticky wage explanation is that its implication for labor productivity is strongly at variance with U.S. labor productivity. This is because contractionary money shocks raise labor productivity in this model, as firms move up their labor demand curves to equate the higher real wage to the higher marginal product of labor. In contrast, actual labor productivity fell 15 percent between 1930-33. This large discrepancy in labor
productivity raises questions about the sticky wage explanation.\textsuperscript{14}

A third drawback to the sticky wage explanation is that there is no theoretical framework for plausibly rationalizing persistently sticky nominal wages during the Depression. The usual factors that are cited for justifying sticky nominal wages were relatively unimportant during this period; there were no long-term nominal wage contracts, and very few workers were members of independent labor unions. Given such limited union representation, it is hard to realistically justify how workers could have commanded such high wages during a period of negative profits, record business failures, and high unemployment. Monetary shocks remain a possibly important factor for 1929-33, but the evidence presented suggests that sticky wages are probably not the main channel.

\textit{Were Financial Intermediation Shocks Quantitatively Important?}

\textit{An Open Question for the Downturn.}

Banking is considered an important candidate shock because suspensions and failures of banks rose during the downturn. Establishing a significant role for banking in a quantitative, equilibrium model remains a challenging task, as we review recent work that indicates simple theories of intermediation show that banking shocks were a minor factor, and that there are several observations that are significantly at variance with banking as a major driving force of the Depression.

Several economists argue that the bank failures and temporary bank closings that occurred between 1930 and 1933 contributed to the severity of the decline phase of the Great Depression. Bernanke (1983) provides empirical support for this argument. He constructs a statistical model, based on Lucas and Rapping’s (1969) model, in which unexpected changes
in the money stock lead to changes in output. Bernanke shows that adding the dollar value of deposits and liabilities of failing and temporarily closed banks as explanatory variables significantly increases the fraction of output variation accounted for by the model. Bernanke and others suggest that these failures reduced the efficiency of intermediation by destroying local information capital that was specific to individual borrower-lender relationships.

Table 9 shows deposits as a fraction of nominal output that were in banks that either failed or temporarily suspended operations during the 1930s. On average, these deposits were about 2.5 percent of output between 1930-33. The absence of failures/suspensions after the adoption of federal deposit insurance in 1933 indicates that this was not a major factor for the weak recovery.

Assessing the quantitative contribution of bank failures and suspensions requires a model that can address two questions: How big was the banking shock during 1930-33? How much did this shock reduce output in these years?

Cole and Ohanian 2001 developed a simple model that captures the view that failures and suspensions destroyed information capital. They modelled banking output as an intermediate input into the production of a single final good, and they assumed that banking output was produced from a constant returns to scale, Cobb-Douglas technology using bank deposits and information capital. In their model, there are a number of bank locations, and information capital is endowed to a specific location. They assume that new information capital cannot be created. This implies that deposits will be allocated across bank locations to equalize their marginal product. Aggregate banking output is then the sum of the outputs at all the bank locations. To maximize the impact of a banking shock, they assume that all of a bank’s information capital is lost if the bank fails or if it temporarily suspended operations.
Their model implies that the fraction of information capital destroyed - and the fraction of banking output destroyed during the depression due to this factor - is equal to the cumulative fraction of deposits in failed or suspended banks between 1930-33. These cumulative figures for the four years are 1.7 percent, 6.0 percent, 8.0 percent, and 19.0 percent.  

How much did this reduction in banking output reduce GNP? Cole and Ohanian estimate this using a simple growth accounting analysis. With perfect competition, a first order expansion of the production function implies that the percentage change in aggregate output, \( \hat{y} \), is equal to the percentage change in the intermediate inputs \( (\hat{y}_i) \), multiplied by their value added shares \( (\gamma_i) \). This first order approximation is not specific to their environment, but rather holds in any model with perfect competition and a constant returns to scale technology:

\[
(5) \quad \hat{y} = \sum_{i=1}^{n} \gamma_i \hat{y}_i.
\]

The percentage of value added from the banking sector just prior to the Depression was about 1.5 percent. This implies that bank failures/suspensions reduced GNP by considerably less than one percent per year for each year.

This analysis indicates that bank failures and suspensions were not a major driving factor through the simple neoclassical channel of banking as an input to final goods production. An alternative possibility is that bank failures and suspensions were a major factor, but that this simple model does not have the mechanism that generates this effect. We now consider some possible factors that could increase the impact of failures/suspensions, but that are missing from the model. One possibility is that the first order approximation is inaccurate, because of very limited substitutability across the intermediate inputs. If this was
true, then banking’s value added share of value added should have increased substantially during the Great Depression. This did not happen. It’s value added share remained around 1 percent in 1933.

Another possibility is that an externality could have magnified this effect. Cole and Ohanian extended their local information capital analysis to pursue this story by assuming that the quantity of information capital was a productive externality at the state level. Specifically, the output of a state is given by:

\[ Y_{it} = Z_{it}^b F(K_{it}, L_{it}, ...) \]

where \( Z_{it} \) is banking information capital in state “i” at date t.

If banking was a key factor, then the states with the biggest fractions of deposits at suspended/failed banks should have had the biggest depressions. This did not happen. Figure 3 shows a scatterplot between the change in personal income between 1929-32 and the fraction of deposits in suspended/failed banks for each of the 48 states. There is no systematic relationship between these variables in the cross-section; the correlation between suspended/failed deposits and personal income is only -.13. The correlation between suspended/failed deposits and state-level manufacturing employment, which is an alternative measure of statewide economic activity, is also low (.12).

Cole and Ohanian (2001) also examined broader implications of shocks to financial intermediation by analyzing changes in the overall quantity of bank deposits and loans, changes in interest rate spreads, and changes in retained earnings. These data also raise questions about banking as a major depressing factor. We summarize each of these analyses in turn.

An alternative banking view of the Depression is that total banking services were in
scarce supply not just because of failures and suspensions, but also because of exogenous
deposit withdrawal at all banks. If exogenous withdrawals of deposits were a major factor,
then the deposit/output ratio should have decreased during the depression, reflecting the
relative scarcity of deposits. This did not happen - this ratio rose from 0.59 in 1929 to 0.78 in
1932. Commercial and industrial loan data also supports the view that banking services were
not in relatively scarce supply during the Depression. Loans fell less than output between
1930-32, and the stock of loans relative to GNP rose from 0.40 to 0.47 between 1929 and 1932.
Additional evidence that banking capacity was not scarce is the behavior of bank holdings
of federal securities. Banks holdings of federal securities rose from five percent of output in
1929 to 14 percent of output in 1933, and rose further to 21 percent in 1939. These data
suggest banking capacity was not in relatively scarce supply in the 1930s.

Another possibility is that shocks to intermediation exogenously raised the spread
between borrowing and lending rates, which contributed to the Depression by reducing bor-
rowing. Assessing this view requires correcting the borrowing-lending spread for endogenous
changes in default premia, which likely rose during the Depression. Cole and Ohanian (2001)
addressed this issue by measuring the spread between borrowing and lending rates for securi-
ties with different default risk. The key implication of the theory is that if exogenously higher
borrowing-lending spreads were a key factor driving the Depression, then we should observe
large increases in the spread, irrespective of the quality of the security, and these increases
should be much larger than those observed during post-World War II recessions.

This did not occur. First, the spread between borrowing rates and lending rates for
high quality borrowers changed very little during the Depression; the spread between the Aaa
rate and the government bond rate (which they used as a proxy for the lending rate) rose
from 113 basis points in 1929 to an average of 125 basis points between 1930-33. Second, the increase in the spread for high default securities did not rise as much as it does during post-World War II recessions. The spread on Baa securities rose 194 basis points, increasing from 230 basis points in 1929 to an average of 424 basis points between 1930-33. This 194 basis point increase is smaller than the average increase in this spread of over 200 basis points that occurs during post-World War II recessions. Moreover, since the Depression was a period in which default probabilities were much higher than average, correcting the Depression spreads for this factor may generate a spread that is significantly lower than that during typical recessions.

The fact that spreads between risk-free and high quality securities changed very little during the Depression, and the fact that on average, the increase in the spread between risk-free and low quality securities during the Depression was smaller than during typical recessions, raise questions about the role of interest rate spreads as a major driving force behind the Depression.

Cole and Ohanian also examined how other variables should have changed if banking shocks were a major contributing factor, including the behavior of retained earnings, which are a very good substitute for intermediated funds. If banking shocks were a major driving factor behind the Depression, then firms should have increased their stock of retained earnings to substitute out of external finance to internal finance, and to provide a buffer stock of cash. This did not happen. Figure 4 shows that retained earnings fell substantially during the Depression. They fell 50 percent in 1930, and were negative between 1931-33. Negative retained earnings means that firms were reducing their buffer cash reserves. If cash was so precious during the Depression because of negative banking shocks, why were firms
eliminating their cash reserves?

These observations highlight some of the challenges facing banking-driven theories of the Depression. If banking was a key driving factor, then quantitatively assessing this factor requires a theoretical framework that can successfully account for the facts that there is no systematic relationship between the severity of that the banking crisis and the level of the depression in the cross-section of the U.S., that the increase in borrowing/lending spreads during the Depression is no greater than the average increases observed in mild recessions, that the deposit/output ratio and loan/output ratio both rise during the Depression, and that corporate cash reserves fell significantly. We are unaware of any models that are consistent with these observations. Developing models that can confront these data is an important first step in the process of quantifying the contribution of banking shocks to the Depression, and should be pursued in future research.

□ Probably not much during the Recovery.

We now consider whether intermediation shocks were an important factor behind the weak recovery. The introduction of federal deposit insurance largely eliminated banking panics after 1933. The leading intermediation shock for the recovery period in the literature is higher reserve requirements. In August 1936, the Federal Reserve increased the required fraction of net deposits that member banks must hold as reserves from 10 percent to 15 percent. This fraction rose to 17.5 percent in March 1937 and then rose to 20 percent in May 1937. Some economists, including Friedman and Schwartz, argue that this factor contributed to weak macroeconomic performance during 1937 and 1938.

These economists argue that these policy changes increased bank reserves, which reduced lending and, consequently, reduced output. If this were true, we would expect to see
output fall shortly after these changes. This did not happen. Between August 1936, when
the first increase took place, and August 1937, industrial production rose about 12 percent.
Industrial production did begin falling until October 1937, which is 14 months after the first
and largest increase in reserve requirements. (Industrial production data are from the Oc-
tober 1943 Federal Reserve Index of Industrial Production of the Board of Governors of the
Federal Reserve System.)

Another shortcoming of the reserve requirement view is that interest rates did not rise
after these policy changes. Commercial loan rates fell from 2.74 percent in January 1936 to
2.65 percent in August 1936. These rates then fell to 2.57 percent in March 1937 and rose
slightly to 2.64 percent in May 1937, the date of the last increase in reserve requirements.
Lending rates then ranged between 2.48 percent and 2.60 percent over the rest of 1937 and
through 1938. Interest rates on other securities showed similar patterns: rates on Aaa-, Aa-,
and A-rated corporate debt were roughly unchanged between 1936 and 1938.17 (Interest rate
data are from Banking and Monetary Statistics, 1914–1941 of the Board of Governors of
the Federal Reserve System.) These data raise questions about the view that higher reserve
requirements had important macroeconomic effects in the late 1930s.

Diagnosing the Weak Recovery - A Big distortion in the Labor Market

Neoclassical theory indicates that the weak recovery from the Depression is a puzzle. We
now use the theory to help identify candidate factors that kept the economy depressed after
in the first order conditions can be used to diagnose depressions.18

Table 11 shows the four standard efficiency conditions for the competitive decentral-
ization of our model with log utility over consumption and leisure. There are two equations for the household and two equations for a representative firm.

Table 11 - The Efficiency Conditions in the Growth Model

<table>
<thead>
<tr>
<th></th>
<th>Household</th>
<th>Firm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Labor</td>
<td>$\psi / (1 - n_t) = w_t / c_t$</td>
<td>$w_t = f_{nt}$</td>
</tr>
<tr>
<td>Capital</td>
<td>$1 / c_t = \beta (r_t + 1 - \delta) / c_{t+1}$</td>
<td>$r_t = f_{kt}$</td>
</tr>
</tbody>
</table>

In the table, $w$ denotes the wage rate, $r$ denotes the rental rate on capital, and $f_{nt}$ and $f_{kt}$ are the partial derivatives of the technology with respect to labor and capital. We refer to these conditions using $i = H, F$ for the household and the firm, and $j = L, K$ for labor and capital.

If the conditions hold, then the ratio of the left-hand side of the conditions to the right-hand side of the conditions is equal to 1. We therefore form the ratio between the left and right-hand sides of each of these equations, which we denote as $\phi_{ijt}$, and we parameterize the model for each country so that these conditions equal 1 prior to the depression. We then measure these ratios during the Depression relative to their normal values.

These deviations provide clues to the factors that might account for these long depressions. For example, a household labor deviation suggests either that households could not satisfying this condition (e.g. an above-market wage that restricts trade in labor services) or that there is a difference between the wage and the actual return to work (e.g. taxes or subsidies). Similar reasoning applies to interpreting deviations in the household capital condition. Deviations in the firm labor and capital conditions suggests that these factors are
not being compensated according to their marginal products, which could reflect changes in rent-sharing and the distribution of income. While this discussion is not exhaustive, it does show how these deviations identify possible suspects for an initial investigation.

Table 12 shows the efficiency condition deviations for the U.S. in 1939 relative to 1929. The data show that 3 of the 4 conditions are distorted. The marginal rate of substitution between consumption and leisure (MRS) is 41 percent below the wage rate, and factor prices differ considerably from their implied marginal products. The wage rate substantially exceeds the marginal product of labor, and the return to capital is below the marginal product of capital. There is no deviation in the household’s Euler equation, however.

Table 12 - Distortions in the U.S. Efficiency Conditions: 1939 vs. 1929

<table>
<thead>
<tr>
<th>Household-Labor</th>
<th>Household-Capital</th>
<th>Firm-Labor</th>
<th>Firm-Capital</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.59</td>
<td>1.00</td>
<td>0.79</td>
<td>1.26</td>
</tr>
</tbody>
</table>

We now document how much of these deviations are accounted for by changes in quantities and how much are accounted for by changes in factor prices. Table 13 therefore shows the wage rate divided by productivity in 1939, relative to this same ratio in 1929 and shows the difference in the real return to capital (in percentage points) between 1939 and 1929.

Table 13 - Relative U.S. Factor Prices: 1939 vs. 1929

<table>
<thead>
<tr>
<th>Real Wage/TFP</th>
<th>Real Return to Capital</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.25</td>
<td>0.1%</td>
</tr>
</tbody>
</table>
The table shows that the wage rate is 25 percent above its value implied by productivity growth, but that the return to capital is very close to its 1929 level. A high real wage during a period of Depression is a puzzle. Why weren’t more people working, given the high real wage? Why was the real wage so high, given low consumption and labor? This suggests that some factor prevented normal competitive forces from equating the supply of labor to the demand for labor. Instead, these data indicate that some factor raised the wage above its market clearing level, and that this high wage prevented households from satisfying their MRS condition.

A Resolution of the Weak Recovery

Cole and Ohanian (2004) argued that government labor and industrial policies are a key factor contributing to the weak recovery. Government policies toward monopoly changed considerably in the 1930s. In particular, the National Industrial Recovery Act of 1933 allowed much of the U.S. economy to cartelize. For over 500 sectors, including manufacturing, antitrust law was suspended and incumbent business leaders, in conjunction with government and labor representatives in each sector, drew up codes of fair competition. Many of these codes provided for minimum prices, output quotas, and open price systems in which all firms had to report current prices to the code authority and any price cut had to be filed in advance with the authority, who then notified other producers. Firms that attempted to cut prices were pressured by other industry members and publicly berated by the head of the NIRA as “cut-throat chiselers.” In return for government-sanctioned collusion, firms gave incumbent workers large pay increases and agreed to engage in collective bargaining with independent unions.
Cole and Ohanian (2004) present evidence that shows these policies increased relative prices and real wages by 25 percent or more in sectors that were effectively cartelized, and that the policies accounted for about 60 percent of the weak recovery in a conservatively parameterized model.

**Conclusion and Directions for Future Research**

There are a number of fascinating questions and challenges about the Great Depression. One is developing models of negative productivity shocks for 1929-33. There were large decreases in TFP and labor productivity that don’t seem to be fully accounted for by the “usual suspects” of capacity utilization and increasing returns. Clearly, an exogenous, productivity shock explanation of the Depression is unsatisfactory, as it simply pushes the question of “What caused the Depression?” one step back. Thus, developing and testing models that can explain why productivity fell so much may advance our understanding of 1929-33, and may also have broader implications for understanding procyclical productivity during normal business cycle fluctuations. Another is developing alternative monetary models to the sticky wage model, either as a model for why productivity fell, or as a complementary factor to productivity. A third avenue is developing financial intermediation models that are consistent with the depression observations of no systematic relationship between the severity of the depression and the severity of the banking crisis in the cross section, higher deposit/output and loan/output ratios, relatively small increases in borrowing/lending spreads, and large reductions in retained earnings.

Regarding the weak recovery, a remaining important puzzle is why the marginal product of capital was so much higher than the return to capital in the late 1930s. In Cole and
Ohanian’s model, capital is rented by firms on a competitive market and the real return is thus equated to the marginal product. We suspect that this large gap between the marginal product and the real return may be due to labor holding up sunk capital. This is because the late 1930s were the heyday of labor bargaining power, as The National Labor Relations Act of 1935 allowed workers to take a variety of actions against firms, including using the “sit-down” strike, in which workers forcibly occupied factories and prevented production. These strikes were effective in a number of major industries, including the auto and steel industries. Our current research is developing a dynamic equilibrium hold-up model along these lines.
Notes

For other studies of the Depression and many additional references, see Bernanke 1995 Brunner 1981; Temin 1989, 1993; Eichengreen 1992; Calomiris 1993; Margo 1993; Romer 1993; Bernanke 1995; Bordo, Erceg, and Evans 1996; and Crucini and Kahn 1996.

Note that in the closed economy framework of the neoclassical growth model, savings equals investment.

We end our analysis in 1939 to avoid the effects of World War II.

We make the trend adjustment by dividing each variable by its long-run trend growth rate relative to the reference date. For example, we divide GNP in 1930 by 1.019. This number is 1 plus the average growth rate of 1.9 percent over the 1947–97 period and over the 1919–29 period. For 1931, we divide the variable by 1.019², and so forth.

To obtain this measure, we divide per capita output in 1939 by per capita output in 1929 (0.89) and divide the result by 1.019¹⁰.

This point is first stressed in Hall 1978.

Hours will be constant along the steady-state growth path if preferences and technology satisfy certain properties. See King, Plosser, and Rebelo 1988.

The average ratio of employment in 1939 to employment in 1929 was one in these countries, indicating that employment had recovered.

We used Marcet’s parameterized expectations procedure.

Our earlier paper (Cole and Ohanian, 1999) conducted a similar exercise and reported that productivity shocks reduced output by about 15 percent. This was a typographical error.

Some economists have argued that capital’s share of output is larger than 1/3, based
on unmeasured capital such as organizational capital and human capital. We also conducted the analysis using a model with a 2/3 capital share. The predicted recovery was also much faster in this model, with output recovering to 95 percent of trend by 1939.

To understand why a trade disruption would have such a small effect on output in a country with a small trade share, consider the following example. Assume that final goods are produced with both domestic \((Z)\) and foreign \((M)\) intermediate goods and that the prices of all goods are normalized to one. Assuming an elasticity of substitution between home and foreign goods of one implies that the production for final goods, \(Y\), is Cobb-Douglas, or

\[
Y = Z^\alpha M^{1-\alpha}
\]

where \(\alpha\) is the share parameter for intermediate inputs. This assumption implies that with the level of domestic intermediate goods held fixed,

\[
\%\Delta Y = (1 - \alpha)\%\Delta M.
\]

The fact that U.S. imports were 4 percent of total output and U.S. exports 5 percent in 1929 suggests that the highest the cost share of inputs in production could have been is \(0.04/0.95 \approx 0.04\). Hence, an extreme disruption in trade that led to an 80 percent drop in imports would lead to only a 3.2 percent drop in output. (See Crucini and Kahn 1996 for more on this issue.)

We experimented with a variety of models, and found the results to be robust to plausible variations in the model.

Note that the sticky wage model, augmented with variable capacity utilization, cannot account for lower labor productivity. This model generates higher labor productivity in response to unexpected deflation.
The data do not distinguish between banks that failed, and banks that temporarily suspended operations.

Note that this measure of suspended deposits (as a fraction of total deposits) differs from that in Table 9.

Interest rates on Baa debt, which is considered by investment bankers to have higher default risk than these other debts, did begin to rise in late 1937 and 1938.

A number of other economists have also used subsets of the conditions we examine, including Parkin (1984), Hall (1986), Ingram, Kocherlakota, and Savin (1997), and Mulligan (2000) for analyses of the household’s static first order condition that equates the marginal rate of substitution between consumption and leisure to the wage.

The data are taken from Cole and Ohanian (1999). The wage is the manufacturing wage from Hanes (1996), divided by the GNP deflator. The capital stock is real equipment and structures for the corporate sector. Hours worked is from Kendrick (1961). The gross return to capital is corporate profits relative to the corporate capital stock, deflated by the GNP deflator. We use a five percent depreciation rate, which is the historical rate for the corporate capital stock during this period.
Appendix

The Neoclassical Growth Model

Here we describe the neoclassical growth model, which provides the theoretical framework in the preceding paper.

The neoclassical growth model has become the workhorse of macroeconomics, public finance, and international economics. The widespread use of this model in aggregate economics reflects its simplicity and the fact that its long-run predictions for output, consumption, investment, and shares of income paid to capital and labor conform closely to the long-run experience of the United States and other developed countries.

The model includes two constructs. One is a production function with constant returns to scale and smooth substitution possibilities between capital and labor inputs. Output is either consumed or saved to augment the capital stock. The other construct is a representative household which chooses a sequence of consumption, savings, and leisure to maximize the present discounted value of utility.\textsuperscript{20}

The basic version of the model can be written as maximizing the lifetime utility of a representative household which is endowed initially with $k_0$ units of capital and one unit of time at each date. Time can be used for work to produce goods ($n_t$) or for leisure ($l_t$). The objective function is maximized subject to a sequence of constraints that require sufficient output $[f(k_t, n_t)]$ to finance the sum of consumption ($c_t$) and investment ($i_t$) at each date. Each unit of date $t$ output that is invested augments the date $t + 1$ capital stock by one unit. The capital stock depreciates geometrically at rate $\delta$, and $\beta$ is the household’s discount

37
factor. Formally, the maximization problem is

\[ \max_{\{c_t, l_t\}} \sum_{t=0}^{\infty} \beta^t u(c_t, l_t) \]

subject to the following conditions:

\[ f(k_t, n_t) \geq c_t + i_t \]

\[ i_t = k_{t+1} - (1 - \delta)k_t \]

\[ 1 = n_t + l_t \]

\[ c_t \geq 0, n_t \geq 0, k_{t+1} \geq 0. \]

Under standard conditions, an interior optimum exists for this problem. (See Stokey, Lucas, and Prescott 1989.) The optimal quantities satisfy the following two first-order conditions at each date:

\[ u_t = u_{c_t} f_2(k_t, n_t) \]

\[ u_{c_t} = \beta u_{c_{t+1}} [f_1(k_{t+1}, n_{t+1}) + (1 - \delta)]. \]

Equation (A6) characterizes the trade-off between taking leisure and working by equating the marginal utility of leisure, \( u_{l_t} \), to the marginal benefit of working, which is working one additional unit and consuming the proceeds: \( u_{c_t} f_2(k_t, n_t) \). Equation (A7) characterizes the trade-off between consuming one additional unit today and investing that unit and consuming the proceeds tomorrow. This trade-off involves equating the marginal utility of consumption today, \( u_{c_t} \), to the discounted marginal utility of consumption tomorrow and multiplying by the marginal product of capital tomorrow. This version of the model has a steady state in
which all variables converge to constants. To introduce steady-state growth into this model, the production technology is modified to include labor-augmenting technological change, $x_t$:

$$x_{t+1} = (1 + \gamma)x_t$$

(A8)

where the variable $x_t$ represents the efficiency of labor input, which is assumed to grow at the constant rate $\gamma$ over time. The production function is modified to be $f(k_t, x_t n_t)$. King, Plosser, and Rebelo (1988) show that relative to trend growth, this version of the model has a steady state and has the same characteristics as the model without growth.

This very simple framework, featuring intertemporal optimization, capital accumulation, and an aggregate production function, is the foundation of many modern business cycle models. For example, models with technology shocks start with this framework and add a stochastic disturbance to the production technology. In this case, the resource constraint becomes

$$z_t f(k_t, n_t) \geq c_t + i_t$$

(A9)

where $z_t$ is a random variable that shifts the production function. Fluctuations in the technology shock affect the marginal products of capital and labor and, consequently, lead to fluctuations in allocations and relative prices. (See Prescott 1986 for details.)

Models with government spending shocks start with the basic framework and add stochastic government purchases. In this case, the resource constraint is modified as follows:

$$f(k_t, n_t) \geq c_t + i_t + g_t$$

(A10)

where $g_t$ is stochastic government purchases. An increase in government purchases reduces output available for private use. This reduction in private resources makes households poorer.
and leads them to work more. (See Christiano and Eichenbaum 1992 and Baxter and King 1993 for details.)

Because these economies do not have distortions, such as distorting taxes or money, the allocations obtained as the solution to the maximization problem are also competitive equilibrium allocations. (See Stokey, Lucas, and Prescott 1989.) The solution to the optimization problem can be interpreted as the competitive equilibrium of an economy with a large number of identical consumers, all of whom start with \( k_0 \) units of capital, and a large number of firms, all of whom have access to the technology \( f(k, n) \) for transforming inputs into output. The equilibrium consists of rental prices for capital \( r_t = f_1(k_t, n_t) \) and labor \( w_t = f_2(k_t, n_t) \) and the quantities of consumption, labor, and investment at each date \( t = 0, \ldots, \infty \). In this economy, the representative consumer’s budget constraint is given by

\[
(A11) \quad r_t k_t + w_t n_t \geq c_t + i_t.
\]

The consumer’s objective is to maximize the value of discounted utility subject to the consumer’s budget constraint and the transition rule for capital \((A3)\). The firm’s objective is to maximize the value of profits at each date. Profits are given by

\[
(A12) \quad f(k_t, n_t) - r_t k_t - w_t n_t.
\]

The effects of monetary disturbances can also be studied in the neoclassical growth framework by introducing money into the model. The introduction of money, however, represents a distortion; consequently, the competitive equilibrium will not generally coincide with the solution to the optimization problem. (See Stokey, Lucas, and Prescott 1989.) In this case, the equations for the competitive equilibrium, rather than the optimization problem, are used in the analysis.
One widely used approach to adding money to the equilibrium model is to introduce a cash-in-advance constraint, which requires that consumption be purchased with cash:

\[(A13) \quad m_t \geq p_t c_t\]

where \(m_t\) is the money supply and \(p_t\) is the price (in dollars) of the physical good. In this model, changes in the money stock affect expected inflation, which, in turn, changes households’ incentives to work and thus leads to fluctuations in labor input. (See Cooley and Hansen 1989 for details.) More-complex monetary models, including models with imperfectly flexible prices or wages or imperfect information about the stock of money, also use the basic model as a foundation.
Notes

20 Solow’s (1956) original version of this model features a representative agent who in- elastically supplies one unit of labor and who consumes and saves a fixed fraction of output. Cass (1965) and Koopmans (1965) replace the fixed savings formulation of Solow with an optimizing representative consumer.
References


Bordo, Michael; Erceg, Christopher; and Evans, Charles. 1996. Money, sticky wages, and the Great Depression. Discussion paper, Rutgers University.


BOX

The Recession of 1921: The Recovery Puzzle Deepens

Many economists, including Friedman and Schwartz (1963), view the 1921 economic downturn as a classic monetary recession. Under this view, the 1921 recession and subsequent recovery support our view in the accompanying article that the weak 1934–39 recovery is puzzling.

In 1921, the monetary base fell 9 percent, reflecting the Federal Reserve’s policy which to reduce the price level from its World War I peak. This decline is the largest one-year drop in the monetary base in the history of the United States. The price level did fall considerably, declining 18.5 percent in 1921. Real per capita output also fell in 1921, declining 3.4 percent relative to trend.

Since many economists assume that monetary factors were important in both the 1929–33 decline and the 1921 recession, we compare these two downturns and their recoveries in the two tables shown here. These tables show the price level normalized to 100 in the year before the downturn and normalized detrended real per capita output.

There are two key differences between these periods. One is that the decrease in output relative to the decrease in the price level during the 1920s is small compared to the decrease in output relative to the decrease in the price level that occurred during the 1930s. The 18.5 percent decrease in the price level in 1921 is more than five times as large as the 3.4 percent decrease in output in 1921. In contrast, the decrease in the price level is only about 62 percent of the average decrease in output between 1929 and 1933. The other difference is that the 1921 recession was followed by a fast recovery. Even before the price level ceased falling, the economy began to recover. Once the price level stabilized, the economy grew rapidly.
Real per capita output was about 8 percent above trend by 1923, and private investment was nearly 70 percent above its 1921 level in 1923. This pattern is qualitatively consistent with the predictions of monetary business cycle theory: a drop in output in response to the price level decline, followed immediately by a significant recovery.

In contrast, the end of the deflation after 1933 did not bring about a fast recovery after the 1929–33 decline. This comparison between these two declines and subsequent recoveries supports our view that weak post-1933 macroeconomic performance is difficult to understand. The recovery from the 1921 recession offers evidence that factors other than monetary shocks prevented a normal recovery from the 1929–33 decline.
Figure 1: Detrended Levels of Output and Consumption
Figure 2: Actual and Predicted Output in 1929-39

- **Index (1929=100)**
  - Actual Output
  - Predicted Output

- **Years**
  - 1929
  - 1931
  - 1933
  - 1935
  - 1937
  - 1939
Figure 3: Personal Income vs Suspensions by State during the Depression

Commercial Bank Suspensions 1929-33 / Total Deposits 1929
Figure 4: Domestic Industries: Profits, Dividends and Retained Earnings

- After-tax Profits
- Dividends
- Retained Earnings