

The Wealth of Working Nations

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Motivation

- As the populations of advanced economies age, output growth per capita is becoming an increasingly misleading indicator for many purposes.
- Changes in the working-age population have become so large that output growth per capita can hide important movements in output per working-age adult (adults between 15 and 64 years old).
- Output per working-age adult: measure of how much we produce given available L and prevailing social norms.
- I will tackle the three issues I am asked about every time I explain this paper:
 1. YES, we are aware that some adults over 64 continue working.
 2. YES, we are aware that you can also measure GDP per worker/hour worked.
 3. YES, we are aware that for some important questions, total GDP or GDP per capita are still the relevant measurement.

This matters...a lot!

- Japan: the poster child of bad economic performance.
- Between 1991 and 2019, GDP in Japan grew at an annual rate of 0.83%, much lower than the 2.58% of the U.S.

Pesek (2014) and Japanization

...few lessons are more timely or critical than those offered by Japan, a once-vibrant model for developing economies that joined the world's richest nations, lost its way and has been struggling to relocate it ever since.

In this book I explore what the world can learn from a Japanese economic funk that began more than 20 years ago and has never really ended. That means exploring where Japan went wrong, how it sank under the weight of hubris and political atrophy, and missed opportunity after opportunity to scrap an insular model based on overinvestment, export-led growth, and excessive debt.

The blame game

- Fear of Japanization leads to vehement policy recommendations:
 1. More aggressive fiscal/monetary policy.
 2. More structural reforms.
- But if one looks at output per working-age adult, Japan has grown at an annual rate of 1.39%, while the U.S. has grown at a not-much-higher 1.65%.
- All the difference is accumulated in the 1990s. From 1998 to 2019, Japan has grown *slightly faster* than the U.S. in terms of per working-age adult: an accumulated 31.9% vs. 29.5%.
- Explanation: since 1991, working-age adults in Japan have fallen 14%; in the U.S., they have increased by 30%.

Issue I: What about older people working?

- Yes, indeed:
 1. Participation rate of adults in Japan 65 and over: 25.3% in 1991 and 25.3% in 2019.
 2. Participation rate of adults in the U.S. 65 and over: 11.5% in 1991 and 20.2% in 2019.
- We lack more detailed info on what older workers do (e.g., hours, occupation, etc.) and their contribution to GDP.
- So, we will perform a decomposition exercise where we “impute” workers older than 64 to the working-age population.
- Our results are roughly the same.

Issue II: Why not GDP per worker/hour worked?

- It is often argued that Western Europe's performance in terms of output per worker/hour worked is much better than its performance in terms of output per capita.
- Minor point: data on hours are not that great.
- Bigger point: number of workers and hours worked are *endogenous* to labor market policies, taxes, etc.
- For example, if restrictive labor regulations or high taxes expel from the labor force the less productive workers (as one would expect), average labor productivity would increase through a composition effect.
- Thus, high growth (or level) of GDP per worker/hour worked can be hard to interpret.
- Nonetheless, I will also show you an interesting decomposition later. Again, our results are roughly the same (except for Spain!).

Issue III: On the continuing usefulness of GDP and GDP per capita

- GDP and GDP per capita are still useful for many purposes.
- GDP: sustainability of public debt.
- GDP per capita: welfare.
- **Klenow et al. (2023)** argue for the importance of considering the total population to evaluate social welfare growth.

- We do not have much to say about migration *per se*. As far as it changes population, it is captured in our different measures.
- Interestingly: low correlation between immigration and output growth per working adult.
- Fertility? Really long lags (we will return to this later).

Rest of the presentation

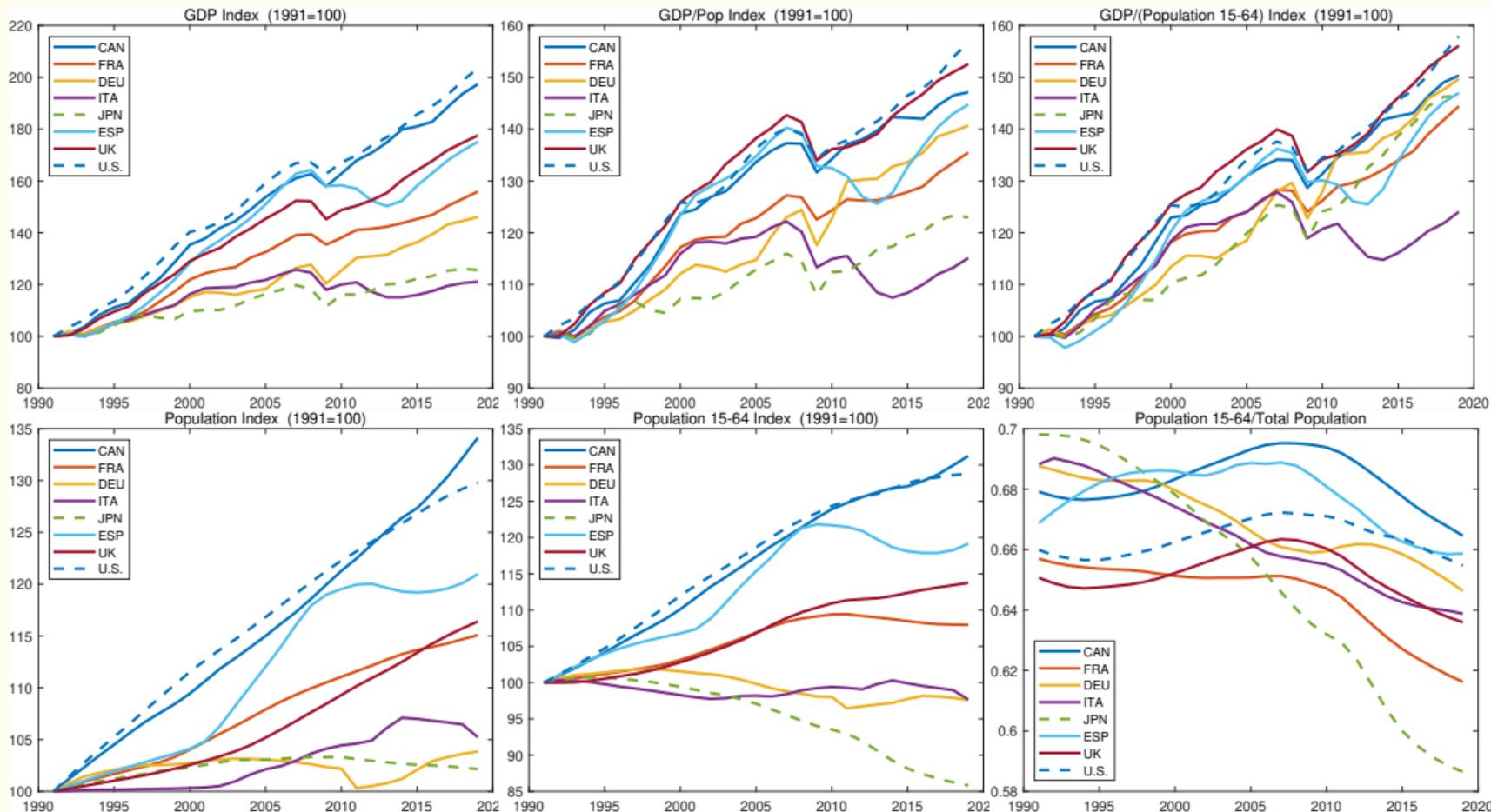
- Document the main argument for a larger sample of countries.
- Think about the data through the lenses of the neoclassical growth model.
- Discuss several extensions.
- Talk about China and India.
- (Maybe after we finish): Some final thoughts on the demographic future of humanity.

Data

- We use the World Bank's World Development Indicators (WDI) database.
- We did not have a good experience with the Penn World Tables (PWT). See [Pinkovskiy and Sala-i-Martin \(2016\)](#).
- G7 countries plus Spain.
- Real GDP is the GDP in national constant prices.
- The working-age population is the population between 15 and 64 years old.

Some facts

1991-2019	Canada	France	Germany	Italy	Japan	Spain	UK	U.S.
GDP	2.47	1.61	1.38	0.70	0.83	2.05	2.08	2.58
GDP per Capita	1.40	1.10	1.25	0.52	0.76	1.35	1.53	1.63
Population	1.05	0.50	0.14	0.18	0.08	0.68	0.54	0.94
GDP per Working-age adult	1.48	1.33	1.47	0.79	1.39	1.41	1.62	1.65
Working-age Population	0.98	0.27	-0.09	-0.08	-0.54	0.63	0.46	0.91



A decomposition

- We decompose output as follows:

$$Y_t = N_t \tilde{a}_t \tilde{e}_t \tilde{h}_t \tilde{y}_t$$

where:

1. N_t : total population at t .
 2. $\tilde{a}_t = (WA)_t / N_t$: working age adults per person.
 3. $\tilde{e}_t = E_t / (WA)_t$: employment per working-age adult.
 4. $\tilde{h}_t = H_t / E_t$: hours worked per employed person.
 5. $\tilde{y}_t = Y_t / H_t$: output per hour worked.
- We compute annual growth rates for each component.

Results

1991-2019		Canada	France	Germany	Italy	Japan	Spain	UK	USA
GDP	Y_t	2.47	1.61	1.38	0.70	0.83	2.05	2.08	2.58
Population	N_t	1.05	0.50	0.14	0.18	0.08	0.68	0.54	0.94
Working-age per person	\tilde{a}_t	-0.08	-0.23	-0.22	-0.27	-0.62	-0.05	-0.08	-0.03
Emp. rate working-age	\tilde{e}_t	0.42	0.35	0.57	0.34	0.74	0.90	0.36	0.17
Hours worked per worker	\tilde{h}_t	-0.17	-0.30	-0.40	-0.26	-0.61	-0.14	-0.11	-0.04
GDP per hour worked	\tilde{y}_t	1.23	1.28	1.31	0.71	1.26	0.67	1.37	1.53
Total hours	H_t	1.23	0.33	0.08	0.00	-0.43	1.40	0.71	1.04

Model

Why a model?

- We want a model to organize our thinking about the effects of changes in the working-age population.
- We could go as complex as desired (OLG structure, endogenous growth, endogenous fertility, migration, ...).
- I have done all of those in previous papers.
- The goal today is simpler: get the right intuition and orders of magnitude.
- Thus, a minimalistic model is better.

The Neoclassical growth model

- The economy populated by an infinitely lived representative household of varying size N_t .
- Preferences:

$$\max_{C_t/N_t} \sum_{t=0}^{\infty} \beta^t N_t \log \left(\frac{C_t}{N_t} \right)$$

- Output: $Y_t = K_t^\theta (A_t L_t)^{1-\theta}$.
- $A_t = A_0(1 + g)^t$: labor-augmenting technology. Thus, TFP equals $A_t^{1-\theta}$.
- $K_{t+1} = I_t + (1 - \delta)K_t$.
- $C_t + I_t = Y_t$.
- $N_t = \prod_{i=1}^t (1 + n_i)$, given $N_0 = 1$.

- Given the growth of technology g and population n , we must normalize the variables:

$$c_t = \frac{C_t}{A_t N_t},$$

$$k_t = \frac{K_t}{A_t N_t},$$

$$l_t = \frac{L_t}{A_t N_t},$$

$$y_t = \frac{Y_t}{A_t N_t} = \left(\frac{K_t}{A_t N_t} \right)^\theta \left(\frac{A_t L_t}{A_t N_t} \right)^{1-\theta} = k_t^\theta l_t^{1-\theta},$$

where $l_t = L_t/N_t$.

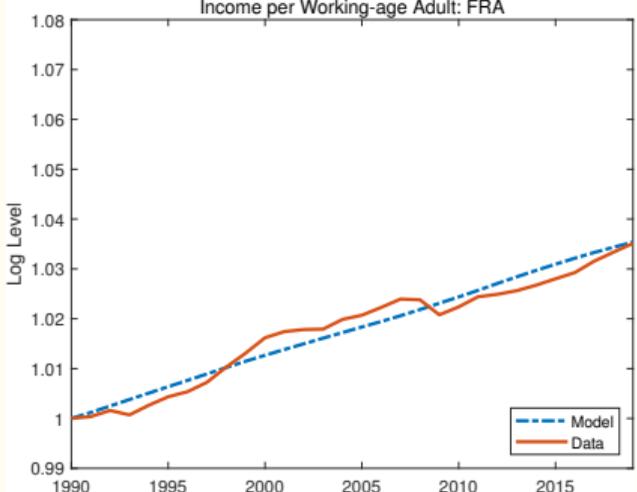
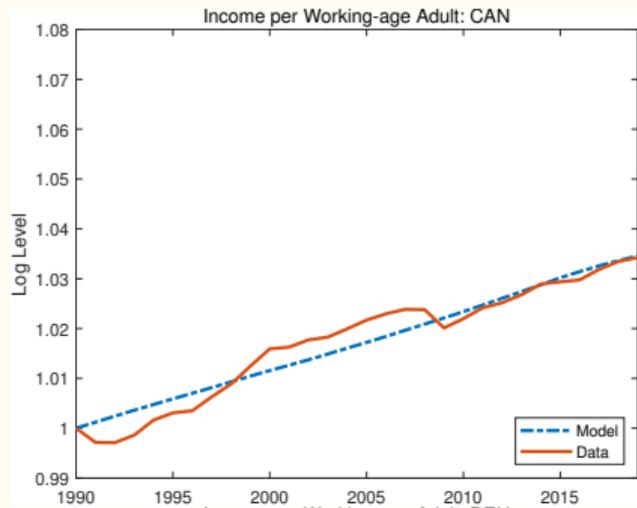
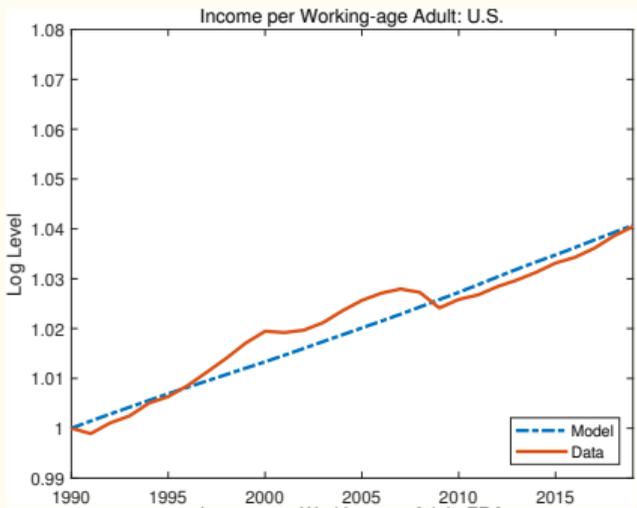
Intuition of the model

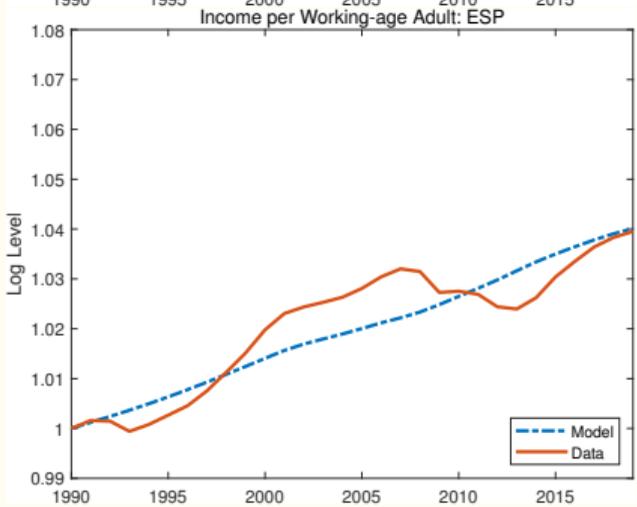
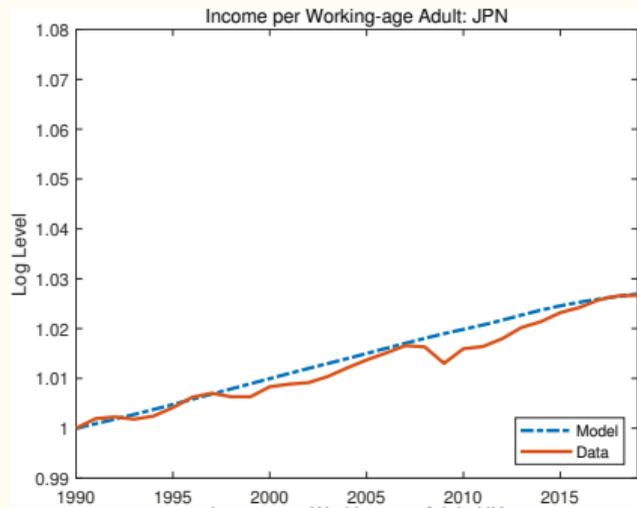
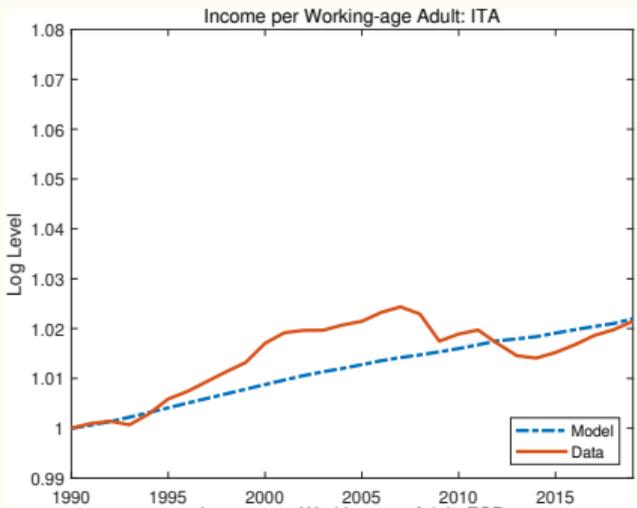
- A standard Euler equation:

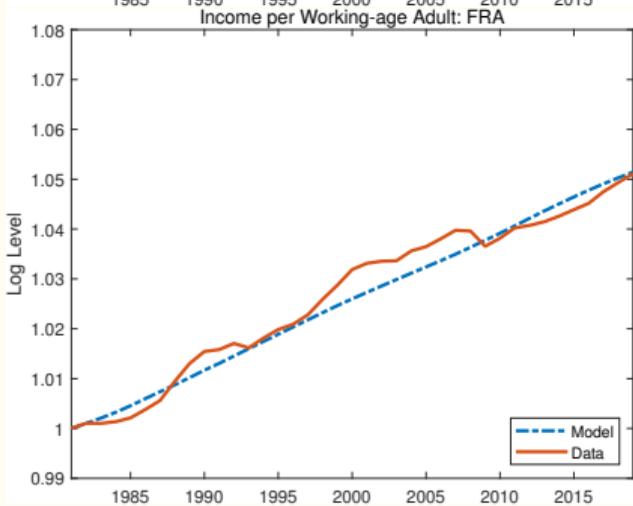
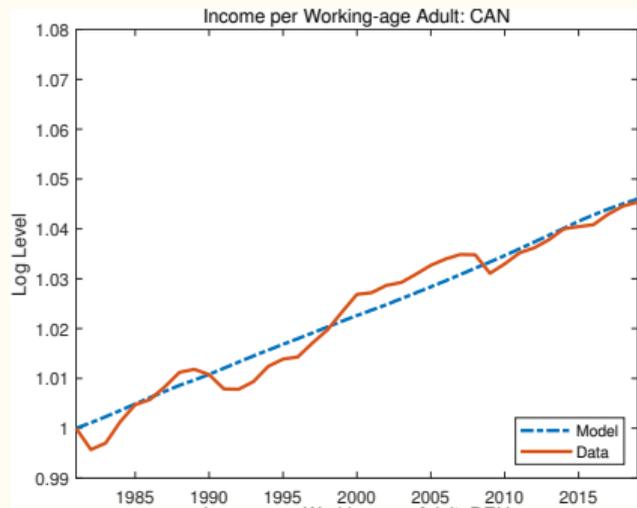
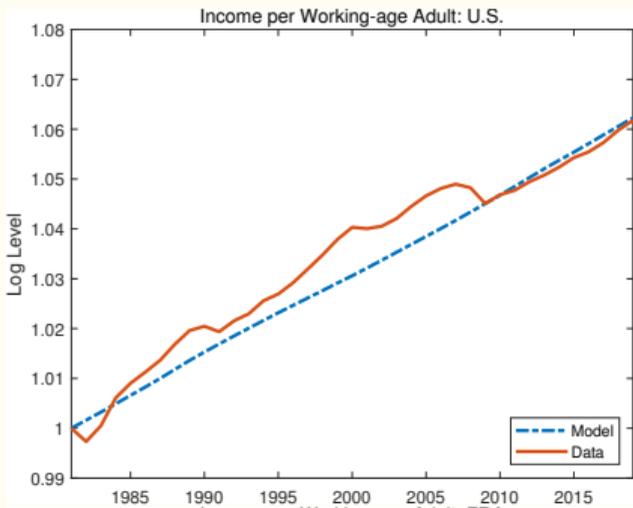
$$c_t^{-1}(1 + g) = \beta c_{t+1}^{-1} (\theta(k_{t+1})^{\theta-1}(l_{t+1})^{1-\theta} + 1 - \delta).$$

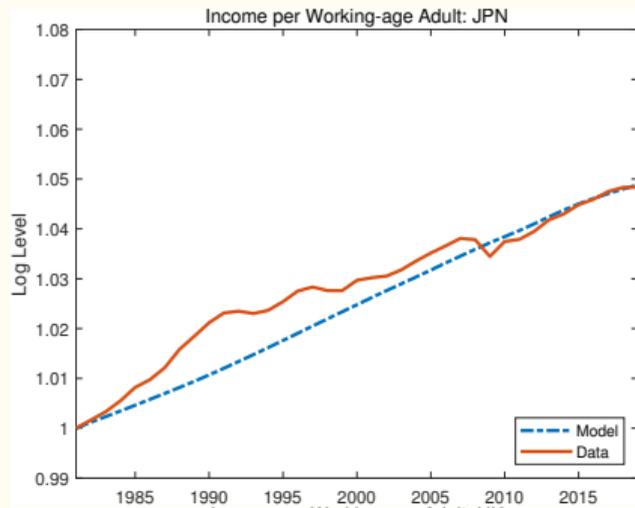
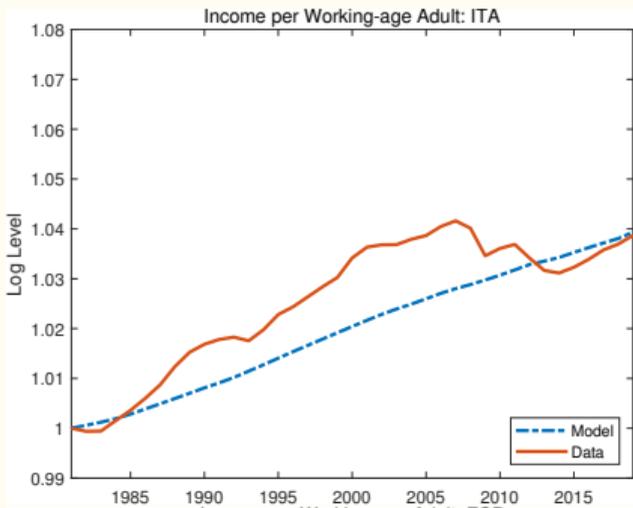
- This Euler equation looks like the optimality condition of the textbook neoclassical growth model with population and trend technological growth except for l_{t+1} .
- Case 1: $l_{t+1} = \hat{l}$ is constant. This is equivalent to a constant in front of the (normalized) production function and, hence, irrelevant to the dynamics of the model. Shocks to A_t have the usual effects on output and investment.
- Case 2: l_{t+1} changes. This is equivalent to a technological shock: a drop in l_{t+1} lowers total production, investment, and output.
- In other words, changes in l_{t+1} have the same effect as technological shocks in a real business cycle model without labor choice (and with the same persistence and propagation).

Parameter		Value
Discount factor	β	0.946
Capital share	θ	0.39
Depreciation rate	δ	0.04
Labor augmenting technology growth rate, Canada	g	0.0133
Labor augmenting technology growth rate, France	g	0.0103
Labor augmenting technology growth rate, Germany	g	0.0169
Labor augmenting technology growth rate, Italy	g	0.0107
Labor augmenting technology growth rate, Japan	g	0.0196
Labor augmenting technology growth rate, Spain	g	0.0165
Labor augmenting technology growth rate, U.K.	g	0.0188
Labor augmenting technology growth rate, U.S.	g	0.0178





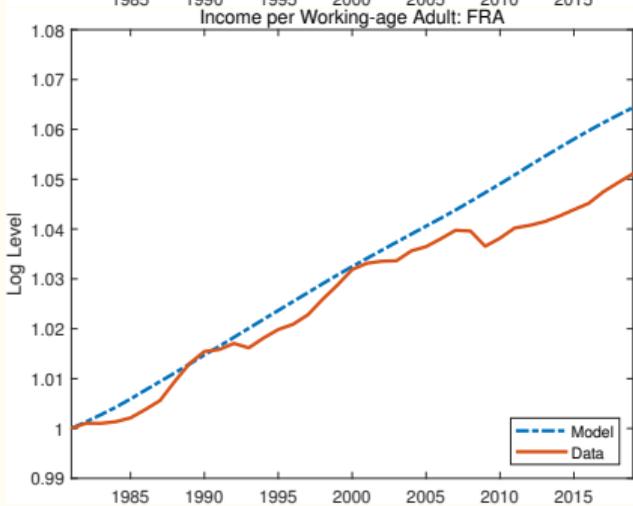
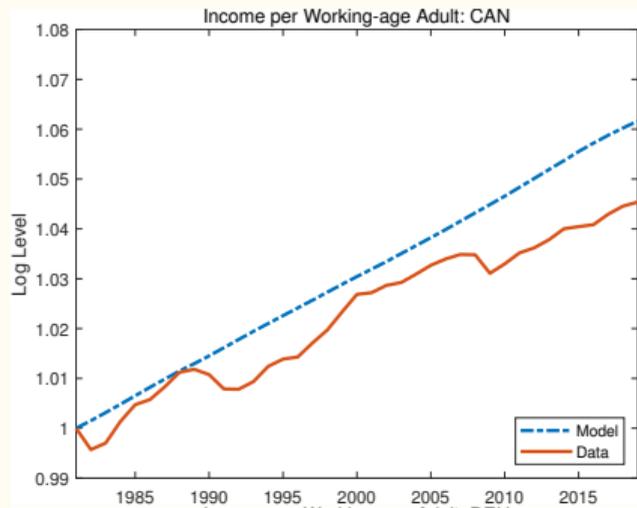
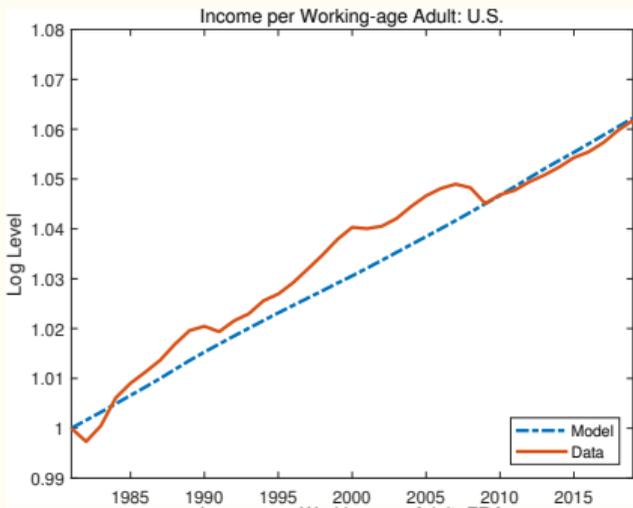


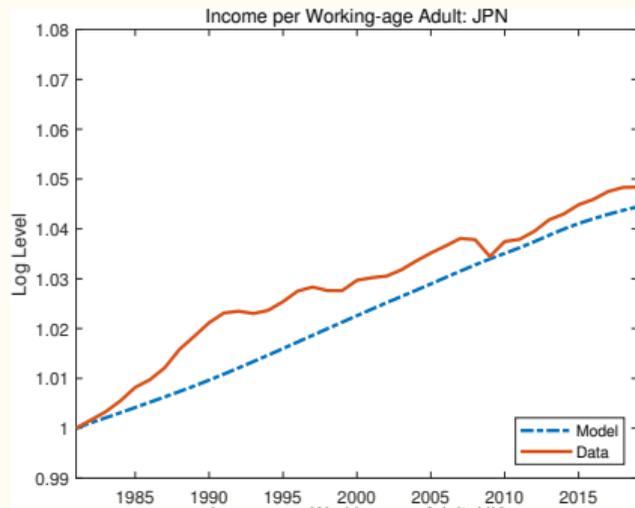
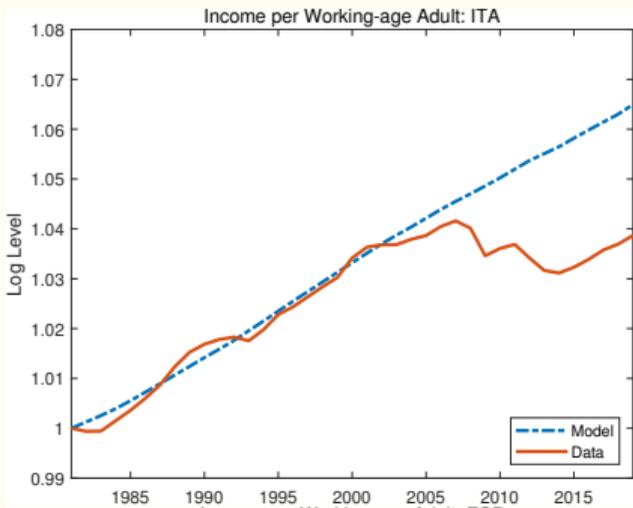


Extensions

An alternative calibration

- What if we use g from the U.S. instead of each country's?
- As a first-order approximation, one can consider the U.S.' g as a measure of the growth of the world's technological frontier.
- This exercise controls for the possibility that different aging speeds in each country might lead to different g 's.
- This exercise helps visualize the economies that have had mediocre (e.g., Canada) or disastrous performance (e.g., Italy).



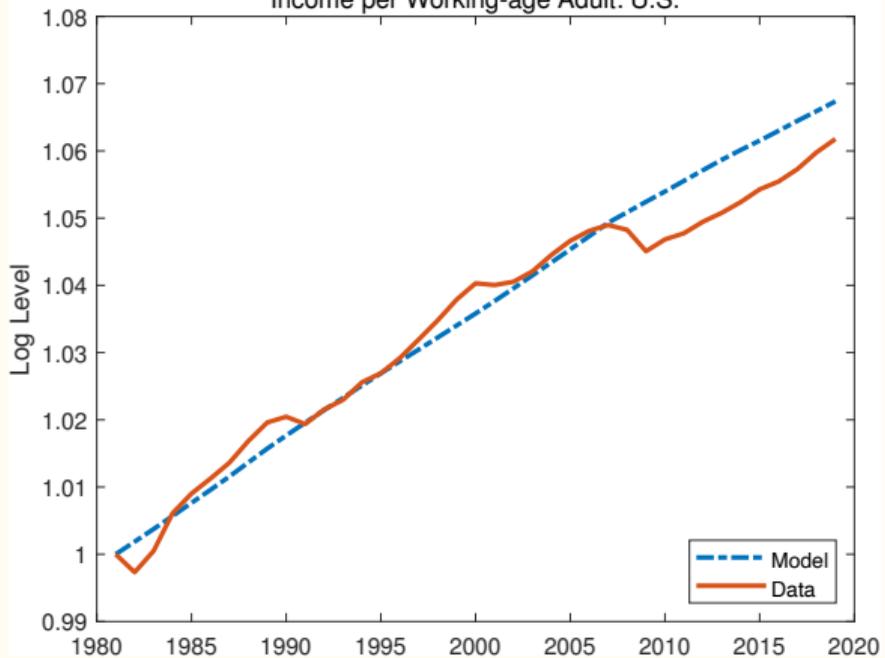


- We split our sample between the periods 1981-2007 and 2008-2019, or before and after the financial crisis.
- How can we incorporate this idea into the model?
 1. Different trend.
 2. Permanent drop.

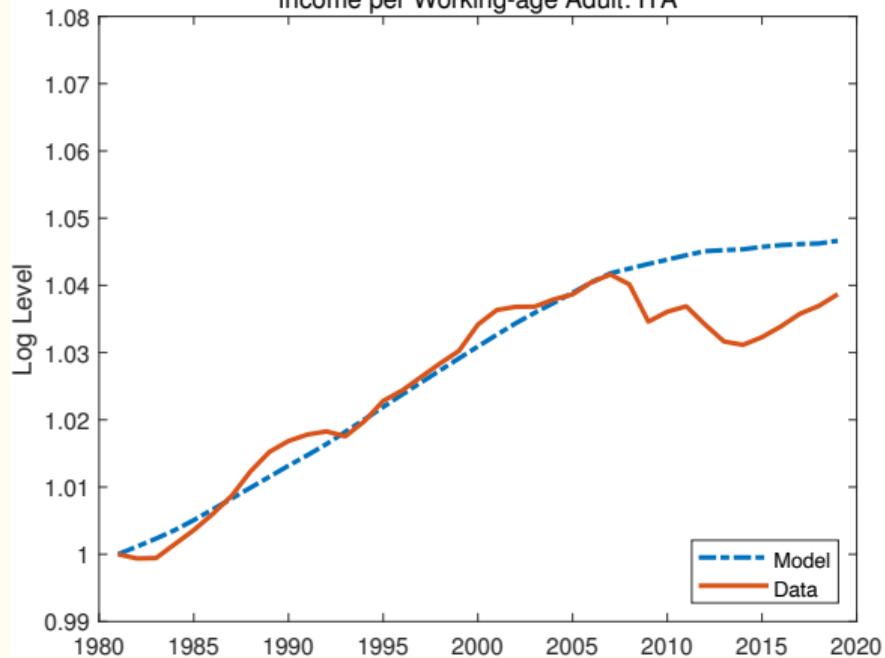
1981-2007	Canada	France	Germany	Italy	Japan	Spain	UK	USA
GDP	2.68	2.24	1.99	1.84	2.41	3.15	2.76	3.19
GDP per Capita	1.57	1.67	1.80	1.71	2.08	2.44	2.43	2.11
Population	1.09	0.56	0.19	0.13	0.32	0.70	0.33	1.05
GDP per Working-age Adult	1.49	1.61	1.84	1.67	2.25	2.10	2.31	2.06
Working-age Population	1.17	0.62	0.15	0.17	0.15	1.03	0.44	1.10
Working-age Pop. Ratio	0.68	0.65	0.68	0.67	0.68	0.67	0.65	0.66

2008-2019	Canada	France	Germany	Italy	Japan	Spain	UK	USA
GDP	1.79	1.03	1.27	-0.23	0.58	0.61	1.43	1.81
GDP per Capita	0.65	0.61	1.16	-0.36	0.68	0.38	0.71	1.11
Population	1.13	0.42	0.11	0.14	-0.10	0.23	0.71	0.70
GDP per Working-age Adult	1.07	1.11	1.35	-0.11	1.49	0.78	1.10	1.34
Working-age Population	0.71	-0.07	-0.08	-0.12	-0.90	-0.16	0.33	0.46
Working-age Pop. Ratio	0.68	0.63	0.66	0.65	0.61	0.67	0.65	0.66

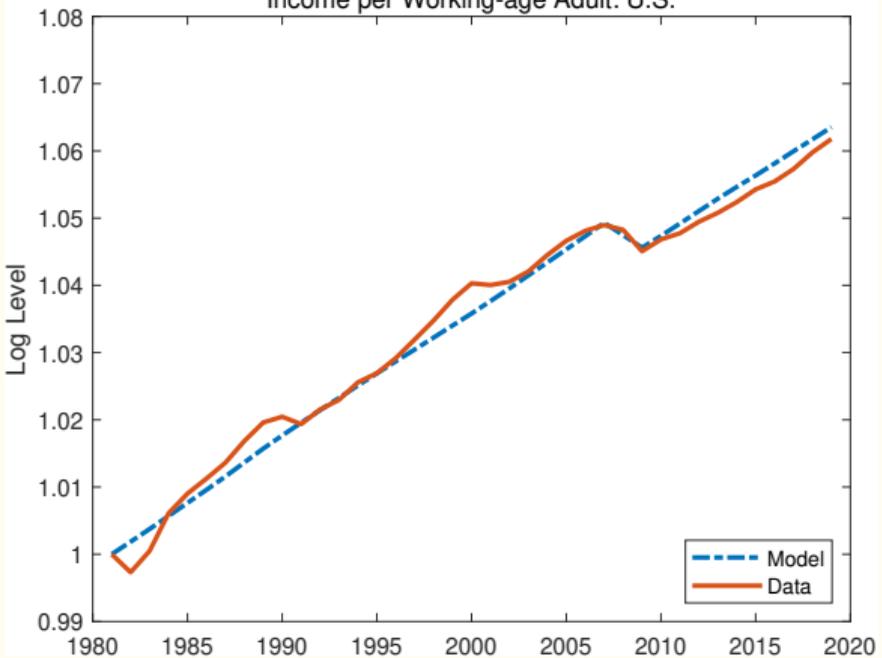
Income per Working-age Adult: U.S.



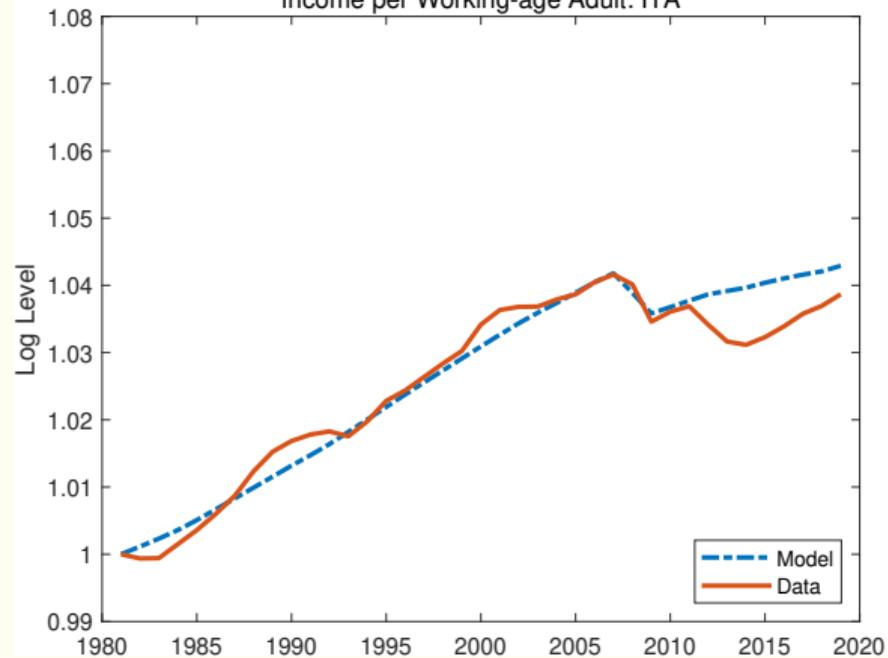
Income per Working-age Adult: ITA



Income per Working-age Adult: U.S.

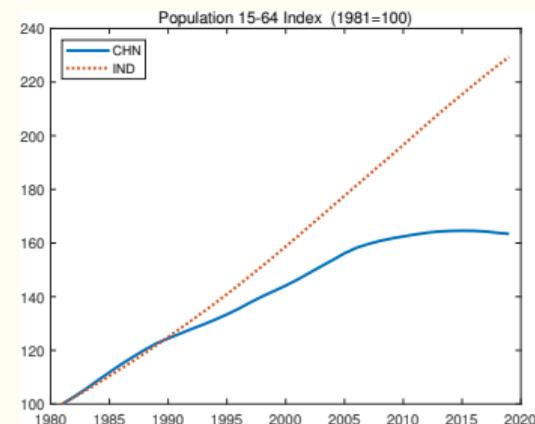
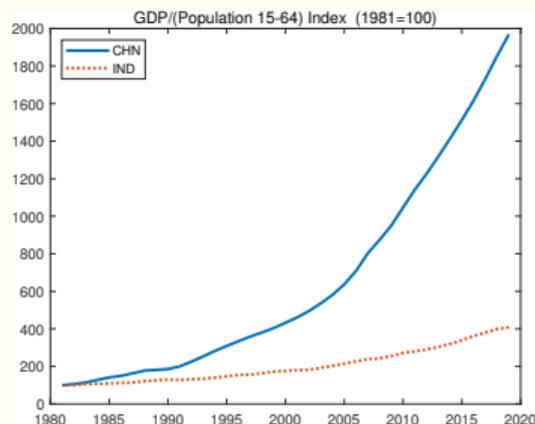
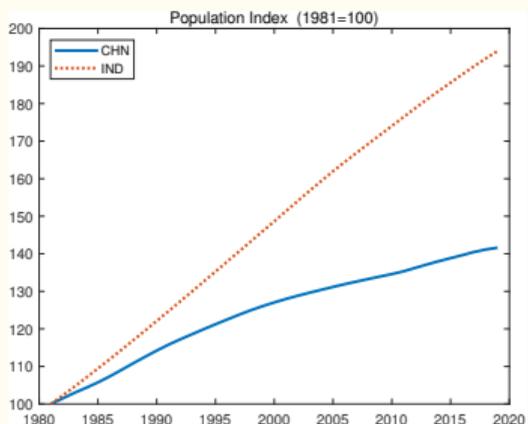
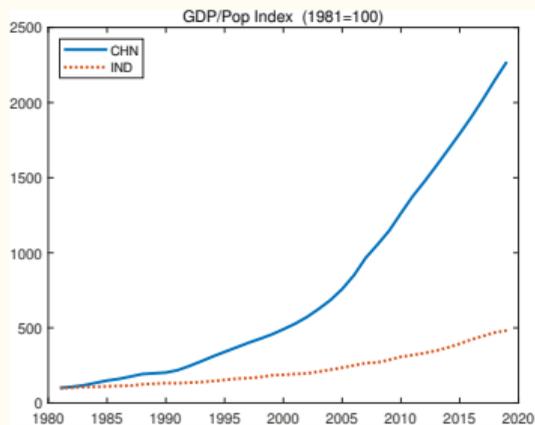
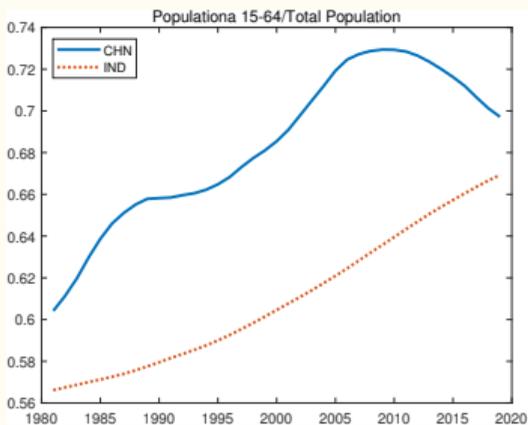
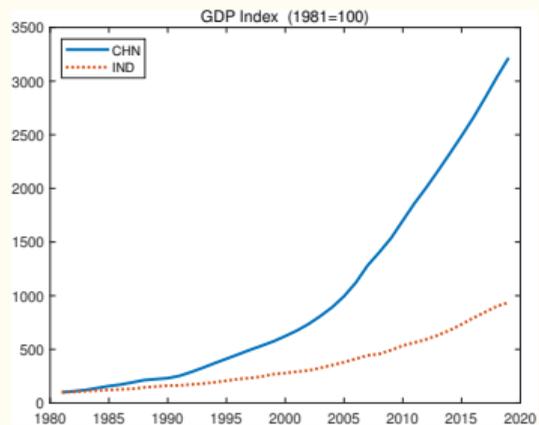


Income per Working-age Adult: ITA



China and India

1981-2019	China	India
GDP	9.60	6.08
GDP per Capita	8.60	4.25
Population	0.92	1.76
GDP per Working-age Adult	8.18	3.79
Working-age Population	1.31	2.21
Working-age Pop. Ratio	0.68	0.61



Some final thoughts on the demographic future of humanity

Quid rides? Mutato nomine de te fabula narratur

- The present of Japan is the future of the globe.

The total fertility rate (TFR) of a population

The average number of children that would be born to a woman over her lifetime if:

1. She were to experience the current age-specific fertility rates throughout her lifetime.
2. She were to live through ages 15-44.

- Japan's TFR fell below 2.1 (explanation of the importance of 2.1 in next slide) in 1974. Right now is around 1.25.
- A few other examples:
 1. Iran: 1.69.
 2. U.S.: 1.62.
 3. Brazil: 1.45.
 4. China: 1.0
 5. South Korea: 0.7.

The replacement rate

- The TFR governs whether a population reaches the *replacement rate*: whether enough children are born to sustain population levels (forgetting net immigration).
- A simple formula:

$$\text{Replacement rate} \approx \frac{1 + \text{sex ratio at birth}}{\text{Probability of a woman to survive to 30}}$$

- Replacement rate for rich countries: ≈ 2.1 . Why?
 - Without outside intervention ≈ 1.05 boys are born for every girl.
 - Probability of a woman surviving to 30 is about 0.98.
- Thus:

$$\text{Replacement rate rich country} \approx \frac{1 + 1.05}{0.98} \approx 2.1$$

The replacement rate in developing economies

- Think, however, about developing countries with different parameters:

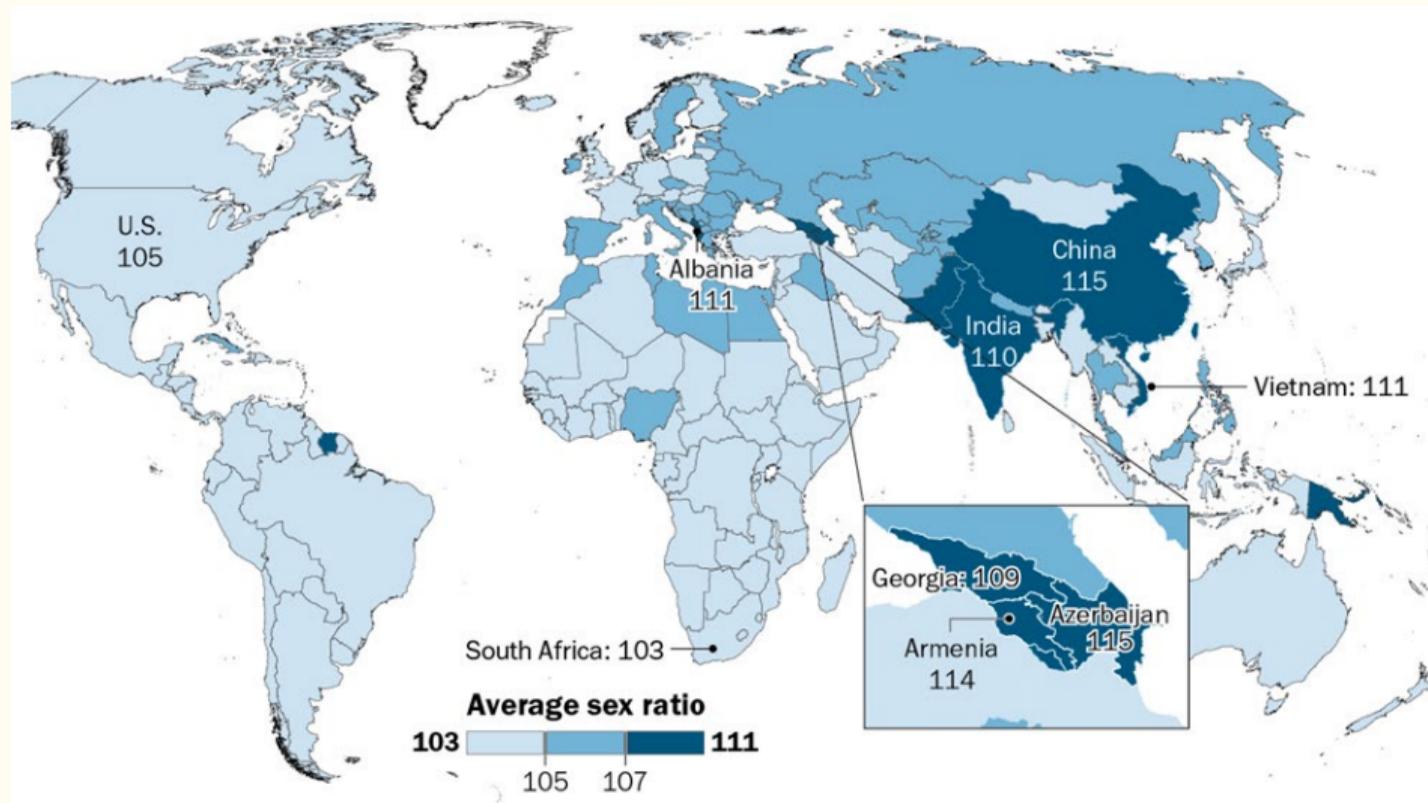
1. Many populations practice selective abortions.
2. Female mortality rates are quite higher.

- Thus:

$$\text{Replacement rate developing country} \approx \frac{1 + 1.1}{0.8} \approx 2.6$$

- Replacement rate for some African countries can be as high as 3.

Average sex ratio at birth, or the number of male births per 100 female births, from 2000-20



Note: Globally, the natural sex ratio at birth ranges from 103 to 107 boys per 100 girls.
Source: United Nations World Population Division, 2019.
"India's Sex Ratio at Birth Begins To Normalize"

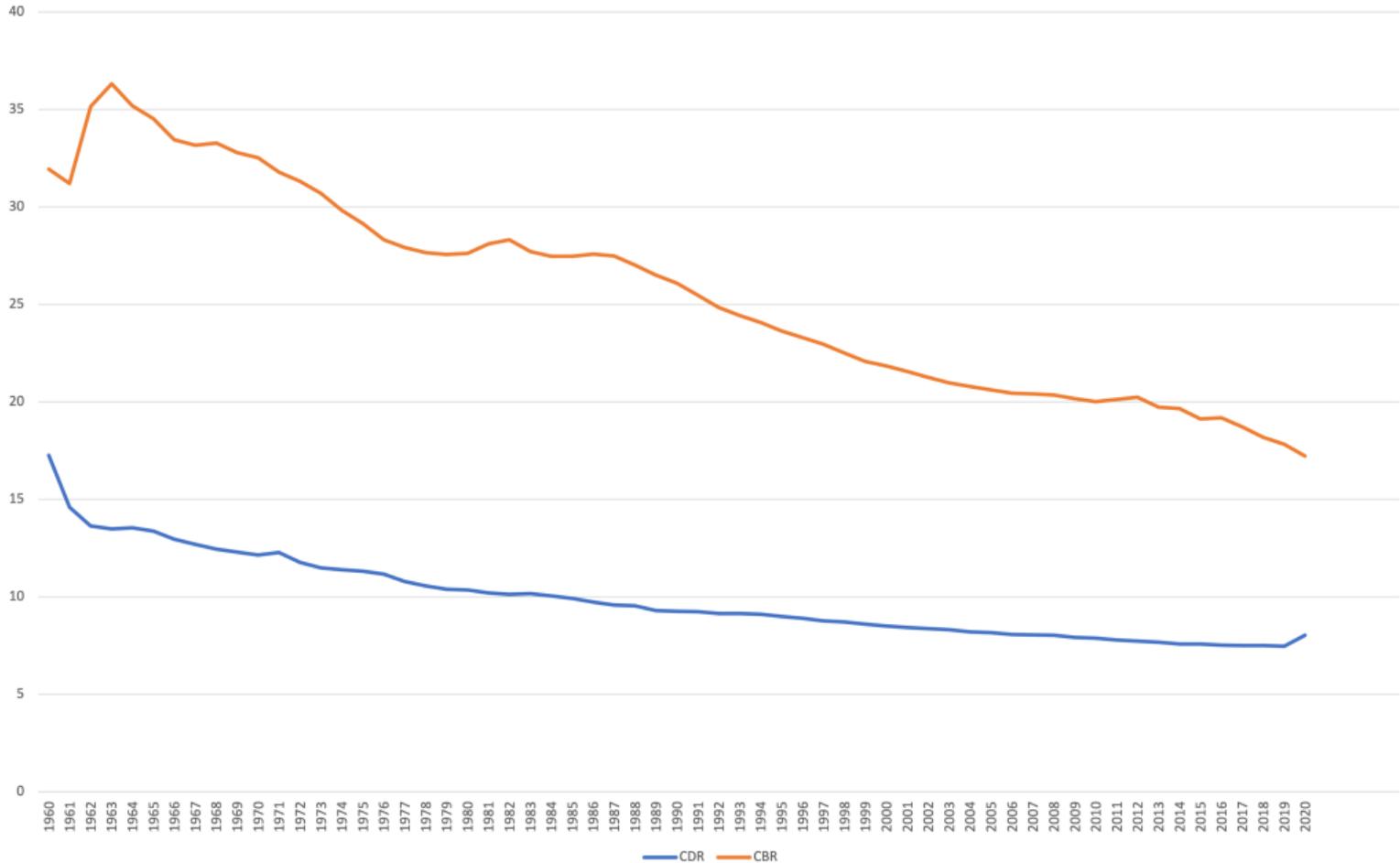
The world replacement rate

- The world replacement rate in 2023:

$$\text{Replacement rate world} \approx \frac{1 + 1.07}{0.91} \approx 2.25$$

- According to the United Nations World Population Prospects 2022, the world TFR is 2.3.
- However, the United Nations World Population Prospects *overestimate* the world TFR. For example, in 2023, there were 9 million births in China vs. 10.6 million in the UN forecast.
- I calculate that we are around 2.1-2.2.
- Thus, most likely, the world is *already below* the replacement rate.
- The world population is still growing: momentum effect of past large cohorts and increases in life expectancy.

CBR vs. CDR



When will momentum end?

- More uncertainty here: it depends on the future evolution of fertility and mortality.
- According to the United Nations World Population Prospects 2022, medium variant, the world population will peak in 2086 at 10.43 billion (vs. 8 billion right now).
- I disagree. I see the peak of population size at around 9.7 billion c. 2055.
- Why?
 1. United Nations World Population Prospects are conservative in their assumptions about the fall of fertility:
 - For example, China had in 2023 the births the United Nations World Population Prospects forecasted for 2050.
 - The United Nations World Population Prospects assumes partial recoveries of fertility in low-fertility countries. We have yet to see many examples of this happening.
 2. My research shows that fertility falls are becoming faster.

An easy way to check: “the rule of 85”

- Imagine you have a country where life expectancy is 85 years: the highest life expectancy in the world right now (Japan, Spain, etc.).
- Imagine that, from now on, you have 1,000 births per year, every year.
- What would be your population in about 100 years? $85,000 = 85 * 1,000$.
- Thus, you can look at the current births of any given country, multiply by 85, and get *a sense* of the long-run population (without migrations).
- For example, South Korea had 230k births in 2023. Long-run population: 19.5 million ($85 * 230k$). Current population: 51.6 million.
- An equivalent way to look at it: $1000/85 = 11.76$. When a country's CBR falls below 11.76 per 1000, births are already insufficient to keep the population constant (this usually happens *around 30 years after* TFR falls below replacement).

Let me stop here

- First time that humanity is below the replacement rate in the last 100,000 years.
- Yes, the world population often dropped. Still, it was caused by famines and diseases, not by low births (wars never were so crucial demographically speaking at the global level because they tend to be localized).
- Furthermore, the world TFR is falling very fast all across the globe (including Africa!).
- In fact, faster than most forecasts, even ten years ago.