

Exercise #1-4, 6-10

- 1) The two main components of dry air are N_2 and O_2 . Air does not absorb microwave radiation because N_2 and O_2 are symmetrical homonuclear molecules that do not have a permanent dipole moment, and therefore do not absorb microwaves to produce rotational spectra.
- 2) BF_3 (trigonal planar), S_2 (linear), CO_2 (linear), SO_3 (trigonal planar), and $SiCl_4$ (tetrahedral) will not produce rotational spectra because they are very symmetric molecules. [NH_3 —trigonal bipyramidal; SO_2 —bent are asymmetrical and will produce rotational spectra].
- 3) The selection rule is that $\Delta J = +1$ or -1 . $J=5 \rightarrow J=4$ and $J=4 \rightarrow J=5$ are allowed.
- 4) $\omega = 3.842 \text{ cm}^{-1} = 384.2 \text{ m}^{-1}$; $E = hc \omega = (6.63 \times 10^{-34} \text{ J s}) (3.00 \times 10^8 \text{ m/s}) (384.2 \text{ m}^{-1}) = 7.64 \times 10^{-23} \text{ J}$
 $\lambda = hc/E = (6.63 \times 10^{-34} \text{ J s}) (3.00 \times 10^8 \text{ m/s}) / (7.64 \times 10^{-23} \text{ J}) = 0.00260 \text{ m} = 2.6 \text{ mm}$

$$E (J=1 \rightarrow J=0) = 7.64 \times 10^{-23} \text{ J (the energy for } J=0 \rightarrow J=1)$$

$$I, \text{ moment of inertia for } {}^{12}C^{16}O \text{ molecule} = \mu r^2 = (12 \times 15.995) / (12 + 15.995) = 6.8562 \text{ g/ mole} \times (1 \text{ mole} / 6.02 \times 10^{23} \text{ molecules}) r^2 = (1.1389 \times 10^{-23} \text{ g/ molecule}) r^2 = (1.1389 \times 10^{-26} \text{ kg/ molecule}) r^2$$

$$E (J=0 \rightarrow J=1) = 2B_e = 2h^2 / (8\pi^2 \mu r^2) = 7.64 \times 10^{-23} \text{ J}$$

$$r = \sqrt{(2h^2 / (8\pi^2 (1.1389 \times 10^{-26} \text{ kg}) (7.64 \times 10^{-23} \text{ J})))} = \sqrt{1.28 \times 10^{-20} \text{ m}^2} = 1.13 \times 10^{-10} \text{ m} = 113 \text{ pm}$$

- 6) $E (J=1 \rightarrow J=2) = 4B_e = 4h^2 / (8\pi^2 \mu r^2) = 10.19 \times 10^{-24} \text{ J}$
 $\mu \text{ for } {}^{39}K^{35}Cl = (38.96 \times 34.97) / (38.96 + 34.97) = 18.43 \text{ g/ mole} \times (1 \text{ mole} / 6.02 \times 10^{23} \text{ molecules})$
 $= 3.061 \times 10^{-23} \text{ g/ molecule} = 3.061 \times 10^{-26} \text{ kg/ molecule}$
 $r = \sqrt{(4h^2 / (8\pi^2 (3.061 \times 10^{-26} \text{ kg}) (10.19 \times 10^{-24} \text{ J})))} = \sqrt{7.14 \times 10^{-20} \text{ m}^2} = 2.67 \times 10^{-10} \text{ m} = 267 \text{ pm}$
- 7) $v = 6.350 \times 10^5 \text{ MHz} = 6.350 \times 10^{11} \text{ Hz}$
 $E = hv = (6.63 \times 10^{-34} \text{ J s}) (6.350 \times 10^{11} \text{ Hz}) = 4.210 \times 10^{-22} \text{ J}$
 $\mu \text{ for } {}^1H^{35}Cl = (1.008 \times 34.97) / (1.008 + 34.97) = 0.9798 \text{ g/mole} \times (1 \text{ mole} / 6.02 \times 10^{23} \text{ molecules})$
 $= 1.628 \times 10^{-24} \text{ g/ molecule} = 1.628 \times 10^{-27} \text{ kg/ molecule}$

$$E \text{ spacing } (J=0 \rightarrow J=0) = B_e = h^2 / (8\pi^2 \mu r^2) = 4.210 \times 10^{-22} \text{ J}$$

$$r = \sqrt{(h^2 / (8\pi^2 (1.628 \times 10^{-27} \text{ kg}) (4.210 \times 10^{-22} \text{ J})))} = \sqrt{8.123 \times 10^{-21} \text{ m}^2} = 9.013 \times 10^{-11} \text{ m} = 90.13 \text{ pm}$$

Yes, this bond length makes sense—it is smaller than for KCl and it should be K is in the fourth period and considerably bigger than H.

- 8) Dry air does not absorb IR radiation because the major components of dry air, N_2 and O_2 , are homonuclear diatomic molecules. They cannot increase their vibrational energy by absorption of IR radiation because their dipole moments do not oscillate during vibration. Water, on the other hand, is a bent molecule with 2 H atoms and O atoms. It can absorb IR radiation because it has an oscillating dipole moment associated with its three vibrational modes—its antisymmetrical stretching mode, its symmetric stretching mode, and its bending mode (<http://www.lsbu.ac.uk/water/vibrat.html> or <http://www.atmos.albany.edu/deas/atmclasses/atm335/vib1.htm>).
- 9) The bending mode of CO_2 will be excited by IR radiation because its dipole moment oscillates during the bending motion.
- 10) The antisymmetrical stretch of CO_2 will also be excited by IR radiation because its dipole moment oscillates during the antisymmetric stretching motion.