Financial Integration, Financial Development and Global Imbalances

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Abstract

Global financial imbalances can be the outcome of financial integration when countries differ in financial markets development. Countries with more advanced financial markets accumulate foreign liabilities in a gradual, long-lasting process. Differences in financial development also affect the composition of foreign asset portfolios: countries with negative net foreign asset positions maintain positive net holdings of non-diversifiable equity and FDI.

Three empirical observations motivate our analysis: (1) financial development varies widely even among industrial countries, with the United States ranking at the top; (2) the secular decline in the U.S. net foreign asset position started in the early 1980s, together with a gradual process of international financial integration; (3) the portfolio composition of U.S. net foreign assets features increased holdings of risky assets and a large increase in debt.
1 Introduction

At the end 2006, the current account deficit of the United States reached 1.6 percent of the world’s GDP, the largest in the country’s history. Continuing a trend that started in the early 1980s, the U.S. net foreign asset (NFA) position fell to -5 percent of the world’s output. During this period, the U.S. foreign asset portfolio also changed dramatically: net equity and FDI climbed to 1/10 of U.S. GDP, while net debt obligations increased sharply to about 1/3 of U.S. GDP.

These unprecedented global imbalances are the focus of a large and growing literature. Some studies argue that the imbalances resulted from economic policy misalignments in the U.S. and abroad,¹ while others argue that they were caused by events such as differences in productivity growth, business cycle volatility, demographic dynamics, a ‘global savings glut,’ or valuation effects.² To date, however, a quantitatively consistent explanation of both the unprecedented magnitude of the changes in NFA positions and the striking changes in their portfolio structure has proven elusive.

In this paper we show that both of these phenomena can be explained as the equilibrium outcome of financial integration across countries with heterogeneous domestic financial markets. This is a relevant hypothesis because the reforms that integrated world capital markets starting in the 1980s were predicated on their benefits for efficient resource allocation and risk sharing across countries, ignoring the fact that domestic financial systems differed substantially,

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¹See, for example, Summers (2004), Obstfeld and Rogoff (2004), Roubini and Setser (2005), Blanchard, Giavazzi, and Sa (2005), Krugman (2006).

and these differences persist today despite the globalization of capital markets. In short, financial integration was a global phenomenon, but financial development was not.

The empirical motivation for our analysis derives from three key observations:

1. **There is a high degree of heterogeneity in domestic financial markets across countries, and these differences remain largely unaltered despite financial globalization and financial development.** The top panel of Figure 1 plots the financial development index constructed by the International Monetary Fund for industrial countries (see IMF (2006)). The index shows that there are large differences even among advanced economies, with the United States ranked first. In addition, the gaps of other industrial countries relative to the U.S. did not change significantly between 1995 and 2004. Similar features are evident in another index of financial development constructed by Abiad, Detragiache, and Tressel (2008) for industrial and emerging economies for the 1973-2002 period. As shown in the bottom panel of Figure 1, while financial liberalization progressed in both OECD and emerging economies over the last 30 years, the gap between the two groups of countries has not changed.

[Place Figure 1 here]

2. **The secular decline of the NFA position of the most financially developed country—the United States—began roughly at the same time as the financial globalization process, in the early 1980s.** The top panel of Figure 2 shows the Chinn-Ito financial openness index for the United States, the industrial countries excluding the U.S., and all countries except the U.S. Capital markets in the United States have been relatively open to the rest of the world throughout the last three decades. Most of the other countries started opening their capital
accounts gradually since the early 1980s. The bottom panel of Figure 2 shows that this process of financial integration produced a world-wide surge in gross stocks of foreign assets and liabilities.

[Place Figure 2 here]

3. The decline in the U.S. NFA position was accompanied by a marked change in the portfolio composition of foreign assets of all countries. Figure 3 plots the two broad components of the total NFA positions: Net debt instruments (including international reserves) and net portfolio equity and foreign direct investment (FDI). The plots show that the United States increased net holdings of risky assets (portfolio equity and FDI), and reduced net holdings of riskless assets into a very large negative position. Other industrial countries changed net holdings of risky assets in a similar way, but hardly changed holdings of riskless assets. The emerging economies reduced net holdings of risky assets and increased holdings of riskless assets. See also Curcuru, Dvorak, and Warnock (2008), Gourinchas and Rey (2007) and Lane and Milesi-Ferretti (2007).

[Place Figure 3 here]

We build a model suitable for empirical analysis where we take as given observations 1. and 2. to explain the facts highlighted in 3. (i.e. the changes in NFA positions and in their portfolio structure). In our model, countries are inhabited by ex-ante identical agents who face two types of idiosyncratic shocks: endowment and investment shocks. Financial development is defined by the extent to which a country’s legal system can enforce
financial contracts among its residents so that they can use these contracts to insure against
idiosyncratic risks.

In our model, the state of development of a country’s legal system is represented by
the fraction of individual income that the country’s residents can divert from creditors. In
autarky, countries with better legal systems, or more financially developed, attain lower
average wealth-to-income ratios and higher interest rates. Upon financial liberalization,
interest rates are equalized across countries but the gap in their wealth-to-income ratios
widens significantly. The latter occurs after a protracted process that takes several years
to be completed, and that is responsible for large, sustained declines in NFA positions like
the one experienced by the United States. We show that moderate differences in financial
development can easily lead to NFA positions larger than half of domestic production.
Moreover, the adjustment process of NFA can take more than 30 years.

A second key feature that characterizes the legal systems is that enforcement is “residence
based”. That is, the enforcement of financial contracts is determined by the law of the
country where the agent resides. Alternatively, “source based” enforcement would imply
that the enforcement of financial contracts is determined by the law of the country where
the incomes are generated. With residence based enforcement, our model can explain not
only the change in overall NFA positions but also their portfolio structure (i.e. the most
financially developed country has a large, negative NFA position, but it also has positive net
holdings of non-diversifiable equity and large, negative net holdings of riskless bonds). Our
quantitative analysis shows that this is indeed the case for economies that resemble the U.S.
vis-a-vis the rest of the world. Moreover, a three-country extension of the model accounts
for both the large negative NFA position of the United States and the differences in portfolio
structures across the United States, other industrial countries and emerging economies.

The premise that differences in domestic financial markets can produce external imbalances has precedent in the literature. Willen (2004) studied the qualitative predictions of a two-period endowment-economy model with exponential utility and normal-i.i.d. shocks. He showed that, under incomplete markets, trade imbalances emerge due to reduced savings by the agents residing in countries with ‘more complete’ asset markets. Our model embodies this mechanism but differs in two key respects. First, we allow for endogenous production with ‘production risks,’ which is necessary for explaining the composition of asset portfolios. Second, we study an infinite horizon model with standard constant relative risk aversion preferences, exploring both the qualitative and quantitative predictions of the model.

Caballero, Farhi, and Gourinchas (2008) also emphasize the role of heterogeneous domestic financial systems in explaining global imbalances, but using a model in which financial imperfections are captured by a country’s ability to supply assets in a world without uncertainty. In our framework, instead, financial imperfections have a direct impact on savings, and therefore, on the demand for assets. Uncertainty is crucial in our framework: without risk there are no imbalances even if financial markets are heterogeneous. The two papers also differ in the main driving forces of global imbalances. In Caballero et al. the imbalances are generated by differential shocks to productivity growth and/or to the financial structure of countries. Our explanation relies instead on the integration of capital markets, given the differences in the characteristics of domestic financial markets.

Our work is also related to studies that investigate global imbalances with quantitative dynamic general equilibrium models (see IMF (2005), Hunt and Rebucci (2005) and Faruqee et al. (2007)). In these studies, global imbalances emerge as the outcome of a combination of
exogenous shocks, such as a permanent increase in the U.S. fiscal deficit, a permanent decline in the rate of time preference in the U.S., and a permanent increase in foreign demand for U.S. financial assets. In contrast, our model predicts a reduction in U.S. savings and an increase in the foreign demand for U.S. assets endogenously, after financial integration, because of the different characteristics of the U.S. financial system. This occurs even if all countries have identical preferences, resources and production technologies.

The rest of the paper is organized as follows: Section 2 describes a basic two-country framework that we use to characterize analytically the key theoretical results. Section 3 extends the basic model to make it suitable to map it to the data. Section 4 conducts the quantitative analysis and identifies the winners and losers from financial liberalization. Section 5 compares the implications of our assumption of residence based enforcement with different variants of source based enforcement. We find that if enforcement of financial contracts involving international payments is fully source based in all countries, our model still accounts for large negative positions in NFA and riskless assets in the most financially developed country, but it does produce positive net holdings of risky assets in that country. However, mixed environments that combine source and residence based enforcement, which are likely to be more realistic, support equilibria with positive net foreign equity positions in the most financially developed country. Section 6 extends our notion of financial development to allow for differences in borrowing limits. This allows the model to account for differences in portfolio structures across the U.S., other industrial countries and emerging economies. This section also shows that the results can be extended to the case in which there are differences in growth rates and income volatility across countries. Section 7 concludes.
2 A model of financial globalization with financial heterogeneity.

We now describe a simple version of the model that illustrates the key properties analytically. These properties are preserved in the general setup we will use in the quantitative analysis.

Consider an economy composed of two countries, \( i \in \{1, 2\} \), inhabited by a continuum of agents of total mass 1. Agents maximize the expected lifetime utility \( E \sum_{t=0}^{\infty} \beta^t U(c_t) \), where \( c_t \) is consumption at time \( t \) and \( \beta \) is the discount rate. The utility function is strictly increasing and concave with \( U(0) = -\infty \) and \( U'''(c) > 0 \).

Each country is endowed with a unit of a non-reproducible, internationally immobile asset, traded at price \( P^i_t \). This asset can be used by each agent in the production of an homogeneous good, with a one-period gestation lag. Thus, the individual production function is \( y_{t+1} = z_{t+1} k_t^\nu \), where \( k_t \) is the quantity of the asset used at time \( t \), \( z_{t+1} \) is a project-specific idiosyncratic discrete shock, and \( y_{t+1} \) is the output produced at time \( t + 1 \). We refer to \( z_{t+1} \) as an investment shock because it determines the ex-post return on the investment \( k_t \).

We assume that \( \nu < 1 \), i.e. individual production displays decreasing returns to scale. This property derives from the assumption that production also requires the input of managerial or organizational capital, of which agents have limited supply. Managerial capital cannot be divided among multiple projects but it is internationally mobile. Therefore, with capital mobility agents can choose to operate at home, buying the domestic productive asset, or abroad, buying the foreign productive asset. Without capital mobility, agents can buy only the productive asset located at home.\(^3\)

\(^3\)The limited supply of the productive asset is similar to the Lucas’ tree model with two important differences. First, the tree or the fruits of the tree are combined with another input of production, the managerial capital. This introduces decreasing returns to scale. Second, shocks to production, which can also be interpreted as shocks to the fruits of the tree, are project-specific, and therefore, ‘idiosyncratic’. In the typical Lucas’ tree model, the realizations of the shocks are the same for all agents operating in the same
Agents also receive income in the form of an *idiosyncratic* stochastic endowment, $w_t$, that follows a discrete Markov process. Therefore, there are two types of risk due to endowment and investment shocks. We can interpret $w_t$ as labor income and $y_t$ as capital income.

The impact of endowment shocks is beyond the control of individual agents while that of investment shocks can be avoided by choosing not to purchase the productive asset. With this difference at play, we can distinguish risky from riskless investments so that agents face a nontrivial portfolio choice. We can then study not only how financial markets heterogeneity affects net foreign asset positions but also their composition.

Note that production is individually run and shocks are idiosyncratic: there are no aggregate shocks. Therefore, cross-country sharing of aggregate risks is not an issue here. Also notice that there is no aggregate accumulation of capital. For an extension with capital accumulation see Mendoza, Quadrini, and Ríos-Rull (2008).

Let $s_t \equiv (w_t, z_t)$ be the pair of endowment and investment shocks with Markov transition process denoted by $g(s_t, s_{t+1})$. Agents can buy contingent claims, $b(s_{t+1})$, that depend on the next period’s realizations of these shocks. Because there is no aggregate uncertainty, the price of one unit of consumption goods contingent on the realization of $s_{t+1}$ is $q_t^i(s_t, s_{t+1}) = g(s_t, s_{t+1})/(1 + r_t^i)$, where $r_t^i$ is the equilibrium interest rate.

Define $a_t$ as the end-of-period net worth before consumption. The budget constraint for an individual agent is:

$$ a_t = c_t + k_t P_t^i + \sum_{s_{t+1}} b(s_{t+1}) q_t^i(s_t, s_{t+1}), $$

(country, that is, there are only ‘aggregate’ shocks.)
and the agent’s net worth evolves according to:

\[ a(s_{t+1}) = w_{t+1} + k_t P_{t+1}^i + z_{t+1} k_t^ \nu + b(s_{t+1}). \] (2)

If asset markets were complete, i.e. without restrictions on the set of feasible claims, agents would be able to perfectly insure against all risks. However, there are market frictions and the set of feasible claims is constrained in each country. In particular, we assume that contracts are not perfectly enforceable due to the limited (legal) verifiability of shocks. Because of the limited verifiability, agents can divert part of their incomes from endowment and production, but they lose a fraction \( \phi^i \) of the diverted income. The parameter \( \phi^i \) characterizes the degree of enforcement of financial contracts in country \( i \). This is the only feature that differentiates the two countries.

We also assume that there is limited liability and agents cannot be excluded from the market after defaulting. Under these assumptions, Appendix B shows that contract enforceability imposes the following two constraints:

\[ a(s_n) - a(s_1) \geq (1 - \phi^i) \cdot \left[ (w_n + z_n k_t^\nu) - (w_1 + z_1 k_t^\nu) \right] \] (3)

\[ a(s_n) \geq 0 \] (4)

for all \( n \in \{1, ..., N\} \). Here \( n \) is the index for a particular realization of the two shocks with \( s_1 \) the lowest (worse) realization. The number of all possible realizations is \( N \).

The first condition requires that the variation in net worth, \( a(s_n) - a(s_1) \), cannot be smaller than the variation in income, scaled by \( 1 - \phi^i \). This constraint can also be written in
terms of the contingent claims. Using the definition of $a(s_{t+1})$ provided in (2), the constraint (3) can be rewritten as:

$$b(s_n) - b(s_1) \geq -\phi^i \cdot \left[ (w_n + z_n k^\nu_t) - (w_1 + z_1 k^\nu_t) \right]$$

(5)

When $\phi^i$ is positive, agents can choose unequal amounts of contingent claims, and therefore, they can get some insurance. If $\phi^i$ is sufficiently large, agents can achieve full insurance. When $\phi^i = 0$—implying that income can be diverted without losses—only non-state-contingent claims are feasible. Constraint (4) imposes that net worth cannot be negative. This follows from the assumption of limited liability.

A key assumption is that $\phi^i$ pertains to the country of residence of the agents, regardless of the geographic location of their assets. In particular, if asset markets are globally integrated, domestic agents can buy foreign productive assets and receive foreign income, but still their access to insurance is determined by the domestic, not the foreign $\phi$. This implies that the ability of an agent to divert investment incomes generated abroad depends on the legal environment of the country of residence.

This assumption is based on the idea that the verification of diversion requires the verification of individual consumption. Because individual consumption takes place in the country of residence, the institutional features of the country of residence are the ones that matter for enforcement. Section 5 explores the extent to which our results are robust to alternative assumptions about the residence or source nature of $\phi^i$.

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4One way to think about this assumption is that agents have the ability to repatriate the incomes earned abroad. Once the incomes are transferred back to the home country, the verifiability of these incomes is determined by the institutions at home.
2.1 Optimization problem and equilibrium

Let \( \{P^i_t, q^i_t(s_{\tau},s_{\tau+1})\}_{\tau=t}^{\infty} \) be a (deterministic) sequence of prices in country \( i \). With capital mobility these prices are equalized internationally, and therefore, an individual agent is indifferent about the domestic versus foreign location of the productive investment. We can then write the optimization problem of an individual agent as if he or she only buys domestic \( k \). Independently of the international capital mobility regime, this can be written as:

\[
V^i_t(s,a) = \max_{c,k,b(s')} \left\{ U(c) + \beta \sum_{s'} V^i_{t+1}(s',a(s')) g(s,s') \right\}
\]

subject to \((1), (2), (3)\) and \((4)\)

where we denote current ‘individual’ variables without subscript and next period ‘individual’ variables with the prime superscript. Notice that this is the optimization problem for any deterministic sequence of prices, not only steady states. This motivates the time subscript in the value function.

The solution to the agent’s problem yields decision rules for consumption, \( c^i_t(s,a) \), productive assets, \( k^i_t(s,a) \), and contingent claims \( b^i_t(s,a,s') \). Since in the equilibrium with capital mobility agents are indifferent about the location of the productive investment, we do not have to specify whether the holding of productive capital, \( k^i_t(s,a) \), is domestic or foreign. The decision rules determine the evolution of the distribution of agents over \( s, k \) and \( b \), which we denote by \( M^i_t(s,k,b) \).
Definition 1 (Financial autarky) Given the financial development indicator, $\phi^i$, and initial wealth distributions, $M^i_t(s,k,b)$, for $i \in \{1, 2\}$, an equilibrium without international mobility of capital is defined by sequences of: (i) agents’ policies $\{c^i_\tau(s,a), k^i_\tau(s,a), b^i_\tau(s,a,s')\}_{\tau=t}^\infty$; (ii) value functions $\{V^i_\tau(s,a)\}_{\tau=t}^\infty$; (iii) prices $\{P^i_\tau, r^i_\tau, q^i_\tau(s,s')\}_{\tau=t}^\infty$; (iv) distributions $\{M^i_\tau(s,k,b)\}_{\tau=t+1}^\infty$.

Such that: (i) the policy rules solve problem (6) and $\{V^i_\tau(s,k)\}_{\tau=t}^\infty$ are the associated value functions; (ii) prices satisfy $q^1_\tau = g(s,s')/(1+r^1_\tau)$; (iii) asset markets clear, $\int_{s,k,b} k^1_\tau(s,a)M^1_\tau(s,k,b) = 1, \int_{s,k,b,s'} b^1_\tau(s,a,s')M^1_\tau(s,k,b)g(s,s') = 0$ for each $i \in \{1, 2\}$ and $\tau \geq t$; (iv) the sequence of distributions is consistent with the initial distributions, the individual policies and the stochastic processes for the idiosyncratic shocks.

The definition of the equilibrium with globally integrated capital markets is similar, except for the prices and market clearing conditions (ii) and (iii). With financial integration there is a global market for assets and asset prices are equalized across countries. Therefore, condition (ii) becomes $q^1_\tau = g(s,s')/(1+r^1_\tau) = g(s,s')/(1+r^2_\tau) = q^2_\tau$ and $P^1_\tau = P^2_\tau$. Furthermore, asset markets clear globally instead of country by country. Therefore, the market clearing condition for the productive assets becomes $\sum_{i=1}^2 \int_{s,k,b} k^i_\tau(s,a)M^i_\tau(s,k,b) = 2$ and the market clearing condition for contingent claims becomes $\sum_{i=1}^2 \int_{s,k,b,s'} b^i_\tau(s,a,s')M^i_\tau(s,k,b)g(s,s') = 0$.

With capital mobility, the assets owned by a country are no longer equal to the assets located in the country, and hence NFA positions are generally different from zero. Consequently, since at equilibrium agents are indifferent about the location of the productive investment, only the ‘net’ share of the foreign productive asset is determined. The same holds for the
contingent claims. Therefore, the net foreign asset position of country $i$ is given by:

$$NFA^i_\tau = \int_{s,k,b,s'} b^i_\tau(s,a,s') g(s,s') M^i_\tau(s,k,b) + \int_{s,k,b} \left[ k^i_\tau(s,a) - 1 \right] P_\tau M^i_\tau(s,k,b)$$

The first term in the right-hand-side is the net position in ‘contingent claims.’ The second is the net position in ‘productive assets.’ We refer to the first term as bond position or international lending, when positive, and debt position or borrowing when negative.

### 2.2 Equilibria with and without capital mobility

This section characterizes the properties of the equilibrium with and without financial integration. To clarify the different roles played by endowment and investment shocks, we consider separately the cases with only endowment risks and with only investment risks.

#### 2.2.1 Endowment shocks only

Assume $z$ is not stochastic ($z = \bar{z}$), so that there are only endowment shocks. Denote by $\tilde{\phi}$ a sufficiently high value of the enforcement parameter so that (3) is not binding and hence markets are complete. With i.i.d. shocks, $\tilde{\phi} = 1$ suffices, while persistent shocks require $\tilde{\phi} > 1$. To show the importance of domestic financial development, we compare the limiting cases of complete markets ($\phi = \tilde{\phi}$) with the environment without state-contingent claims ($\phi = 0$). We first look at the autarky regime and then at the financially integrated regime.

When $\phi = \tilde{\phi}$, constraint (3) is not binding by assumption. Therefore, the first-order conditions of problem (6) with respect to $k$ and $b(w')$ are:

$$U'(c) = \beta (1 + r_1) U'(c(w')) + (1 + r_1) \lambda(w'), \quad \forall w'$$

(7)
where $\lambda(w')$ is the Lagrange multiplier associated with the limited liability constraint (4) and $R_{t+1}(k, \bar{z}) = (P_{t+1} + \nu \bar{z} k^{\nu-1})/P_t$ is the gross marginal return from the productive asset. Notice that $R_{t+1}(k, \bar{z})$ is decreasing in $k$.

Since in this case agents have complete insurance, condition (7) holds for any realization of $w'$, which implies that next period consumption $c(w')$ is the same for all $w'$. Moreover, conditions (7) and (8) imply $R_{t+1}(k, \bar{z}) = 1 + r_t$, so the marginal return on the productive asset is equal to the interest rate. Because $R_{t+1}(k, \bar{z})$ is strictly decreasing in $k$, this implies that all agents choose the same input of the productive asset, that is, $k = 1$. Given that the supply of the productive asset is fixed, total output is also fixed. We now establish that the full insurance autarky equilibrium must satisfy $\beta(1 + r_t) = 1$.

**Lemma 1** Under the financial autarky regime and $\phi = \bar{\phi}$ the interest rate and the price of the productive asset are constant and equal to $r = 1/\beta - 1$ and $P = \nu \bar{z}/r$ respectively.

**Proof 1** By way of contradiction, if $\beta(1 + r_t) \neq 1$, condition (7) implies that consumption growth of all agents is either positive or negative. This cannot be an equilibrium because aggregate output remains constant. Therefore, $r_t = 1/\beta - 1 = r$. Because all agents use the same units of the productive asset, $k = 1$, conditions (7) and (8) imply $(P_{t+1} + \nu \bar{z})/P_t = 1 + r$. The only stationary solution for this difference equation is $P_t = P_{t+1} = \nu \bar{z}/r$. Q.E.D.

Consider next the case of an economy in financial autarky but with $\phi = 0$. The enforceability constraint (3) imposes that $b(w_1) = \ldots = b(w_N) = b$, that is, assets cannot be state-
contingent. The first-order conditions are:

\[ U'(c) = \beta(1 + r_t) EU'(c(w')) + (1 + r_t) E\lambda(w') \] (9)

\[ U'(c) = \beta R_{t+1}(k, \bar{z}) EU'(c(w')) + R_{t+1}(k, \bar{z}) E\lambda(w') \] (10)

These conditions still imply that \( R_{t+1}(k, \bar{z}) = 1 + r_t \) and the input of the productive asset is the same for all agents. Thus, all agents receive the same investment income. However, the absence of state-contingent assets implies that the endowment risk cannot be insured and individual consumption is not constant. It varies with the realization of the endowment as in the standard Bewley (1986) economy. As it is known from the savings literature (see Huggett (1993), Aiyagari (1994) and Carroll (1997)), the uninsurability of the idiosyncratic risk generates precautionary savings and in the steady state \( \beta(1 + r) < 1 \). Formally,

**Lemma 2** Under the financial autarky regime and \( \phi = 0 \)., the interest rate satisfies \( r_t < 1/\beta - 1 \) and the steady state price is \( P = \nu \bar{z}/r \).

The proof is standard and uses convexity of marginal utility together with the fact that all households employ the same amount of productive asset.

Using these lemmas we can compare countries in financial autarky at different stages of financial development: The country with a lower degree of financial development \( (\phi = 0) \) has a lower interest rate and, at least in the steady state, a higher asset price than a more financially developed country.

Consider now the steady state equilibrium of an economy where there is perfect mobility of capital between country 1 (henceforth C1), characterized by \( \phi_1 = \bar{\phi} \), and country 2
(henceforth C2) characterized by $\phi^2 = 0$. In this case, the perfect substitutability of assets implies that their prices are equated across countries, and so are the world interest rate and the holdings of productive assets by all agents. Given that C1 has no need for precautionary savings while C2 does, the conflict gets resolved by households in C1 hitting the limited liability constraint (4). The following proposition formalizes this result.

**Proposition 1** Suppose that $\phi^1 = \bar{\phi}$ and $\phi^2 = 0$. In the equilibrium with financial integration, $r_t < 1/\beta - 1$ and C1 accumulates a negative NFA position but holds a zero net position in the productive asset.

**Proof 1** Appendix C.

This proposition holds only for the limiting cases of $\phi^1 = \bar{\phi}$ and $\phi^2 = 0$. However, we can infer the properties of the equilibrium for intermediate values of $\phi$ (i.e. for any case $0 \leq \phi^2 < \phi^1 < \bar{\phi}$). In general, lower values of $\phi$ increase precautionary savings and reduce the equilibrium interest rate. Therefore, once the capital markets are liberalized, the country with a lower value of $\phi$ accumulates a positive NFA position.

This point is illustrated in Figure 4. The figure plots the aggregate demand for assets (supply of savings) in each country as an increasing function of $r$. C1 has deeper financial markets ($\phi^1 > \phi^2$), and hence lower asset demand for each interest rate. Because the supply of the productive asset is fixed, aggregate net savings (in units of $K$) must be zero under autarky in each country. This requires a higher interest rate in C1 ($r^1 > r^2$).

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5 The asset demand curves in Figure 4 correspond to the well-known average asset demand curve from the closed-economy heterogeneous agents literature (e.g. Aiyagari (1994)). Average asset demand approaches infinity as the interest rate converges to the rate of time preference from below. This is because agents need an infinite amount of precautionary savings to attain a level of consumption that is not stochastic.
2.2.2 Investment shocks only

We now consider the case in which the productivity $z$ is stochastic while the endowment is constant at $w = \bar{w}$. This assumption allows us to distinguish debt instruments from risky investments such as FDI. As before, we compare equilibria under autarky and under financial integration for the limiting cases of $\phi = \bar{\phi}$ and $\phi = 0$.

The first-order conditions in autarky for an economy with $\phi = \bar{\phi}$ are:

$$U'(c) = \beta(1 + r_t)U'(c(z')) + (1 + r_t)\lambda(z'), \quad \forall z'$$  \hspace{1cm} (11)

$$U'(c) = \beta ER_{t+1}(k,z')U'(c(z')) + E\lambda(z')R_{t+1}(k,z')$$  \hspace{1cm} (12)

The first condition holds for all realizations of $z'$. Therefore, the next period’s consumption, $c(z')$, must be the same for all realizations of $z'$ (full insurance). Because next period’s consumption is not stochastic, conditions (11) and (12) imply that $ER_{t+1}(k,z') = 1 + r_t$.

Therefore, there is no marginal premium for investing in the productive asset and $k$ is the same for all agents. Thus, Lemma 1 also applies here and the only equilibrium is characterized by $\beta(1 + r_t) = 1$. Intuitively, because agents can insure perfectly against the idiosyncratic risk, there are no precautionary savings and in equilibrium the interest rate must be equal to the intertemporal discount rate.

In an economy with $\phi = 0$, the incentive-compatibility constraint (3) imposes that $b(z_1) =$
... = b(z_N) = b, that is, claims cannot be state contingent. The first-order conditions are:

\[ U'(c) = \beta (1 + r_t) E[U'(c(z'))] + (1 + r_t) E[\lambda(z')] \]  
(13)

\[ U'(c) = \beta E[U'(c(z'))R_{t+1}(k, z')] + E[\lambda(z')R_{t+1}(k, z')] \]  
(14)

Lemma 2 also applies here, hence, the equilibrium interest rate is smaller than the intertemporal discount rate. The main difference with the case of endowment shocks is that now there is a marginal risk premium for the risky asset. In particular, if the borrowing limit is not binding, conditions (13) and (14) yield the standard equation for the risk premium:

\[ ER_{t+1}(k, z') - (1 + r_t) = -\frac{Cov(R_{t+1}(k, z'), U'(c(z')))}{EU'(c(z'))} \]

which is positive as long as \( U'(c(z')) \) is negatively correlated with \( R_{t+1}(k, z') \).

Now suppose that the two countries become financially integrated. The first country has \( \phi^1 = \bar{\phi} \) and the second \( \phi^2 = 0 \). The following proposition characterizes the steady state.

**Proposition 2** Suppose that \( \phi^1 = \bar{\phi} \) and \( \phi^2 = 0 \). In the steady state with financial integration, \( r < 1/\beta - 1 \). C1 has a negative NFA position but a positive position in the productive asset. The average return of C1’s foreign assets is larger than the cost of its liabilities.

**Proof 2** Appendix C.

The proposition shows that, with investment shocks, countries with deeper financial markets invest in foreign (high return) assets and finance this investment with foreign debt. In the
particular case in which the most developed country has \( \phi^1 = \bar{\phi} \), Proposition 1 guarantees that this country ends up with a negative NFA position. The higher return derives from the decreasing returns property of the production function. This generates a surplus that compensates the agent's managerial capital.

Consider now the general case with \( 0 \leq \phi^2 < \phi^1 < \bar{\phi} \). C1 has a greater (yet imperfect) ability to insure than C2 and hence it will still buy some of C2’s risky asset,\(^6\) even if it is not always true that it accumulates a negative NFA position. Moreover, the imperfect insurance generates a marginal risk premium even for C1, which is the rationale for the higher return that C1 collects from its foreign investments relative to the cost of its foreign liabilities.

### 2.2.3 Endowment and investment shocks

With both endowment and investment shocks, the first-order conditions are also given by (11)-(14). The only difference is that next period’s consumption depends on both shocks, that is, \( c(s') \). The autarky equilibria are also characterized by Lemmas (1) and (2). The following proposition characterizes the equilibrium under global financial integration.

**Proposition 3** Suppose that \( \phi^1 = \bar{\phi} \) and \( \phi^2 = 0 \). In the steady state with perfect capital mobility, \( r < 1/\beta - 1 \). C1 has a negative NFA position but a positive position in foreign productive assets. The average return of C1 foreign ownership is bigger than the cost of its liabilities.

**Proof 3** Same as in Proposition 2.

\(^6\)The concavity of the production function is crucial for this result. With a linear technology, as in Angeletos (2007), the most developed country would own all of the world’s risky assets. As a result, the less developed country would have less incentives to save.
This is a restatement of proposition 2 for the case with both shocks. In the extreme case with $\phi^1 = \bar{\phi}$ and $\phi^2 = 0$, the addition of endowment shocks does not change the main properties of the equilibrium. In the general case, the interest rate is smaller than the intertemporal discount rate and C1 acquires a positive net position in foreign productive assets, but its NFA position is not necessarily negative. This depends on the relative importance of the two shocks. As long as the endowment shock is sufficiently large, however, C1 will hold a negative NFA position.

3 The general model

We now extend the basic setup presented in the previous section along two dimensions: (1) cross-country diversification of the investment risk; (2) differences in the economic size of countries. We also generalize the model to include any finite number of countries $I \geq 2$. These features allow for a richer quantitative analysis.

We introduce international risk diversification by assuming that managerial capital is now divisible across countries. Each agent is endowed with one unit of this capital. Denoting by $A_{j,t} \in [0, 1]$ the allocation of an agent’s managerial capital in country $j$, the total (worldwide) production at time $t+1$ of the agent is equal to:

$$y_{t+1} = \sum_{j=1}^{I} z_{j,t+1} A_{j,t}^{1-\nu} k_{j,t}^{\nu}, \quad \text{with} \quad \sum_{j=1}^{I} A_{j,t} = 1$$

The variables $z_{j,t+1}$ and $k_{j,t}$ are, respectively, the project-specific idiosyncratic shock and the input of the productive asset in country $j$.

The divisibility of the managerial capital is the most important extension. In the basic
model, each agent had to choose between allocating all the managerial capital in C1 ($A_{1,t} = 1$ and $A_{2,t} = 0$) or in C2 ($A_{1,t} = 0$ and $A_{2,t} = 1$). In contrast, now agents can allocate any fraction $A_{j,t} \in [0, 1]$ in each of the $I$ countries. This has two important implications. First, as long as the shocks $z_{j,t+1}$ are imperfectly correlated, financial integration allows agents to diversify investment risk across countries.\footnote{We are implicitly assuming that agents do not benefit from allocating their managerial capital to multiple operations within each country. The only diversification gains arise from cross-country diversification. Without loss of generality, we can interpret $z_{j,t+1}$ as the residual risk after exploiting all the diversification margins available within each country.} Second, while in the basic model only the net foreign position in the productive asset was determined at equilibrium, now the gross positions are also determined.

Let $s_t \equiv (w_t, z_{1,t}, \ldots, z_{I,t})$ be the endowment and investment shocks and $g(s_t, s_{t+1})$ their transition probabilities. As in the basic model, agents can buy contingent claims, $b(s_{t+1})$. The price of one unit of consumption goods contingent on the realization of $s_{t+1}$ is $q_t^i(s_t, s_{t+1}) = g(s_t, s_{t+1})/(1 + r_t^i)$, where $r_t^i$ is the equilibrium interest rate in country $i$.

Given the end-of-period net worth before consumption, $a_t$, the budget constraint is:

$$a_t = c_t + \sum_{j=1}^{I} k_{j,t} P_t^j + \sum_{s_{t+1}} b(s_{t+1}) q_t^i(s_t, s_{t+1}),$$

(15)

and net worth evolves according to:

$$a(s_{t+1}) = w_{t+1} + \sum_{j=1}^{I} \left[ k_{j,t} P_t^j + z_{j,t+1} A_{1,t}^{1-\nu} k_{j,t}^\nu \right] + b(s_{t+1}).$$

(16)

The features of the financial environment are the same as in the basic model: shocks are not verifiable and agents can divert part of the incomes from endowment and production,
both domestic and abroad, but in the process they lose a fraction $\phi^i$ of the diverted income. As before $\phi^i$ pertains to the ‘residence’ of agents as opposed to the ‘source’ of the income.

Following the same steps of Appendix B, the enforcement of financial contracts imposes the following constraints:

$$a(s_n) - a(s_1) \geq (1 - \phi^i) \cdot \left[ w_n - w_1 + \sum_{j=1}^{I} (z_{j,n} - z_{j,1}) A_{j,t}^{1-\nu} k_{j,t}^{\nu} \right]$$  \hspace{1cm} (17)

$$a(s_n) \geq 0$$  \hspace{1cm} (18)

for all $n \in \{1, ..., N\}$, where $N$ is the number of all possible realizations of endowment and investment shocks and $s_1$ is the lowest (worse) realization.\(^8\)

There is a difference with the previous constraint (3). Now individual agents have both differentiated domestic and foreign incomes from productive investments. Before, all income from productive investments was subject to the same shock and hence could not be distinguished.

The last extension of the model relates to the economic size of countries participating in world capital markets. This is important for the quantitative properties of the model. Obviously, large imbalances for $C_1$ can arise only if the economy of $C_2$ is relatively large. In our model, differences in economic size could derive from differences in population and/or in productivity, that is, in the average value of the endowment $w$ and in the per-capita supply of the productive asset $k$. However, for the properties we are interested in, what matters are differences in the aggregate economic size of countries, independently of the factors that

\(^8\)A generic $s_n$ contains $1 + I$ elements: the endowment shock $w_n$ and the realizations of the idiosyncratic shocks in each of the $I$ countries, that is, $z_{j,n}$ for $j = 1, ..., I$. 

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account for them. Therefore, to simplify the analysis, we assume that differences in economic size derive only from differences in population.

We denote by $\mu^i$ the population share of country $i$ and continue to assume that the per-capita endowment $w$ and the per-capita domestic supply of the productive asset are the same in all countries. This extension does not alter the analytical results of Section 2.

3.1 Optimization problem and equilibrium

Given deterministic sequences of prices $\{\{P^j_\tau, q^j_\tau(s_{\tau}, s_{\tau+1})\}_{\tau=t}^{\infty}\}_{j=1}^{I}$, a single agent’s problem in country $i$ can be written as:

$$V^i_t(s, a) = \max_{A, k, b(s')} \left\{ U(c) + \beta \sum_{s'} V^i_{t+1}(s', a(s')) g(s, s') \right\}$$

subject to (15), (16), (17), (18),

$$A_j \in [0, 1], \sum_{j=1}^{I} A_j = 1.$$

The definition of the autarky equilibrium is equivalent to the definition provided for the basic model. This is because all the extensions introduced in this section matter only for the regime with capital mobility. With capital mobility the individual states variables are given by $(s, A, k, b)$. The variable $s$ is an $I + 1$- dimensional vector containing the realization of the endowment plus the realizations of the investment shocks in each of the $I$ countries. The variables $A$ and $k$, without subscripts, are $I$- dimensional vectors containing, respectively, the allocation of managerial capital and the ownership of productive assets in each of the $I$
countries. Finally, the realized claim $b$ remains one-dimensional as in the simpler version of the model. The definition of the equilibrium with capital mobility is as follows.

**Definition 2 (Financial integration equilibrium)** Given the financial development indicator, $\phi^i$, and initial wealth distributions, $M^i_t(s, A, k, b)$, a general equilibrium with international capital mobility is defined by sequences of: (i) individual policies $\{c^i_t(s, a), b^i_t(s, a, s'), \{A^i_{j,\tau}(s, a), k^i_{j,\tau}(s, a)\}\}_j$, (ii) value functions $\{V^i_t(s, a)\}_{\tau=t}$; (iii) prices $\{\{P^i_j, r^i_j, q^i_j(s, s')\}\}_{j=1}^I$, (iv) distributions $\{M^i_t(s, A, k, b)\}_{\tau=t+1}$, such that: (i) the policy rules solve problem (19) with $\{V^i_t(s, a)\}_{\tau=t}$ as associated value functions; (ii) prices satisfy $q^i_j = g(s, s'_j)$; (iii) the global markets for the productive assets of each country clear,

$$\sum_{i=1}^I \int_{s,A,k,b} k^i_{j,\tau}(s, a)M^i_t(s, A, k, b) = \mu^j$$

for $j = 1, ..., I$; (iv) the worldwide market for contingent claims clears,

$$\sum_{i=1}^I \int_{s,A,k,b,s'} b^i_t(s, a, s')M^i_t(s, A, k, b)g(s, s') = 0;$$

(v) the sequence of distributions is consistent with the initial distributions, the individual policies and the idiosyncratic shocks.

It is important to emphasize that, in general, the market-clearing conditions for productive assets do not lead to the equalization of their prices, that is, $P^i_t$ is not equal to $P^j_t$ for $i \neq j$. This is because, unless the shocks are perfectly correlated across countries, agents are not indifferent about the composition of their portfolios of productive assets. This is in contrast to the equalization of the interest rates: all that matters for the choice of the contingent
claims are their returns, which are determined by the interest rate.

It is possible to derive some analytical results for this general model that are similar to those of the basic model. The optimality conditions are analogous, except that now we also have the conditions characterizing the optimal cross-country allocation of managerial capital. These conditions are \( \frac{k_i}{A_i} = \frac{k_j}{A_j} \) for all \( j = 1, ..., I \). If we consider the case in which \( I = 2 \), \( \phi^1 = \bar{\phi} \), \( \phi^2 = 0 \), we can prove that the same properties shown in Section 2.2 apply to the general model. This is obvious because, with \( \phi^1 = \bar{\phi} \), agents in C1 do not require a marginal premium on the productive investments. Hence, they are indifferent about the domestic and foreign allocation of the managerial capital.

4 Quantitative analysis

We now turn to the quantitative implications of the model. The goal is to compare stationary equilibria under financial autarky and perfect capital mobility and to study the transitional dynamics from the former to the latter. Financial globalization is introduced as a once-and-for-all unanticipated regime change. We use a baseline scenario with \( I = 2 \). The first country, C1, is representative of the United States. The second country, C2, aggregates all remaining countries. Later on we add a third country to separate emerging economies from industrial countries other than the United States.

4.1 Calibration

We set the population size of country 1 to \( \mu^1 = 0.3 \) so as to match the U.S. share of world GDP, which is about 30 percent. The stochastic endowment takes two values given by \( w = \bar{w}(1 \pm \Delta_w) \), with symmetric transition probability matrix. The investment shock also
takes two values, \( z = \bar{z}(1 \pm \Delta z) \) but it is assumed to be iid. Interpreting \( w \) as labor income and \( y \) as net capital income, we set \( \bar{w} = 0.85 \) and then we parameterize the production function so that \( y = \bar{z}k^\nu = 0.15 \). Because per-capita assets are \( k = 1 \), this requires \( \bar{z} = 0.15 \). The share of labor is higher than the typical value of \( 2/3 \) because it is in terms of net income, that is, income net of depreciation. The return to scale parameter is set to \( \nu = 0.75 \) implying a share of managerial capital of \( 0.25 \). This generates managerial rents as a fraction of total net income that are relatively small, about 3.75%.

For the calibration of the stochastic process of the endowment we follow recent estimates of the U.S. earnings process and set the persistence probability to \( 0.95 \) and \( \Delta w = 0.6 \). These values imply that log earnings have an autocorrelation coefficient of \( 0.9 \) and a standard deviation of \( 0.30 \), which are in the ranges of values estimated by Storesletten, Telmer, and Yaron (2004). The variation in the investment shock is set to \( \Delta z = 2.5 \). This implies that the return on productive assets fluctuates between -6\% and 14\%. We take this as an approximation to the volatility of firm-level returns. The correlation in productivity shocks across the different projects is set to zero. Therefore, there is wide scope for international diversification of investment risks.

Next we choose the parameters of the financial structure. Several indicators, such as those reported in Figure 1, suggest that financial markets are significantly different across countries. However, it is difficult to derive a direct mapping from these indicators to the actual values of \( \phi^i \). Given these difficulties, we take a pragmatic approach. We begin by assigning some values and then we conduct a sensitivity analysis. We start with \( \phi^1 = 0.35 \)

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9Because the capital income generated by productive activities is 15% of total net income and the rents are about 25% of capital income, the share of rents in total net income are about \( 0.15 \times 0.25 = 0.0375 \). This is close to Rotemberg and Woodford (1995) 3\% estimate of the profit rate in U.S. firm-level data, although the two estimates are not directly comparable.
and $\phi^2 = 0$. Thus, contingent claims are partially available in country 1 and unavailable in country 2. It is also worth observing that there is a certain degree of equivalence between cross country differences in $\phi$'s and differences in the volatility of idiosyncratic shocks. The assumption that $\phi^1 = 0.35$ implies that the equilibrium allocation in country 1 is similar to the one that would prevail if contingent claims were not available (i.e. $\phi^1 = 0$) but the volatilities of all shocks were 35 percent lower than in country 2.

The utility function is CRRA with the coefficient of risk aversion set to $\sigma = 2$. The intertemporal discount factor is $\beta = 0.925$. With this discount factor, the wealth-to-income ratios in the steady state with capital mobility are 2.86 in country 1 and 3.45 country 2. The worldwide wealth-to-income ratio is about 3.3. This is higher than the typical number of 3 because our income is net of depreciation. The description of the computational procedure is provided in Appendix D.

4.2 Results

Individual policies. Figure 5 plots the individual decision rules as a function of the net worth $a$, for each value of the endowment $w$, in the steady state with capital mobility.\(^{10}\) Three variables are plotted: the value of all contingent claims, $\sum_{s'} b(s')q(s,s')$, the value of productive assets purchased in C1, $k_1 P_1$, and the value of productive assets purchased in C2, $k_2 P_2$.

\[^{10}\text{The current realization of the endowment is a state variable because endowment shocks are persistent. The investment shock } z \text{ can be ignored as state variable because it is } iid.\]
The net position in contingent claims increases with net worth: it is negative for poorer agents and positive for richer agents. The total position in risky investments also increases with $a$. For the range of $a$ plotted in the figure, all agents choose to buy productive assets in both countries. However, as agents become wealthier, they allocate a larger proportion in C2.

The intuition for this pattern can be described as follows. First we should observe that, due to the different economic size of the two countries, the equilibrium price of the productive asset in C2 is smaller than in C1. Suppose on the contrary that the two prices were the same. Because investment shocks are uncorrelated across the different projects, when the prices of the productive assets are the same, investors would allocate an equal share of their investments between the domestic and the foreign projects. Therefore, the total demand for the productive asset in C1 would be exactly equal to the total demand for the productive asset in C2. However, because C2 is larger than C1, the supply in C1 is smaller than in C2. This generates a decline in the price of the productive asset in C2 relatively to the price in C1. The lower price of the productive asset in C2 implies that the expected return from investing in C2 is higher than in C1. Given CRRA utility, as agents become wealthier they assign higher weight on returns and less on risk. Therefore, they value less the benefits from diversification and invest more in C2.

**Aggregate variables.** The first panel of Table 1 reports the equilibrium prices and positions that prevail in the steady state equilibria under autarky and perfect capital mobility. Under capital mobility C1 accumulates a net positive position in productive assets but a much larger negative position in contingent claims (bonds).
C1’s debt and foreign risky asset positions are -89 and 37 percent of its domestic income respectively. As a result, the NFA position is negative and quite large, -51 percent of income. Hence, the model is consistent with the data in predicting that the most financially developed country accumulates a substantial negative NFA, chooses a riskier portfolio and experiences a reduction in the risk-free rate relative to autarky. However, the model overstates the adjustment observed so far in the U.S. economy. As of 2004, the net positions in debt and risky assets were -32 and 9 percent of the U.S. GDP respectively, and the total NFA position was -24 percent of GDP. Note also that the changes in asset prices and interest rates that support these large changes in asset holdings are small.

The model also predicts that financial globalization leads to an increase in the gross holdings of foreign risky assets for all countries (see Figure 5). As Lane and Milesi-Ferretti (2007) noted, this is a salient feature of the financial globalization era (see bottom panel of Figure 2).

A feature of the equilibrium is that the average return from the productive assets is greater than the interest rate. This derives from two mechanisms. First, because of decreasing returns, there is a surplus that compensates managerial capital. Therefore, even if the marginal return on the productive asset is equal to the interest rate, total production is bigger than the opportunity cost of the investment. The second mechanism relates to the investment risk. Because of this risk, investors require a marginal premium over the interest rate which further increases the average return.

\[\text{Decreasing returns are important for this feature of the model and for supporting a well-defined portfolio choice.}\]
Consider now the special versions of the model with only endowment or investment shocks. The second and third panels of Table 1 report the steady states values of some key variables in these cases. With endowment shocks only (Panel B), the model can produce a large negative NFA position in C1 (of roughly -38 percent of domestic income). However, with only endowment shocks, the model cannot explain the observed shift in the composition of the portfolios of foreign assets. By contrast, the setup with only investment shocks (Panel C) does produce a portfolio for C1 characterized by a negative debt position and a positive position in risky assets. The total NFA position, however, is not very large. This is because, as C1 takes a greater position in risky assets, it faces greater risk inducing higher savings.

In summary, these results show that by combining endowment and investment shocks, we can capture both features of the U.S. international asset position: large net foreign liabilities and a portfolio composition tilted toward high-return assets.

**Transition after liberalization.** Figure 6 plots the transitional dynamics from autarky to full financial integration for several aggregate variables. The top left panel shows that the decline in net foreign assets in C1 is a slow, gradual process that takes about 30 years. The current account drops to a deficit of almost 4 percent of domestic income on impact and remains in deficit for many periods until it converges to zero in about 50 years.

The deterioration of the current account in C1 is not as gradual as in the U.S. data. In our results, however, the pattern of a large initial deficit followed by gradual recovery is a consequence of the assumption that capital markets are fully integrated overnight. In reality, financial integration has been a gradual process (see Figure 2). With gradual integration the model would have displayed current account dynamics more in line with the U.S. data.
Figure 6 also plots the dynamics for the components of NFA and the current account. Immediately after financial integration, C1 purchases a large quantity of foreign productive assets financed with foreign debt. Despite the negative NFA position, C1 receives initially positive net factor payments from abroad due to the higher return on the productive assets. These payments, however, are more than compensated by negative net exports and thus the country experiences current account deficits until it reaches the new steady state.

**Normative implications.** We examine next the normative implications of the model. We are interested in answering two questions. First, is financial integration welfare enhancing for the participating countries? Second, how are the welfare effects distributed among the population of each country?

The model features three mechanisms by which financial integration can affect welfare. First, by investing in both countries households can diversify the investment risks. Second, countries can specialize in more (C1) or less (C2) risky activities. Third, financial integration can benefit C1 citizens and hurt C2 residents because its effects on asset prices cause capital gains and losses and changes in the rate of interest (see Figure 6.)

Figure 7 plots the welfare gains (or losses if negative) from financial integration as a function of individual net worth, \( a \), and endowment, \( w \), when the reform is introduced. These welfare gains are computed as the percentage increase in consumption in the autarky steady state that makes each individual agent indifferent between remaining in autarky and shifting to the regime with financial integration. The figure also shows, for each country,
the distribution of agents over net worth in the autarky steady state. This is the initial
distribution when the international capital markets are liberalized.

[Place Figure 7 here]

In C1 all agents gain from liberalization and the gains are especially large for agents with
lower initial wealth. For these agents, the gains derive from all the reasons described above,
and in particular from the reduction in the interest rate. As shown in the bottom-left chart
of Figure 7, poorer agents are initially net borrowers, and therefore, they benefit from a
reduction in the interest rate. Richer agents, instead, are net lenders and they are hurt by
lower interest rates.

The increase in the interest rate relative to autarky in C2 affects negatively the welfare
of its poorer residents because they are net borrowers. These effects are large and the global
effect is a reduction in their welfare. Richer residents in C2 experience overall an increase in
welfare.

We aggregate the individual welfare effects using a social welfare function that weights
each agent’s utility equally. The aggregate welfare effects are measured by the same percentage
increase in the consumption of all agents in the autarky steady state that makes the value
of the aggregate welfare equal to the value in the regime with financial integration. We find
that C1 gains about 2.6 percent of aggregate consumption while C2 loses 0.27 percent.
4.3 Sensitivity to the cross-country correlation of shocks

Table 2 reports the steady state statistics under autarky and financial integration for correlated cross-country investment shocks. Panel A assumes a correlation of 0.5, which reduces the gains from international diversification of investment, and in Panel B the correlation is 1, which completely eliminates such gains.\textsuperscript{12}

[Place Table 2 here]

While the table shows a reduction in the absolute value of the NFA position of C1, such position is still very large. The increase in the correlation of shocks also increases the two components of the NFA position in absolute value, since the gains of specialization are now larger.

The ability to diversify the investment risk is important for welfare. As we increase the cross-country correlation of shocks, and hence reduce the ability to diversify the investment risk, the welfare gains from international capital markets integration become smaller. As a result, C1’s gain falls and C2’s loss rises.

5 Residence versus source based enforcement

The analysis conducted so far was based on the assumption that the enforcement parameter $\phi$ is ‘residence based’, \textit{i.e.} it depends on the country of residence of the agents, independently of whether their incomes are generated at home or abroad, rather than ‘source based’, \textit{i.e.} it depends on where the incomes are generated. Such assumption is based on the view that the\textsuperscript{12}International output correlations are typically in the 0.4-0.7 range, but the relevant correlations to match with the model should be measured at the level of individual incomes, not aggregate output.
ability to verify diversion requires the verification of individual consumption which uses the resident’s country legal system. We now explore environments with alternative assumptions about the residence or source nature of the enforcement of contracts. We consider four alternative scenarios with results reported in Table 3. In all the experiments, we use the same values of $\phi$ as in the baseline calibration, that is, $\phi^1 = 0.35$ and $\phi^2 = 0$.

In panel A the enforcement of contracts for residents of C1 remains as in the baseline model, that is, $\phi^1$ applies to both foreign and domestic incomes. Residents of C2 are bound by $\phi^2$ for incomes earned at home and by $\phi^1$ for incomes earned abroad. Therefore, C2 residents use the legal system of C1 for incomes earned abroad. The enforcement constraint for C2 becomes,

$$a(s_n) - a(s_1) \geq (1 - \phi^2) \cdot \left[ w^n - w^1 + (z^n_2 - z^1_2)A_{2,t}^{1-\nu}k_{2,t}^{\nu} \right] + (1 - \phi^1)(z^n_1 - z^1_1)A_{1,t}^{1-\nu}k_{1,t}^{\nu}. \quad (20)$$

Panel B reverses the situation, C1 residents can use their country’s legal system for activities carried out domestically but they have to use the legal system of C2 for incomes earned abroad. Residents of C2 use their own legal system for all economic activity. Panel C considers the situation where the enforcement is in part source-based and in part residence-based for the residents of both countries. More specifically, the foreign incomes earned by the residents of both countries are enforced according to $\bar{\phi} = (\phi^1 + \phi^2)/2$. This implies that agents in C1 get less insurance on foreign earned incomes than on domestic incomes but still greater than the insurance available to residents of C2. Similarly, C2 agents can get better insurance on incomes earned abroad but not as good as the C1 residents. Lastly, Panel D considers the case in which enforcement is fully source-based in both countries.
The first three panels of Table 3 show that C1 accumulates a large negative NFA asset position and keeps a positive position in productive assets. Therefore, even with partial residence based enforcement, C1 continues to have a positive position in productive assets together with a negative NFA. In the last panel where enforcement is fully source-based, however, the net position in productive assets becomes negative.

6 Alternative forms of financial development: Industrialized versus emerging economies

The only form of financial heterogeneity considered so far derives from cross-country differences in the parameter $\phi$. In this section we consider a second form of financial heterogeneity captured by differences in the liability constraint (condition (4)). This constraint can be written more generally as $a(s_n) \geq a^i$ where $a^i$ is a parameter that differs across countries. Hence, financial development is now captured by differences in $\phi^i$ and $a^i$.

By adding a third country and characterizing financial heterogeneity in terms of both, $a$ and $\phi$, we can replicate the main features of the composition of foreign assets observed separately for the U.S., other industrialized countries and emerging economies. Before adding a third country, we examine how the properties of the model change with different $\phi$’s and/or $a$’s in the two-country setup.

Table 4 compares steady states under autarky and financial integration for different combinations of $\phi$ and $a$. Panel A assumes that both countries have the same $\phi$ but C1 is still more financially developed because it has a lower value of $a$. Panel B allows C1 to be
more financially developed in both dimensions, higher $\phi$ and lower $a$.

[Place Table 4 here]

Independently of whether financial heterogeneity derives from differences in $\phi$ or $a$, C1 ends up with a large negative NFA position. There are important differences, though, in the composition of NFA. In Panel A, where the differences are only in $a$, C1 has also negative net holdings of the productive assets.\textsuperscript{13} In Panel B, with differences in $\phi$, C1 takes a positive net position in productive assets.

These results indicate that cross-country differences in $\phi$ are needed in order to generate a situation in which the United States accumulates a negative NFA position and a positive position in high-return assets. Differences in $a$ cannot yield this outcome by themselves because lower values of $a$ decrease the propensity to save but do not change the propensity to take investment risks.

6.1 A three-country model

It is reasonable to argue that the United States and other industrial countries do not differ much in the institutional and technological environment that allows for the insurance of income risks. Yet, the evidence reviewed in the Introduction shows that the development of non-bank financial intermediation has progressed more in the United States, and this is also consistent with the higher ratio of domestic credit to the private sector to GDP of the U.S. compared to other industrialized countries.\textsuperscript{14} This suggests that the differences in

\textsuperscript{13}This is due to the lower prices of foreign assets.

\textsuperscript{14}According to the World Bank’s \textit{World Development Indicators}, in 2004 domestic credit to the private sector was 191 percent of GDP in the United States v. 136 percent for the other G7 countries and 122 percent.
financial markets between the U.S. and other industrial countries are more likely to derive from differences in \( a \) than in \( \phi \). On the other hand, the financial markets differences between the United States and emerging economies, where the ability to insure risks is much weaker and the volume of credit is much lower, are likely to derive from both, \( a \) and \( \phi \).

To capture these ideas, we extend the model to study the implications of financial integration among three countries or regions: the United States (C1), other developed countries (C2) and emerging economies (C3). Based on the above discussion, we assume that C1 differs from C2 only in \( a \) while it differs from C3 in both \( \phi \) and \( a \). We set \( \phi = (0.5, 0.5, 0.) \) and \( a = (-1, 0, 0) \).\(^{15}\)

We capture the differences in the economic size of the three countries by setting relative population sizes to \( \mu = (0.3, 0.5, 0.2) \). As explained earlier, by setting the population share of emerging economies to 0.2 we capture the fact that these economies contribute about 20 percent of the world GDP.

Except for the parameters of the financial structure and relative population, all other parameters are as in the baseline parametrization. The key steady-state variables are reported in Table 5.

---

\(^{15}\)While it is difficult to obtain direct evidence about the availability of insurance against income risks, there are some studies suggesting that insurance is smaller in emerging economies compared to developed countries, even if only for regional instead of individual shocks. For example, Xu (2008) finds that there is less consumption risk-sharing across Chinese provinces than across US states and Canadian provinces, and concludes that “Chinese households would be willing to pay dearly to insure their consumption against idiosyncratic shocks.” In the same vein, Kim, Kim, and Wang (2006) estimate the degree of consumption risk sharing among 10 East Asian countries and find that about 80 percent of the cross-sectional variation of GDP is not smoothed within the region. Compared to the OECD countries, the degree of risk sharing achieved is significantly lower and the potential gains are larger. An implication of the lower \( \phi \) in emerging economies under autarky is that the risk free interest rate is lower. In this regard, Bailey (1994) reports that in the early stages of China’s financial opening, there were A shares targeted at Chinese savers and B shares for non-Chinese. Type B shares were sold at a large discount, indicating that the internal rate of return was much lower for Chinese households.
The foreign asset structure of the three countries is broadly consistent with the asset structure shown in Figure 3 for the U.S., other industrialized countries and emerging economies. In particular, under financial integration the other industrialized countries (C2) have a very similar position in risky assets as the U.S. (C1). However, the NFA position is significantly smaller compared to C1. On the other hand, C3, which represents the emerging economies, has a positive NFA position and a negative net position in risky assets. The large increase in net bond holdings suggests that, if the foreign bonds are held by official institutions, the model can explain the recent surge in the foreign reserves of emerging economies.

6.2 Adding differences in growth and income volatility

Our model is robust in predicting that, as long as there are differences in domestic financial markets between industrialized and emerging economies, financial globalization may result in the latter becoming net suppliers of funds to the former. In making this case we abstracted from two other important dimensions in which emerging economies differ from industrialized countries: growth rates and incomes volatility.

Growth differences can be important because, as predicted by the standard neoclassical open-economy model, countries experiencing faster growth (emerging economies) should borrow from slow-growing countries (industrialized economies). However, recent trends seem to suggest the opposite (see, for example, Gourinchas and Jeanne (2007)).

The prediction of the neoclassical model about the flow of capital for fast growing countries is an unavoidable consequence of CRRA preferences. Ignoring uncertainty, the Euler equation
reads \((c_{t+1}/c_t)^{\sigma} = \beta(1+r_t)\). Faster growth in consumption before financial integration implies a higher value in the left-hand-side term of the Euler equation, which in turn implies a higher interest rate. As a result, when countries experiencing faster than average growth become financially integrated, their interest rates converge to a lower ‘world’ interest rate and save less.

If we abstract from heterogeneity in domestic financial markets, our model shares the same features of the neoclassical model. However, once we introduce financial markets differences we have two opposing effects. The higher growth of emerging economies induces these countries to save less while the lower development of their financial markets induces higher savings. So ultimately, which mechanism dominates depends on the relative importance of ‘growth differences’ versus ‘financial differences.’

In addition to growth, another important difference between industrialized and emerging economies is that the latter are, typically, countries that are experiencing significant structural changes, which are often associated with greater uncertainty at the individual level.\(^{16}\) Therefore, if we want to capture the differences between industrialized and emerging economies that are relevant for savings, we should allow for three sources of heterogeneity: financial markets development, economic growth and income volatility.

We add heterogeneity in growth and income volatility to the three-country model examined above. An easy way to capture differences in growth rates is to assume that countries have different discount rates. If \(\beta\) is the discount factor for industrialized countries and the growth

---

\(^{16}\)An indicator of this is that inequality tends to increase during phases of rapid growth. See Khan and Riskin (2001) and Naughton (2007). Also, several emerging economies have experienced sudden stops after entering the global financial markets. The role played by differences in the volatility of risk for the accumulation of foreign assets or reserves has also been explored in Durdu, Mendoza, and Terrones (2009) and Carroll and Jeanne (2008).
rate differential between emerging and industrialized countries is $1 + g$, then the discount factor of emerging countries is $\tilde{\beta} = \beta/(1 + g)^\sigma$. With an annual growth differential of 3.5 percent, and given the baseline parametrization $\beta = 0.925$ and $\sigma = 2$, the discount factor for C3 is $\tilde{\beta} = 0.925/1.035^2 = 0.863$. In this case, if C1 and C2 grow at about 2 percent per year, emerging countries (C3) grow at 5.5 percent per year. To account for the higher uncertainty faced by agents in emerging economies, we assume that the standard deviations of endowment and investment shocks in C3 are 50 percent higher than in C1 and C2.

[Place Table 6 here]

Table 6 reports the steady state statistics. Even if C3 grows faster than the other two countries, the combination of greater uncertainty and lower financial development induces agents in C3 to save more. As a result, C3 accumulates a positive NFA position and the composition of its portfolio is tilted toward less risky and less profitable assets. In short, our key findings seem robust to the introduction of differences in growth and incomes volatility.

7 Conclusion

This paper shows that international financial integration can lead to large and persistent global imbalances when countries differ in the degree of domestic financial development. Financial integration induces countries with deeper financial markets to reduce savings and accumulate a large stock of net foreign liabilities in a long and gradual process. Financial heterogeneity also affects the composition of the portfolio of net foreign assets. Countries with deeper financial markets borrow heavily from abroad and invest in high-return foreign risky
assets. These patterns are consistent with the features of the global external imbalances observed since the beginning of the 1980s. The model can generate these patterns as the outcome of financial integration in a world where the development of domestic financial markets is the only source of cross-country heterogeneity.

The main implications of our analysis proved to be robust to: (a) introducing alternative forms of financial development; (b) allowing for international diversification of individual risks; (c) considering residence- or source-based enforcement of contracts; (d) combining domestic financial heterogeneity with relatively large differences in growth rates and idiosyncratic income volatility. Thus, we conclude that financial globalization among countries with heterogeneous domestic financial markets can be an important factor for explaining the large external imbalances that have emerged across the United States, other industrial countries and emerging economies.
A Appendix: Data

**Emerging economies:** Argentina, Brazil, Chile, China, Colombia, Czech Republic, Egypt, Hungary, India, Indonesia, Israel, Jordan, Malaysia, Morocco, Pakistan, Peru, Philippines, Poland, Russia, South Africa, Korea, Thailand, Turkey, Hong Kong, Singapore, Saudi Arabia.

**Financial development indicators:** The International Monetary Fund (IMF (2006)) proposes an index of financial markets development for industrial countries. The index combines information from three core sub-indexes: an index of traditional bank intermediation, an index of new financial intermediation (i.e. intermediation through direct market instruments, such as asset-backed securities and derivatives, and/or non-bank intermediaries, such as hedge funds) and an index of general characteristics of financial markets (e.g. stock market turnover, investor protection, bond market capitalization, etc.). Countries with a higher index undertake a larger volume of financial intermediation through direct market instruments and are viewed as having attained a higher degree of financial development.

Abiad, Detragiache, and Tressel (2008) constructed an 82 country database of financial reforms for both industrialized and emerging economies over the period 1973-2002, with 7 dimensions of financial sector policies: 1) Credit controls and high reserve requirements; 2) Interest rate controls; 3) Entry barriers; 4) State ownership in the banking sector; 5) Capital account restrictions; 6) Prudential regulations and supervision of the banking sector; 7) Securities market policies. The financial liberalization index in the second panel of Figure 1 is the average of those indicators.

**Financial globalization index:** Chinn and Ito (2005) compiled an index of the degree of capital account openness for 163 countries from 1970 to 2004. The index is based on binary dummy variables that codify the restrictions on cross-border financial transactions reported in the IMF’s *Annual Report on Exchange Arrangements and Exchange Restrictions* (AREAER). The dummy
variables reflect the four major categories of restrictions: multiple exchange rates, restrictions on current account transactions, restrictions on capital account transactions, and requirements for the surrender of export proceeds. The index is the first standardized principal component of these four variables and it takes higher values for countries that are more open to cross-border capital transactions. The indices for country groups are computed by averaging the individual country indices, weighted by GDP.

**Foreign asset positions:** Lane and Milesi-Ferretti have constructed data on gross and net foreign assets and liabilities, for different instruments, over the period 1970-2004. See Lane and Milesi-Ferretti (2007). The NFA positions are calculated by aggregating the different assets and liabilities.

**B Appendix: Set of feasible contingent claims**

Suppose that agents have the ability to divert part of their income. Diversion is observable but not verifiable in a legal sense. If an agent diverts $x$, he or she retains $(1 - \phi)x$ while the remaining part, $\phi x$, is lost. We allow $\phi$ to be greater than 1. This can be interpreted as a fine or additional punishment. A similar assumption is made in Castro, Clementi, and MacDonald (2004) in an environment with information asymmetry.

Contracts are signed with financial intermediaries in a competitive environment. Financial contracts are not exclusive, meaning that agents can always switch to another intermediary from one period to the other. The set of state-contingent claims that an intermediary is willing to offer must be incentive-compatible.

Let $V_t(s, a)$ be the value function for an agent with current realization of shocks, $s = (w, z)$, and current net worth, $a$. The net worth is before consumption. After choosing the contingent claims $b(s_n)$, the next period value is $V_t(s_n, a(s_n))$, where $a(s_n) = w_n + z_n k^t + k P_{t+1} + b(s_n)$. In case of
diversion, the agent would claim that the realizations of the endowment and productivity were the lowest levels, $s_1 = (w_1, z_1)$, and divert $w_n - w_1 + (z_n - z_1)k^\nu$. In this process the agent retains $(1 - \phi)[w_n - w_1 + (z_n - z_1)k^\nu]$ and receives $b(s_1)$. Therefore, the net worth after diversion is:

$$w_1 + z_1k^\nu + (1 - \phi) \cdot \left[ w_n - w_1 + (z_n - z_1)k^\nu \right] + kP_{t+1} + b(s_1) =$$

$$a(s_1) + (1 - \phi) \cdot \left[ w_n - w_1 + (z_n - z_1)k^\nu \right]$$

and the value of diversion is:

$$V_t(s_n, a(s_1) + (1 - \phi) \cdot \left[ w_n - w_1 + (z_n - z_1)k^\nu \right])$$

Incentive-compatibility requires that the following holds for all $n = 1, \ldots, N$

$$V_t(s_n, a(s_n)) \geq V_t(s_n, a(s_1) + (1 - \phi) \cdot \left[ w_n - w_1 + (z_n - z_1)k^\nu \right])$$

It is important to emphasize that the financial intermediary can tell whether the agent is diverting but there is no court that can verify this and force the repayment of the diverted funds. Compared to the standard model with information asymmetries, this assumption is convenient because it simplifies the contracting problem when shocks are persistent. Also convenient is the assumption that financial contracts are not exclusive and agents can switch to other intermediaries from one period to the other without a cost. This further limits the punishments available to the current intermediary. Also notice that, although the new level of wealth after diversion is verifiable when a new contract is signed, this does not allow the verification of diversion because the additional resources could derive from lower consumption in previous periods, which is not verifiable. The fraction of lost income $\phi$ can be interpreted as the cost for hiding (making non-verifiable) the
diverted income and for hiding consumption. Again, the intermediary knows that the additional resources come from diversion but it cannot legally prove it.

The last assumption is limited liability. Agents can renegotiate negative values of net worth, and therefore, \( a(s_n) \geq 0 \). The agent’s problem reads:

\[
V_t(s, a) = \max_{c, k, b(s')} \left\{ U(c) + \beta \sum_{s'} V_{t+1}(s', a(s')) g(s, s') \right\}
\]

subject to

\[
a = c + kP_t + \sum_{s'} b(s') q(s, s')
\]

\[
a(s') = w' + z'k^\nu + kP_{t+1} + b(s')
\]

\[
V_t(s_n, a(s_n)) \geq V_t(s_n, a(s_1) + (1 - \phi) \cdot [w_n - w_1 + (z_n - z_1)k^\nu])
\]

\[
a(s_n) \geq 0
\]

Using standard arguments, we can prove that there is a unique solution and the function \( V_t(s, a) \) is strictly increasing and concave in \( a \).\(^{17}\) The strict monotonicity of the value function implies that the incentive-compatibility constraint can be written as:

\[
a(s_n) \geq a(s_1) + (1 - \phi) \cdot \left[ w_n - w_1 + (z_n - z_1)k^\nu \right]
\]

for all \( n = 1, \ldots, N \). This is the constraint we imposed on the original problem.

We arrived at this simple formulation of the enforcement constraints because of the particular environment we considered. With alternative assumption of information asymmetries and persistent shocks, the characterization of the optimal contract becomes more complicated. Because the qualitative properties are similar to the frictions considered here,\(^{18}\) we opted for the simpler route.

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\(^{17}\)The proof is facilitated by defining the variable \( x = k^\nu \). After making the change of variables \( k = x^{1/\nu} \), it can be easily proved that this is a standard concave problem.

\(^{18}\)See, for example, Fernandes and Phelan (2000).
Appendix: Analytical proofs

Proof of Proposition 1  In both economies we have that \( R(k, \bar{z}) = 1 + r_t \). Because with capital mobility there is a single worldwide interest rate, all agents employ the same input of capital \( k = 1 \). Therefore, the net position in the productive asset is zero. We want to show that the interest rate is smaller than the intertemporal discount rate. Suppose, on the contrary, that \( \beta(1 + r_t) \geq 1 \). Under this condition agents in country 1 will have non-negative consumption growth (see Lemma 1) and agents in country 2 will have positive consumption growth (see Lemma 2). This implies that worldwide consumption growth is positive which cannot be an equilibrium because aggregate income is constant. Therefore, the equilibrium must satisfy \( \beta(1 + r_t) < 1 \). Under this condition, agents in country 1 will experience negative consumption growth (see again Lemma 1) until the limited liability constraint (4) binds. Therefore, at some point, the net worth becomes zero for all agents. Because in country 1 the net holding of productive assets is equal to the domestic endowment of 1, the budget constraint becomes \( c_t + P_t + \sum_{w_{t+1}} b(w_{t+1})q(w_t, w_{t+1}) = 0 \). This implies \( \sum_{w_{t+1}} b(w_{t+1})q(w_t, w_{t+1}) < 0 \), that is, country 1 borrows from country 2 (the NFA is negative).

Q.E.D.

Proof of Proposition 2  Suppose that \( \beta(1 + r) \geq 1 \). Under this condition agents in country 1 will have non-negative consumption growth and agents in country 2 will have strictly positive consumption growth (Lemmas 1 and 2 apply also to the case with only investment shocks). This implies that worldwide consumption growth is positive which cannot be a steady state equilibrium. Therefore, \( \beta(1 + r_t) < 1 \). Under this condition agents in country 1 will experience negative consumption growth (see again Lemma 1) until the limited liability constraint (4) binds. Therefore, at some point, the net worth becomes zero for all agents. As in Proposition 1, this implies that the NFA position of country 1 becomes negative.
To show that country 1 has a positive net position in the productive asset, consider again the first order conditions (11)-(14). From these conditions we have that \( ER_t(k, z') = 1 + r \) in country 1 and \( ER_t(k, z') > 1 + r \) in country 2. The monotonicity of \( R_t \) with respect to \( k \) implies that the productive asset used by agents in country 1 is bigger than the productive asset used by agents in country 2. Because the supply is the same, country 1 must owns part of the productive asset of country 2.

What remains to be shown is that for country 1 the average return from the foreign productive investment is higher than the cost of its foreign liabilities. Even thought the marginal return from the productive asset is equalized to the interest rate, the concavity of the production function implies that the average return is higher than the interest rate. This compensates the managerial capital. *Q.E.D.*

\section*{D Appendix: Computational procedure}

We show first that the economy with contingent claims is equivalent to an economy where contingent claims are not allowed but agents face a different process for the exogenous shocks. We can then solve the equivalent economy where the agents’ problem is a standard portfolio choice over riskless and risky assets. After showing this, we describe the computational procedures used to solve for the steady state and transitional equilibria.

\subsection*{D.1 Equivalent economy}

Let \( \bar{b}_t \) be the expected next period value of contingent claims, that is, \( \bar{b}_t = \sum_{s_{t+1}} b(s_{t+1})g(s_t, s_{t+1}) \).

Then a contingent claim can be rewritten as \( b(s_{t+1}) = \bar{b}_t + x(s_{t+1}) \) where \( \sum_{s_{t+1}} x(s_{t+1})g(s_t, s_{t+1}) = 0 \). The variable \( \bar{b}_t \) can be interpreted as a non-contingent bond and \( x(s_{t+1}) \) is the pure insurance...
component of contingent claims. The law of motion for the next period assets becomes:

\[ a(s_{t+1}) = w_{t+1} + \sum_{j=1}^{I} k_{j,t} P_{j,t+1}^{D} + z_{j,t+1} A_{j,t}^{1-\nu} k_{j,t}^{\nu} + \tilde{b}_t + x(s_{t+1}) \]  \( (21) \)

Because agents will choose as much insurance as possible, the incentive-compatibility constraint will be satisfied with equality, that is,

\[ a(s_n) = a(s_1) + (1 - \phi) \cdot [w_n - w_1 + \sum_{j=1}^{I} (z_{j,n} - z_{j,1}) A_{j,t}^{1-\nu} k_{j,t}^{\nu}] \]

Using the law of motion for \( a \), the constraint can be rewritten as:

\[ x(s_n) - x(s_1) = -\phi \cdot [w_n - w_1 + \sum_{j=1}^{I} (z_{j,n} - z_{j,1}) A_{j,t}^{1-\nu} k_{j,t}^{\nu}] \]

which must hold for all \( n \in \{2,..,N\} \). The variables \( x(s_n) \) must also satisfy the zero-profit condition, that is,

\[ \sum_{n} x(s_n) g(s_t, s_n) = 0 \]

Therefore, we have \( N \) conditions and \( N \) unknowns. We can then solve for all the \( N \) values of \( x_n \).

The solution can be written as:

\[ x(s_n) = -\phi \cdot W_n(s_t) - \phi \cdot \sum_{j=1}^{I} Z_{j,n}(s_t) \cdot A_{j,t}^{1-\nu} k_{j,t}^{\nu} \]

where \( W_n(s_t) \) and \( Z_{j,n}(s_t) \) are exogenous variables defined as

\[ W_n(s_t) = w_n - \sum_{\ell} g(s_t, s_\ell) w_\ell \]

\[ Z_{j,n}(s_t) = z_{j,n} - \sum_{\ell} g(s_t, s_\ell) z_{j,\ell} \]
These variables depend on the current shocks because they affect the probability distribution for the next period shocks.

Define the following variables:

\[
\tilde{w}_n(s_t) = w_n - \phi \cdot W_n(s_t)
\]

\[
\tilde{z}_{j,n}(s_t) = z_{j,n} - \phi \cdot Z_{j,n}(s_t)
\]

These are transformations of the shocks. Using the transformed shocks, the law of motion for next period assets can be written as:

\[
a(s_n) = \tilde{w}_n(s_t) + \sum_j \left[ k_{j,t} P_{t+1}^j + \tilde{z}_{j,n}(s_t) \cdot A_{j,t}^{1-\nu} k_{j,t}^\nu \right] + \bar{b}_t
\]

Therefore, by using the transformed shocks \( \tilde{w}_n(s_t) \) and \( \tilde{z}_{j,n}(s_t) \), it is as if agents choose only non-contingent claims. Then the problem becomes a standard portfolio choice between risky assets, \( k_{j,t} \), and a riskless asset, \( \bar{b}_t \). Differences in financial development are captured by difference in the stochastic properties of the transformed shock. So, for example, if \( \phi = 0 \), we go back to the original shock because contingent claims are not feasible. If \( \phi = 1 \) and shocks are iid, the transformed shock becomes a constant. We are in the case of full insurance. Intermediate values of \( \phi \) allow only for partial insurance. In the computation we will solve the portfolio choice in the transformed model.

### D.2 Steady state equilibrium

1. Choose a grid for asset holdings \( a \).

2. Guess the steady state interest rate, \( r \), and the prices \( \{P^j\}_{j=1}^I \).

3. Using the first-order conditions, solve for the optimal portfolio choices at each grid point of
a and for each s, by iterating on the policy rules. The solutions at each grid point are joined with piece-wise linear functions.

4. Find the steady state distribution of agents using the decision rules and compute the clearing conditions for the risky and riskless assets.

5. Update the guesses for the interest rate and the prices of the productive assets (step 2) until the market clearing conditions are satisfied.

D.3 Transitional equilibrium

1. Solve for the initial and final steady states (autarky and mobility).

2. Choose the number of transition periods $T$. This number should be sufficiently large to allow the economy to reach, approximately, the new steady state in $T$ periods.

3. Guess transition sequences for the interest rates, $\{r_t\}_{t=1}^T$, and for the price of the productive assets $\{\{P_j^t\}_{j=1}^I\}_{t=1}^T$. The final prices $\{P_{T+1}^j\}_{j=1}^I$ are set to the steady state values with mobility found in step 1.

4. Using the first-order conditions, solve for the optimal portfolio choices backward starting from $T$. This provides the sequence of optimal decision rules at $t = 1, 2, ..., T$.

5. Using the optimal decision rules, find the sequence of distributions and compute the market-clearing conditions at time $t = 1, 2, ..., T$.

6. Update the guess for the sequences of the interest rates and the prices of the productive assets (step 3) until the market-clearing conditions are satisfied for each $t = 1, 2, ..., T$. 

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References


Figure 1: Indices of financial markets heterogeneity. The index in panel A is from IMF (2006). The index in panel B is from Abiad, Detragiache and Tresselo (2008). See appendix A for the definition of variables.
Figure 2: Indices of financial openness. The index in panel A is from Chinn and Ito (2005). The index in panel B is constructed using data from Lane and Milesi-Ferretti (2006). See appendix A for the definition of variables.
Figure 3: Net foreign asset positions in debt instruments and risky assets. The graphs are constructed using data from Lane and Milesi-Ferretti (2006). See appendix A.
Figure 4: Steady state equilibria with heterogeneous financial conditions.
Figure 5: Policy rules as functions of net worth.
Figure 6: Transition dynamics after capital markets liberalization.
Figure 7: Welfare effects of financial integration.
Table 1: Steady state with and without capital mobility.

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<th>Autarky</th>
<th>Capital mobility</th>
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<tr>
<td></td>
<td>C1</td>
<td>C2</td>
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<tr>
<td>A) Both shocks</td>
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<td>Prices of productive assets</td>
<td>3.08</td>
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<tr>
<td>Bonds</td>
<td>-</td>
<td>-</td>
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<tr>
<td>Welfare gains from liberalization</td>
<td>-</td>
<td>-</td>
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<tr>
<td>B) Endowment shocks only</td>
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<td></td>
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<td>Prices of productive assets</td>
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<td>Welfare gains from liberalization</td>
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<td>C) Investment shocks only</td>
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<td>-</td>
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<tr>
<td>Welfare gains from liberalization</td>
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Notes: Foreign asset positions are in percentage of domestic income (endowment plus domestic investment income). Welfare gains are in percentage of consumption.
Table 2: Sensitivity to the cross-country correlation of shocks.

<table>
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<th>Capital mobility</th>
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<td>C1</td>
<td>C2</td>
</tr>
<tr>
<td></td>
<td>C1</td>
<td>C2</td>
</tr>
<tr>
<td>A) Shocks are partially correlated (correlation=0.5)</td>
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<tr>
<td>Prices of productive assets</td>
<td>3.08</td>
<td>3.40</td>
</tr>
<tr>
<td>Returns on productive assets</td>
<td>4.81</td>
<td>4.30</td>
</tr>
<tr>
<td>Standard deviation of returns</td>
<td>8.11</td>
<td>11.76</td>
</tr>
<tr>
<td>Interest rate</td>
<td>3.25</td>
<td>2.60</td>
</tr>
<tr>
<td>Net foreign asset positions</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Productive assets</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Bonds</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Welfare gains from liberalization</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

| B) Shocks are perfectly correlated (correlation=1) |         |                 |
| Prices of productive assets  | 3.08    | 3.40            |
| Returns on productive assets | 4.81    | 4.30            |
| Standard deviation of returns| 8.11    | 11.76           |
| Interest rate                | 3.25    | 2.48            |
| Net foreign asset positions  | -       | -               |
| Productive assets            | -       | -               |
| Bonds                        | -       | -               |
| Welfare gains from liberalization |        |                 |

Notes: See Table 1.
Table 3: Sensitivity to alternative assumptions about the nature of $\phi$.

<table>
<thead>
<tr>
<th></th>
<th>Autarky</th>
<th>Capital mobility</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$C_1$</td>
<td>$C_2$</td>
</tr>
<tr>
<td>A) Source based only for residents of $C_2$</td>
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<tr>
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</tr>
<tr>
<td>Returns on productive assets</td>
<td>4.81</td>
<td>4.30</td>
</tr>
<tr>
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<td>8.11</td>
<td>11.76</td>
</tr>
<tr>
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<td>2.60</td>
</tr>
<tr>
<td>Net foreign asset positions</td>
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<tr>
<td>Productive assets</td>
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<td>-</td>
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<tr>
<td>Welfare gains from liberalization</td>
<td>2.67</td>
<td></td>
</tr>
<tr>
<td>B) Source based only for residents of $C_1$</td>
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<tr>
<td>Prices of productive assets</td>
<td>3.08</td>
<td>3.40</td>
</tr>
<tr>
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<td>4.81</td>
<td>4.30</td>
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<tr>
<td>Standard deviation of returns</td>
<td>8.11</td>
<td>11.76</td>
</tr>
<tr>
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<td>2.60</td>
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<tr>
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<tr>
<td>Productive assets</td>
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<td>-</td>
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<tr>
<td>Bonds</td>
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</tr>
<tr>
<td>Welfare gains from liberalization</td>
<td>2.87</td>
<td></td>
</tr>
<tr>
<td>C) Partially source based for residents of both countries</td>
<td></td>
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<tr>
<td>Prices of productive assets</td>
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<td>3.40</td>
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<tr>
<td>Returns on productive assets</td>
<td>4.81</td>
<td>4.30</td>
</tr>
<tr>
<td>Standard deviation of returns</td>
<td>8.11</td>
<td>11.76</td>
</tr>
<tr>
<td>Interest rate</td>
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<td>Net foreign asset positions</td>
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<tr>
<td>Bonds</td>
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<tr>
<td>Welfare gains from liberalization</td>
<td>2.71</td>
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<tr>
<td>D) Source based for residents of both countries</td>
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<tr>
<td>Prices of productive assets</td>
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<td>4.30</td>
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<tr>
<td>Standard deviation of returns</td>
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<td>11.76</td>
</tr>
<tr>
<td>Interest rate</td>
<td>3.25</td>
<td>2.60</td>
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<td>Net foreign asset positions</td>
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<tr>
<td>Productive assets</td>
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<td>-</td>
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<tr>
<td>Bonds</td>
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</table>

Notes: See Table 1.
Table 4: Steady state with heterogeneity in $\phi$ and $a$.

<table>
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<th>Autarky</th>
<th>Capital mobility</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C1</td>
<td>C2</td>
</tr>
<tr>
<td>A) Differences in $a$ only: $a_1 = -1$, $a_2 = 0$, $\phi^1 = \phi^2 = 0.35$</td>
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<tr>
<td>Prices of productive assets</td>
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<td>Productive assets</td>
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<td>-</td>
</tr>
<tr>
<td>Bonds</td>
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<td>-</td>
</tr>
<tr>
<td>Welfare gains from liberalization</td>
<td>2.99</td>
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</tr>
<tr>
<td>B) Differences in both: $a_1 = -1$, $a_2 = 0$, $\phi^1 = 0.35$, $\phi^2 = 0$</td>
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<td>Prices of productive assets</td>
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</table>

Notes: See Table 1.
Table 5: Steady state in the three-country economy.

<table>
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<th>Autarky</th>
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</thead>
<tbody>
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<td></td>
<td>C1</td>
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<td>C3</td>
<td>C1</td>
</tr>
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<td>-</td>
<td>-82.24</td>
</tr>
</tbody>
</table>

Notes: The heterogeneous parameters are $\phi = (0.5, 0.5, 0)$, $\omega = (-1, 0, 0)$, $\mu = (0.3, 0.5, 0.2)$. See also Table 1.
Table 6: Steady state in the three-country economy with heterogeneity in financial development, growth and income volatility.

<table>
<thead>
<tr>
<th></th>
<th>Autarky</th>
<th>Capital mobility</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C1</td>
<td>C2</td>
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<tr>
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<td>2.95</td>
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<tr>
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<tr>
<td>Returns on productive</td>
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<td>5.05</td>
</tr>
<tr>
<td>assets</td>
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<td>3.53</td>
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<td>-</td>
</tr>
<tr>
<td>Bonds</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

Notes: The heterogeneous parameters are \( \phi = (0.5, 0.5, 0) \), \( \alpha = (-1, 0, 0) \), \( \beta = (0.925, 0.925, 0.863) \), \( \Delta_w = (0.6, 0.6, 0.9) \), \( \Delta_z = (2.5, 2.5, 3.75) \), \( \mu = (0.3, 0.5, 0.2) \). See also Table 1.