

# Financial Institution Dynamics and Capital Regulations

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- Regulatory discussions during the financial crisis:
  - insufficient capitalization of banks;
  - bank dividend payouts (Acharya, Gujral, Kulkarni and Shin 2011);
  - executive compensation (Financial Stability Forum 2009).
  
- Basel III capital regulations include:
  - Capital conservation buffer (2.5%) + min. capital requirement (4.5%).
  - Distribution of earnings will be restricted if the buffer is drawn down.

# Objective and Issues with Existing Macro-Banking Models

- Our goal: Analysis of macroeconomic implications of minimum capital requirement and conservation buffer in Basel III.
- To do so, we need a model environment whereby over-payment of dividends and executive bonuses naturally arise.
- Existing macro-banking models typically have
  - no outside equity issuance, and/or
  - manager's incentive perfectly aligned with shareholders' interests.
- For today, focus on analyzing an equilibrium without capital regulations to discuss why they may be necessary.

# Our Paper

- A macro-banking model featuring a manager who controls the bank and:
  - ① issues outside equity and dividends (*time inconsistency* problem);
  - ② is *impatient*; and
  - ③ faces *moral hazard* through limited liability.
- These elements allow us to analyze capitalization and risk taking of banks simultaneously.

# Main Results

- Under-capitalization due to time-inconsistency problem. Time inconsistency problems exist because of:
  - Reoptimization of dividend payment, and
  - Dilution of existing equities.
- Excessive leverage by banks due to moral hazard.
- Need for both capital conservation buffer and minimum capital requirement.

# Bank Manager's Problem with Implicit Loans

- Time-inconsistency issue

$$V(n) = \max_{\{c,z,y,e,m\}} \{u(c) + \chi V(f(y))\}$$

subject to

$$c + z + y = n + \alpha m$$

$$m = e\beta\Omega(f(y)).$$

- In equilibrium,

$$\Omega(n) = z(n) + \beta [1 - e(n)] \Omega(f(y(n))).$$

- Bonus incentive

$$c \leq \psi z$$

- Anti-dilution protection

$$e \leq \frac{m}{(n - \gamma c - z) + m}$$

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## Generalized Euler Equation:

$$u_c = \frac{\chi(1-\alpha)f_y}{1 + \alpha\beta\gamma\psi f_y z'_n - \alpha\beta f_y} u'_c.$$

- Knowing that tomorrow's manager will have his own interests, today's manager takes it into account through  $z'_n \equiv \frac{\partial z'}{\partial n'}$ .
- GEE collapses to a usual Euler equation when  $\alpha = 0$ :  $u_c = \chi f_y u'_c$ .
- The manager considers the “cost” of increasing  $y$  through

$$\Omega(f(y)) = -\psi\gamma z(f(y)) + f(y).$$

# Under-Capitalization in MPE (Steady State)

- Markov Perfect Equilibrium:

$$f_y^{ME} = \frac{1}{\chi(1-\alpha) + \alpha\beta(-\gamma\psi z'_n + 1)}$$

- Commitment Equilibrium:

$$f_y^{CM} = \frac{1}{\chi(1-\alpha) + \alpha\beta}$$

- Social Planner

$$f_y^{SP} = \frac{1}{\beta}$$

- Insufficient capitalization if  $z'_n > 0$ .

$$y^{SP} > y^{CM} > y^{ME}.$$

# Numerical Results (Steady State)

- Functional forms:  $u(c) = \log(c)$ ,  $f(y) = y^\nu$ .
- Parameter values:

$\alpha$	$\beta$	$\gamma$	$\chi$	$\psi$	$\nu$
0.98	0.99	0.5	0.9	1.0	0.9

- Results:  $z'_n = 0.036 > 0$ . Thus,  $y^{CM} > y^{ME}$ .

## Commitment Equilibrium vs Markov Perfect Equilibrium

	$y$	$z$	$\Omega$	$z/\Omega$	$m/\Omega$
Commitment	0.31	0.035	0.33	0.10	0.09
Markov Perfect	0.26	0.034	0.28	0.12	0.11

# Model with Loan, Deposit and Default

$$V(n; \Omega) = \max_{\{c, z, y, \ell, d, e, m\}} \left\{ u(c) + \chi \int_{\eta_*(d, y)} V(F(d, y, \eta'); \Omega) G(d\eta') + \chi \underline{V} G(\eta'_*(d, y)) \right\}$$

subject to

$$c + z + y = n + \alpha m$$

Budget Constraint

$$\ell = d + y$$

Balance Sheet

$$m = e \beta \int_{\eta_*(d, y)} \Omega(F(\ell, y, \eta')) dG(\eta')$$

Equity Issuance

$$c \leq \psi z$$

Compensation Constraint

$$e = \frac{m}{(n - \gamma c - z) + m}$$

Dilution Constraint

$$F(d, y, \eta') = R(d + y)^{1-\nu} \eta' - [R_d + h(d)] \cdot d$$

Loan Return

$$\eta_*(d, y) \text{ given by } F(d, y, \eta'_*) = 0$$

Default Threshold

## The model simplifies to...

$$V(n) = \max_{z,y} \left\{ u(\psi z) + \chi \int_{\eta_*(\hat{d}(z,y,n),y)} V \left( F \left( \hat{d}(z,y,n), y, \eta' \right) \right) G(d\eta') \right. \\ \left. + \chi \underline{V} G \left( \eta_*(\hat{d}(z,y,n),y) \right) \right\}$$

- Deposit,  $\hat{d}$ , is determined through the bud. const. given  $(z, y, n)$ :

$$[1 + \psi - \alpha(1 + \gamma\psi)]z + y = (1 - \alpha)n + \alpha\beta \int_{\eta_*(\hat{d},y)} F(\hat{d}, y, \eta') G(d\eta') \\ - \alpha\beta\gamma\psi \int_{\eta_*(\hat{d},y)} z \left( F(\hat{d}, y, \eta') \right) G(d\eta')$$

# Optimality conditions

[z]

$$\psi u_c + \chi \left[ \int_{\eta_*(\hat{d}, y)} V'_n F_d G(d\eta') + [\underline{V} - V(0)] G(\eta_*) \eta_{*d} \right] \hat{d}_z = 0$$

[y]

$$\int_{\eta_*(\hat{d}, y)} V'_n \left( F_d \hat{d}_y + F_y \right) G(d\eta') + [\underline{V} - V(0)] G(\eta_*) \left[ \eta_{*d} \hat{d}_y + \eta_{*y} \right] = 0$$

[envelope]

$$V_n(n) = \chi \left[ \int_{\eta_*(\hat{d}, y)} V'_n F_d G(d\eta') + [\underline{V} - V(0)] G(\eta_*) \eta_{*d} \right] \hat{d}_n$$

# Generalized Euler Equations

[y]

$$\psi u_c \frac{\widehat{d}_y}{\widehat{d}_z} = \chi \int_{\eta_*(\widehat{d}, y)} \frac{\psi(1-\alpha)}{1+\psi-\alpha(1+\gamma\psi)} u'_c F_y G(d\eta') - \chi [\underline{V} - V(0)] G(\eta_*) \eta_{*y}$$

[z]

$$\psi u_c = \chi \left[ - \int_{\eta_*(\widehat{d}, y)} V'_n F_d G(d\eta') + [V(0) - \underline{V}] G(\eta_*) \eta_{*d} \right] \widehat{d}_z$$

# GEEs continued

[y]

$$0 = \psi u_c \cdot \frac{1}{1+\psi-\alpha(1+\gamma\psi)} \left\{$$

$-1$  direct loss in consumption from  $y \uparrow$

$+\alpha\beta \int_{\eta_*(\hat{d},y)} (1 - \gamma\psi z'_n) F_y G(d\eta')$  gain in equity valuation from more loans

$+\alpha\beta\gamma\psi z(0) G(\eta_*) \eta_{*y}$  gain in equity valuation from lower default

$+\chi \int_{\eta_*(\hat{d},y)} \frac{\psi(1-\alpha)}{1+\psi-\alpha(1+\gamma\psi)} u'_c F_y G(d\eta')$  gain in future (consumption) from more loans

$+\chi [V(0) - \underline{V}] G(\eta_*) \eta_{*y}$  gain in continuation value from lower default



# Two State Example

- Suppose  $\eta' \in \{0, 1\}$  and  $h = \kappa \cdot (\ell - y)$ . Let  $p_1 = \Pr(\eta' = 1)$ .
- Long-surviving bankers' leverage and capital can be ordered as

$$\text{leverage}^{ME} > \text{leverage}^{CM} > \text{leverage}^{SP},$$

$$y^{ME} < y^{CM} < y^{SP}.$$

## Proof (Step 1)

- Compare a Markovian manager and a committed manager.
- Regardless of com. tech.,  $\ell(y)$  is the same under moral hazard.

$$D_{\ell}F(\ell(y), y, 1) = 0.$$

- DRS implies  $d\ell(y)/dy < 1$  and leverage is decreasing in  $y$ .
- Again,  $y^{ME} < y^{CM}$  due to time inconsistency. Hence,

$$\text{leverage}^{ME} > \text{leverage}^{CM}.$$

## Proof (Step 2)

- Compare a committed banker and the social planner.
- Only the banker is protected by limited liability.
- Solutions to  $d$  and  $\ell$  satisfy  $d^{CM} > d^{SP}$  and  $\ell^{CM} < \ell^{SP}$ :

$$d^{CM} = \frac{p_1^{-1} [\chi(1-\alpha) + \alpha\beta]^{-1} - R_d}{2\kappa} > \frac{\beta^{-1} - R_d}{2\kappa} = d^{SP},$$

$$\ell^{CM} = [[\chi(1-\alpha) + \alpha\beta] p_1 (1-\gamma) R]^{1/\gamma} < [\beta p_1 (1-\gamma) R]^{1/\gamma} = \ell^{SP}$$

- This implies that  $y^{CM} < y^{SP}$ . As a result,

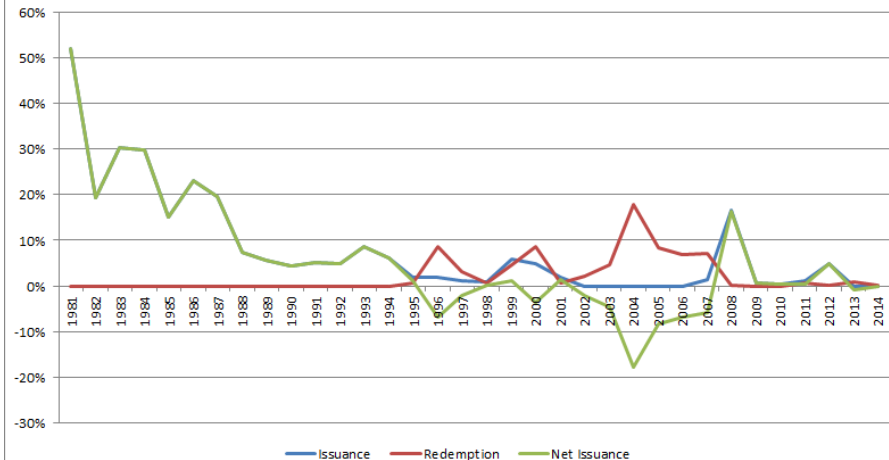
$$\text{leverage}^{CM} > \text{leverage}^{SP},$$

# Conclusion

- Time inconsistency problem regarding outside equity issuance leads bankers to pay excessive dividends and accumulate insufficient capital.
- Moral hazard problem leads to too much borrowing and thus excessive leverage of banks.
- Minimum capital requirement alone may not be adequate to promote capital accumulation. Capital conservation buffer may be an effective policy instrument.
- What's next?
  - Global solution (non-steady-state analysis).
  - Quantitative analysis of capital regulations.
  - Markovian evolution of banking industry.
  - Aggregate shocks.
  - General equilibrium.

# Equity Issuance by Banks in Canada

## Big 6 Common Share Issuance and Redemption



# Dividend Payout by Banks in Canada

