

Course in Heterogeneity: Econ 081

I: Reassessing the Role of Heterogeneity for Business Cycles

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HETEROGENEITY AND INEQUALITY ARE A SIGN OF THE TIMES





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 - Health and Longevity
- But as Macroeconomists, should we care?





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 - There is a lot of wealth that can be used efficiently to weather changes in available resources.
- The Great Recession has highlighted its shortcomings: How come we got such a large recession.

NEOCLASSICAL HETEROGENEOUS AGENT & BUSINESS CYCLES



AIYAGARI-BEWLEY-HUGGETT-IMROHOROLU MODELS WITH AGGREGATE SHOCKS



- Heterogeneous Households only (just for this talk).

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- Why could they generate larger fluctuations?
 - First set of Empirical Reasons
 1. Recessions hit (lower earnings, more unemployment) more vulnerable (poor) households more.
 2. Poor households have a higher Marginal Propensity to Consume out of income than rich households Johnson, Parker, and Souleles (2004), Misra and Surico (2014).



Heterogeneity (Inequality) in 2006:
Marginal Distributions

	y	c	a	SCF 07 a
Mean (2006\$)	62,549	43,980	291,616	497,747



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- a: Bottom 40% holds basically no wealth
- y, c: less concentrated

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a	% Share of:		Exp.Rate c/y (%)
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- 80% poorest account for 63% of consumption

NEOCLASSICAL HETEROGENEOUS AGENT & BUSINESS CYCLES



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 - 3.1 Nonlinear decision rules (at least on the low levels of income and wealth)
 - 3.2 A lot of agents in the states where their behavior is non linear (close to zero cash in hand).

ORIGINAL FINDINGS: HETEROGENEITY DOES NOT MATTER





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 2. Moreover, most agents are in the essentially linear part of the state space
- Heterogeneous agents models are like Rep Agent models for business cycle purposes. Also confirmed in life-cycle models.

WHY IN THOSE MODELS HETEROGENEITY DID NOT MATTER MUCH?





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 3. Large enough shocks

A FIRST UPDATE TO HETEROGENEOUS AGENT MODELS



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- Unemployment insurance system with size $\rho = 50\%$.



Net Worth	Data		Model
	% Share held by:		
	PSID, 06	SCF, 07	
Q1	-0.9	-0.2	0.3
Q2	0.8	1.2	1.2
Q3	4.4	4.6	4.7
Q4	13.0	11.9	16.0
Q5	82.7	82.5	77.8
90 – 95	13.7	11.1	17.9
95 – 99	22.8	25.3	26.0
Top 1%	30.9	33.5	14.2
Gini	0.77	0.78	0.77

- Get's inequality almost right at the very bottom



a Quintile	% Share of:				%c/y	
	y		c			
	Data	Model	Data	Model	Data	Model
Q1	8.6	6.0	11.3	6.6	92.2	90.4
Q2	10.7	10.5	12.4	11.3	81.3	86.9
Q3	16.6	16.6	16.8	16.6	70.9	81.1
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- Rudimentary life cycle is crucial for level of consumption rates and their decline with wealth.

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- If we were to think of Endogenous Labor, it would be Worse (Guerrieri-Lorenzoni-2009)





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- The main feature is to imply a slightly larger drop in consumption to that in Rep agent Models.

WHERE DO WE GO FROM HERE





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- These margins open the door to other type of shocks (financial shocks, government policy shocks, international shocks).





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- Expenditures play a role and adjustment is costly.
 - These are mechanisms that transform a drop in consumption into drops in TFP without reallocation of output to investment. Triggered by drops in Consumption.



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 4. Some labor market frictions that limit wage adjustments.



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 3. Frictions in the goods markets that generate movements in measured GDP.
 4. Some labor market frictions that limit wage adjustments.
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A recession triggered by a shock to households' ability to borrow

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- Most of consumption is non tradable and non investable.





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$$V(\epsilon, e, a) = \max_{c_i, I_N, h, d} u(c, h, d) + \beta \sum_{\epsilon', e', \theta'} \pi_{\theta, \theta'}^\theta \pi_{e'|e, \epsilon}^w \pi_{\epsilon, \epsilon'}^\epsilon V[\epsilon', e', a'(b, h)] \quad \text{s.t.}$$



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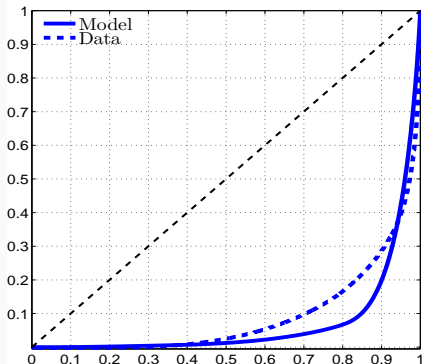
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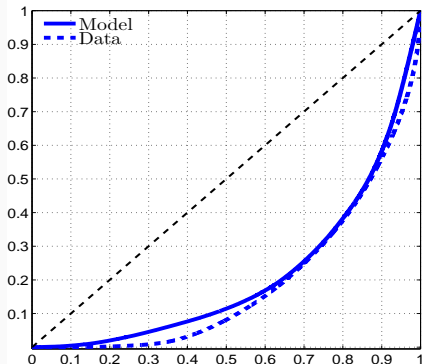
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- Some additional parameters involve the transition and are specified later



Network



Housing



1 Putting the Model to Use: An Experiment





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- We look at the transition. It involves solving for the steady state and then iterating backwards (with the additional problem of solving for equilibrium prices. Hard, but not too hard. Dynare can do it.)





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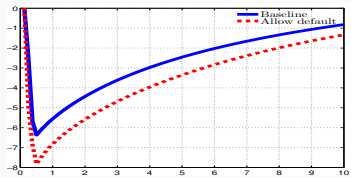


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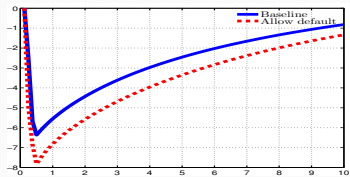
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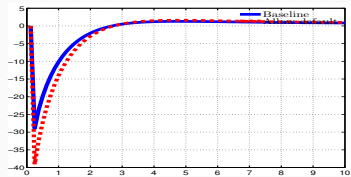
- Like in all heterogeneous agents models, more frictions imply that in the long run output and wealth end up being higher.
- But in our economies the transition is associated to a recession.



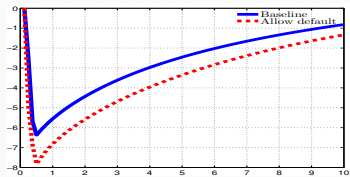
Consumption



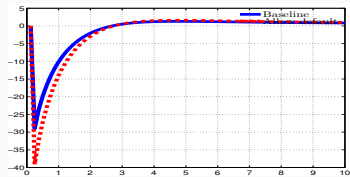
Consumption



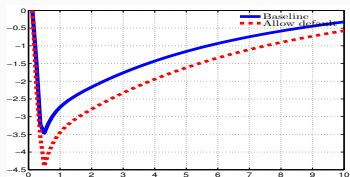
Investment



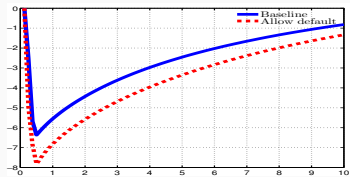
Consumption



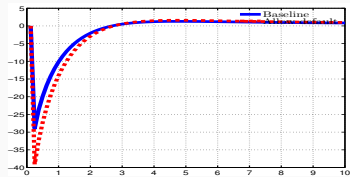
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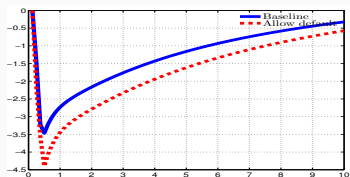
Output



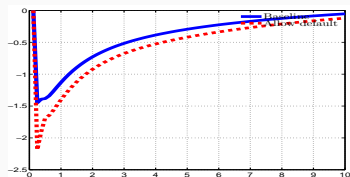
Consumption



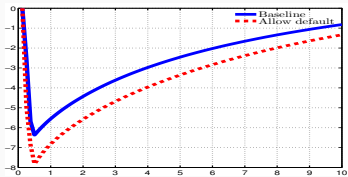
Investment



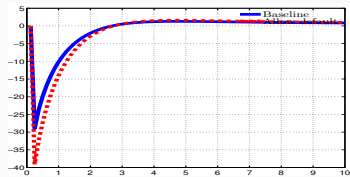
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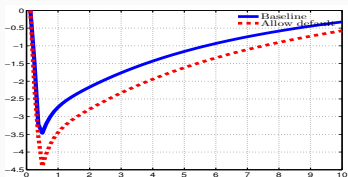
TFP



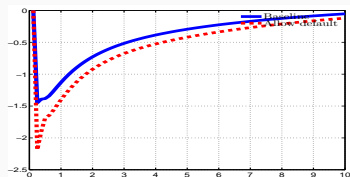
Consumption



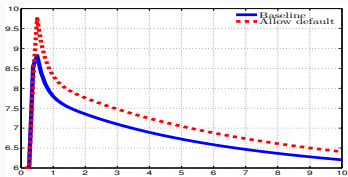
Investment



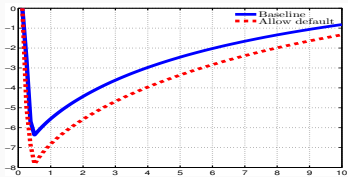
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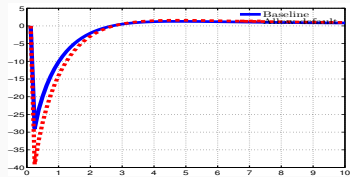
TFP



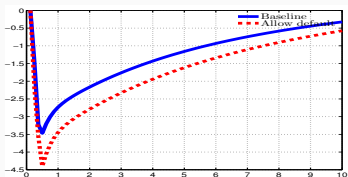
Unemployment rate



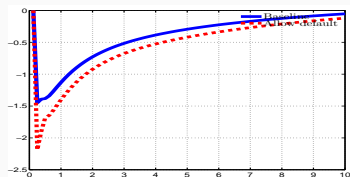
Consumption



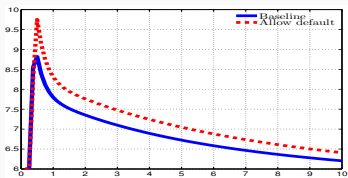
Investment



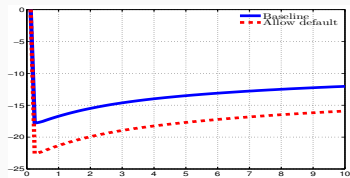
Output



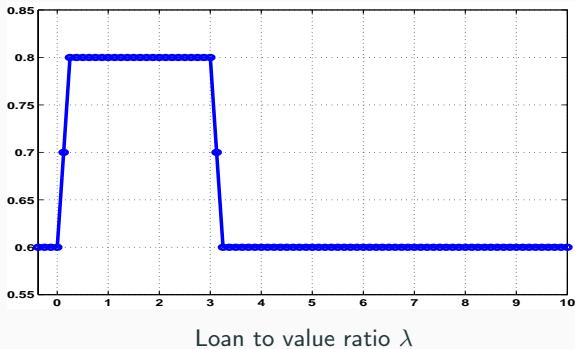
TFP



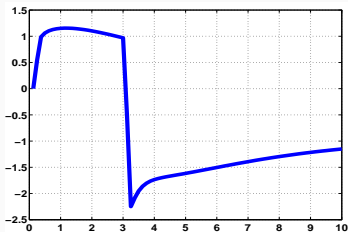
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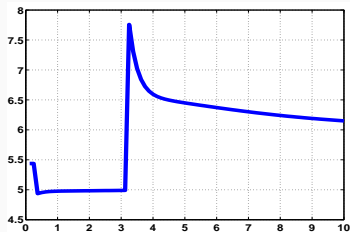
Housing Prices



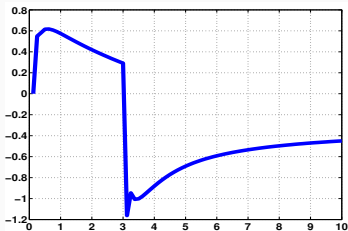
ANOTHER EXPERIMENT A CREDIT CYCLE



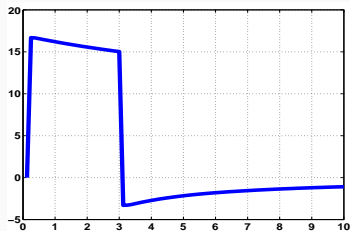
Real output



Unemployment rate



TFP



Housing price



- MIT shocks are NOT the way to study fluctuations.
- Traditionally very complicated methods have been proposed. Some of them based on *quasilinearity* or aggregate capital is the only thing that matters (Krusell and Smith (97,98)) interesting really happens. There are modern linearization versions based on Reiter such as Ahn et al. (17) and Childers (17).
- They approximate somehow the distribution of agents and look for its equilibrium law of motion.

BUT WE CAN DO A LOT BETTER THAN THAT





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2 Conclusion





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- Not only Heterogeneity of households but of firms and financial entities.

Thank You for Coming and
Listening!